

# Working with network data

Jim Bagrow

[james.bagrow@uvm.edu](mailto:james.bagrow@uvm.edu)

[bagrow.com](http://bagrow.com)

Complex Networks

Winter Workshop

2021-01-05



The University  
of Vermont



VERMONT  
COMPLEX SYSTEMS CENTER

**About myself**

# Understanding networks from data

Community detection

Applied to data

## Link communities reveal multiscale complexity in networks

Yong-Yeol Ahn<sup>1,2\*</sup>, James P. Bagrow<sup>1,2\*</sup> & Sune Lehmann<sup>3,4\*</sup>

Ahn *et al.* (2010)

## Mesoscopic Structure and Social Aspects of Human Mobility

James P. Bagrow<sup>1,2\*</sup>, Yu-Ru Lin<sup>3,4</sup>

Bagrow & Lin (2012)

## A Local Method for Detecting Communities

James P. Bagrow<sup>1</sup> and Erik M. Boltt<sup>2,1</sup>

<sup>1</sup> Department of Physics, Clarkson University, Potsdam, NY 13699-5820, USA.

<sup>2</sup> Department of Math and Computer Science, Clarkson University, Potsdam, NY 13699-5815, USA.

Bagrow & Boltt (2005)

PHYSICAL REVIEW E **85**, 066118 (2012)

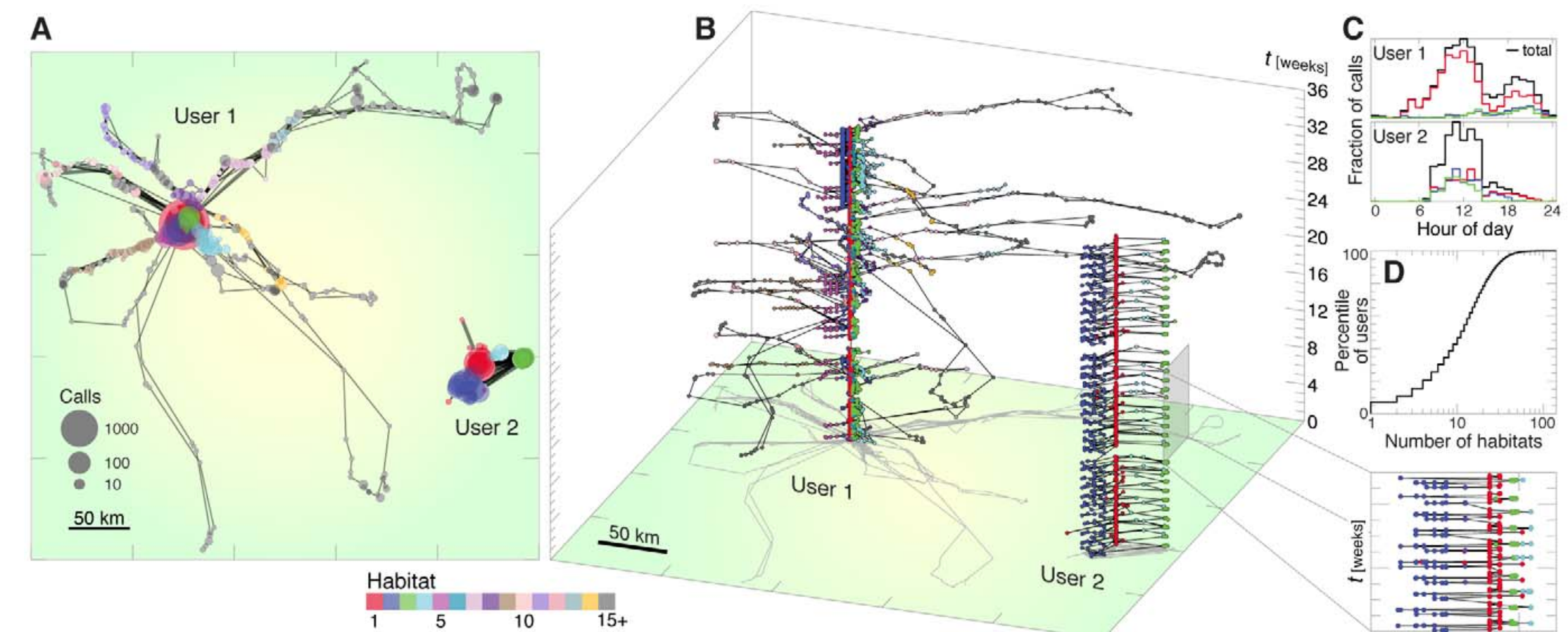
## Communities and bottlenecks: Trees and treelike networks have high modularity

James P. Bagrow\*

Department of Engineering Sciences and Applied Mathematics, Northwestern Institute on Complex Systems,  
Northwestern University, Evanston, Illinois 60208, USA

(Received 2 January 2012; published 15 June 2012)

Bagrow (2012)



# Data + Models

## *Robustness and modular structure in networks*

JAMES P. BAGROW

Mathematics & Statistics, University of Vermont, Burlington, VT, USA  
and

Center for Complex Network Research, Northeastern University, Boston, MA, USA  
(e-mail: james.bagrow@uvm.edu)

SUNE LEHMANN

DTU Informatics, Technical University of Denmark, Kgs Lyngby, Denmark  
and

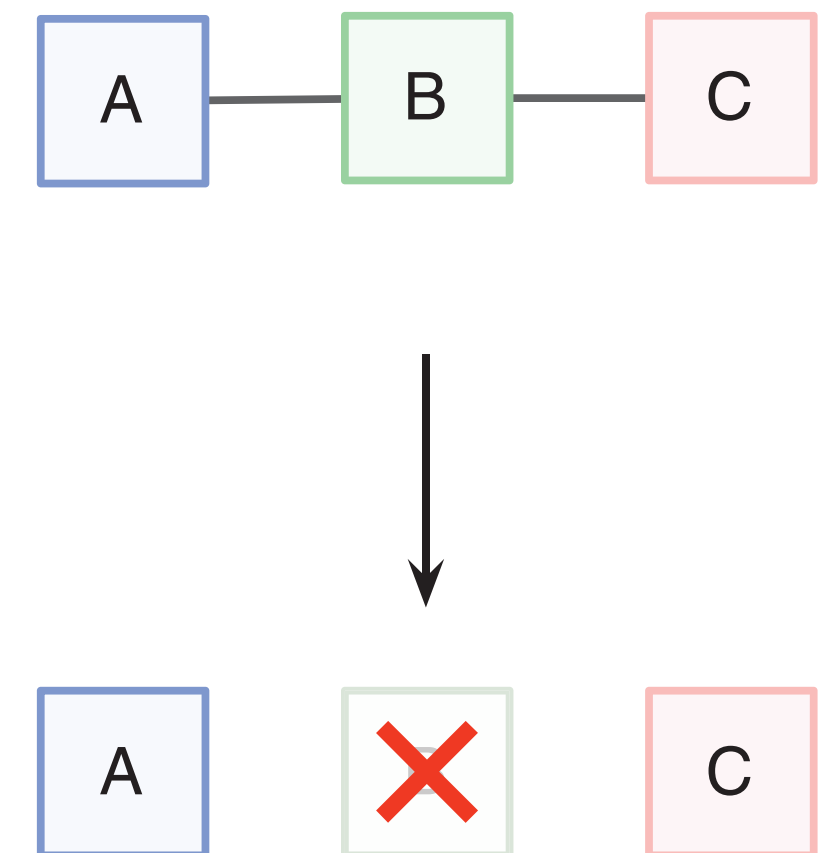
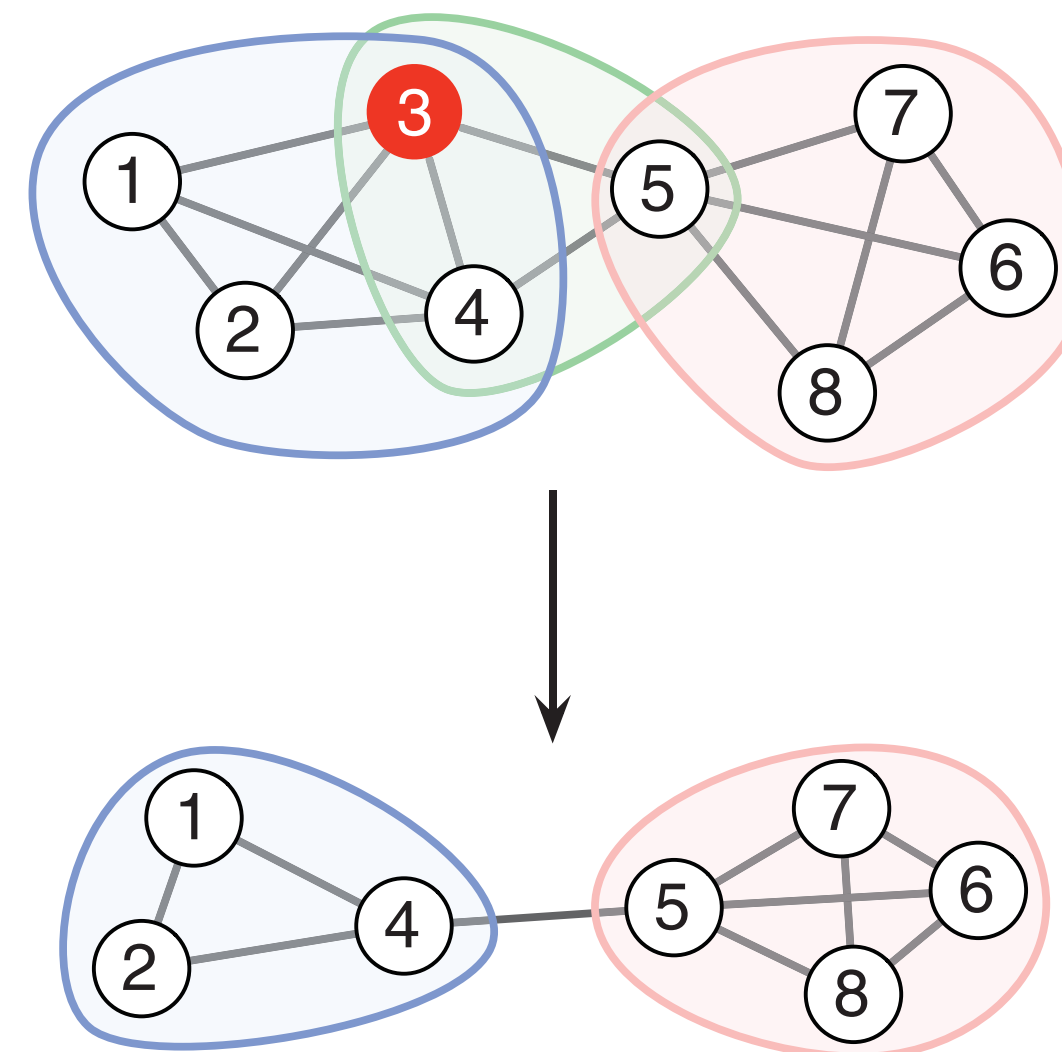
College of Computer and Information Science, Northeastern University, Boston, MA, USA  
(e-mail: sljo@dtu.dk)

YONG-YEOL AHN

School of Informatics & Computing, Indiana University, Bloomington IN, USA  
and

Center for Complex Network Research, Northeastern University, Boston, MA, USA  
(e-mail: yyahn@indiana.edu)

How does missing data change the appearance of detected communities?



# Data + Models

## The quoter model: A paradigmatic model of the social flow of written information

James P. Bagrow<sup>1,a)</sup> and Lewis Mitchell<sup>2,b)</sup>

<sup>1</sup>Department of Mathematics and Statistics, University of Vermont, Burlington, Vermont 05405, USA

<sup>2</sup>School of Mathematical Sciences, North Terrace Campus, The University of Adelaide, Adelaide, South Australia 5005, Australia

(Received 31 October 2017; accepted 23 February 2018; published online 11 July 2018)

## Measuring the flow of information between individuals

nature  
human behaviour

LETTERS

<https://doi.org/10.1038/s41562-018-0510-5>

### Information flow reveals prediction limits in online social activity

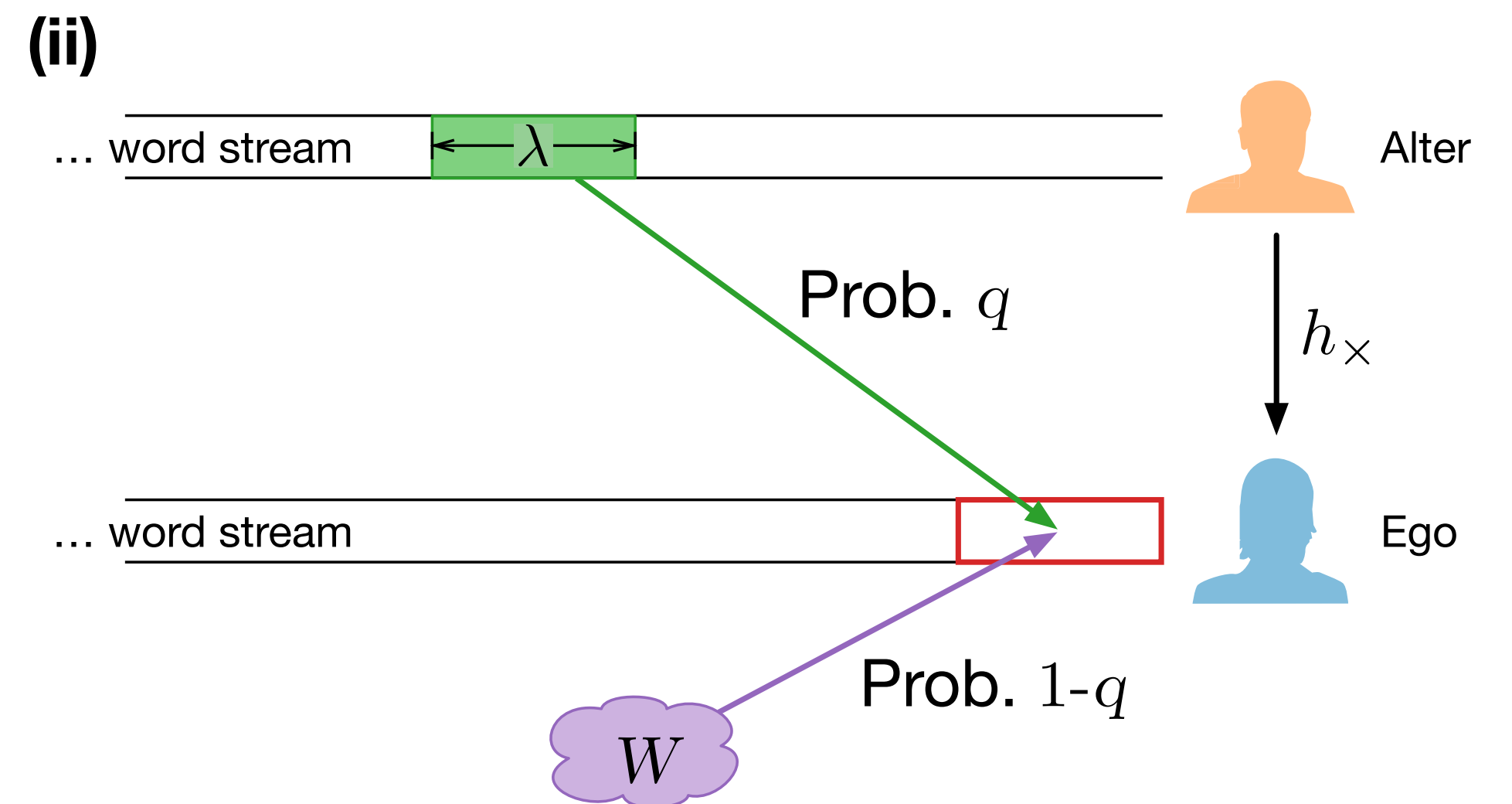
James P. Bagrow<sup>1,2\*</sup>, Xipei Liu<sup>1,2</sup> and Lewis Mitchell<sup>1,2,3\*</sup>

Modern society depends on the flow of information over online social networks, and users of popular platforms generate substantial behavioural data about themselves and their social ties<sup>1-5</sup>. However, it remains unclear what fundamental limits exist when using these data to predict the activities and interests of individuals, and to what accuracy such predictions can be made using an individual's social ties. Here, we show

postings to online social platforms present a unique opportunity to explore the textual content of messages in conjunction with their timings, giving a richer understanding of social ties.

Information theory allows us to mathematically quantify the information contained in data and is well suited to data in the form of online written communication. Although the mathematical definition of information is somewhat distinct from our com-

- (i) Alter: Hey, let's go to the beach tomorrow.  
Ego: It might rain, so let's go to the movies.



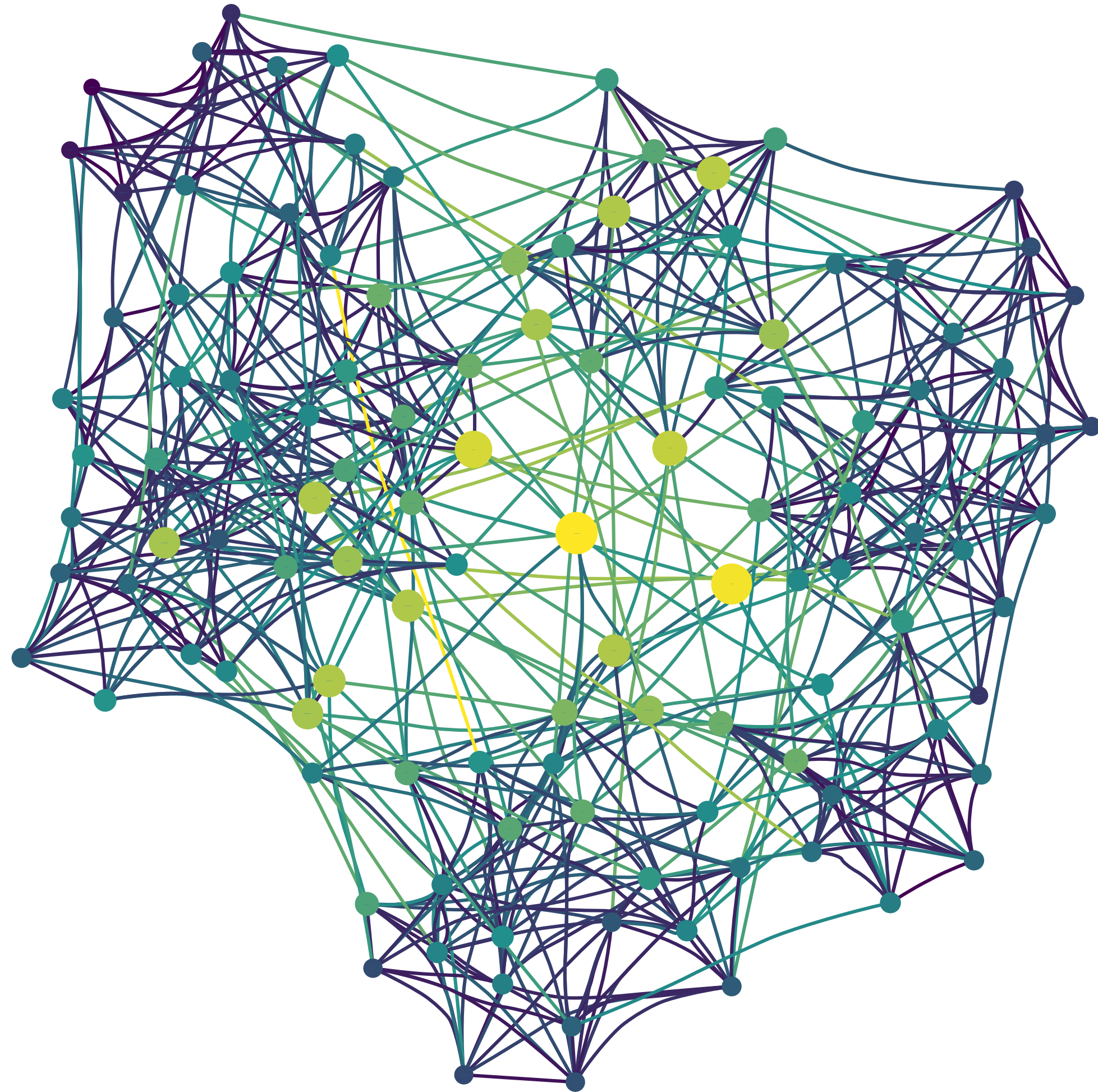
Bagrow & Mitchell (2018)  
Bagrow *et al* (2019)

# Rough Outline

Slides available on  
[bagrow.com](http://bagrow.com)

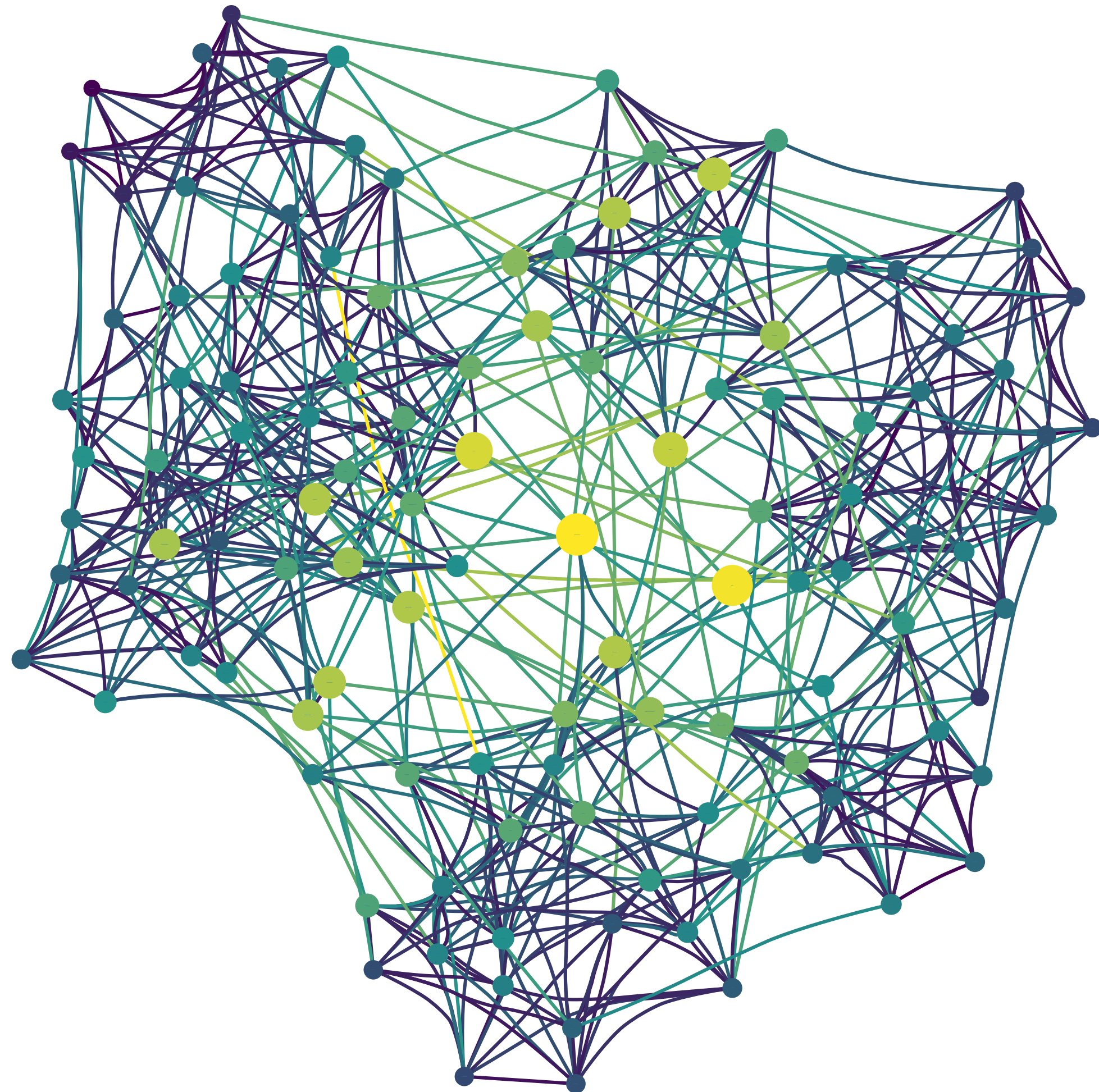
- Basics
  - file formats, code, databases
- Networks from data
  - common tasks and good practices
- Case studies and examples
- Machine learning for data and networks
- Visualization (*time permitting*)

# Network data are simple



- Looks like a complicated object
- Lots of measures, metrics, and algorithms to quantify and understand it
- But from a data perspective, very little to implement

# Network data are simple



Store graph topology → need to define the **nodes** (vertices) and the **links** (edges):

$$G = (V, E), |V| = N, |E| = M$$

Edgelist:

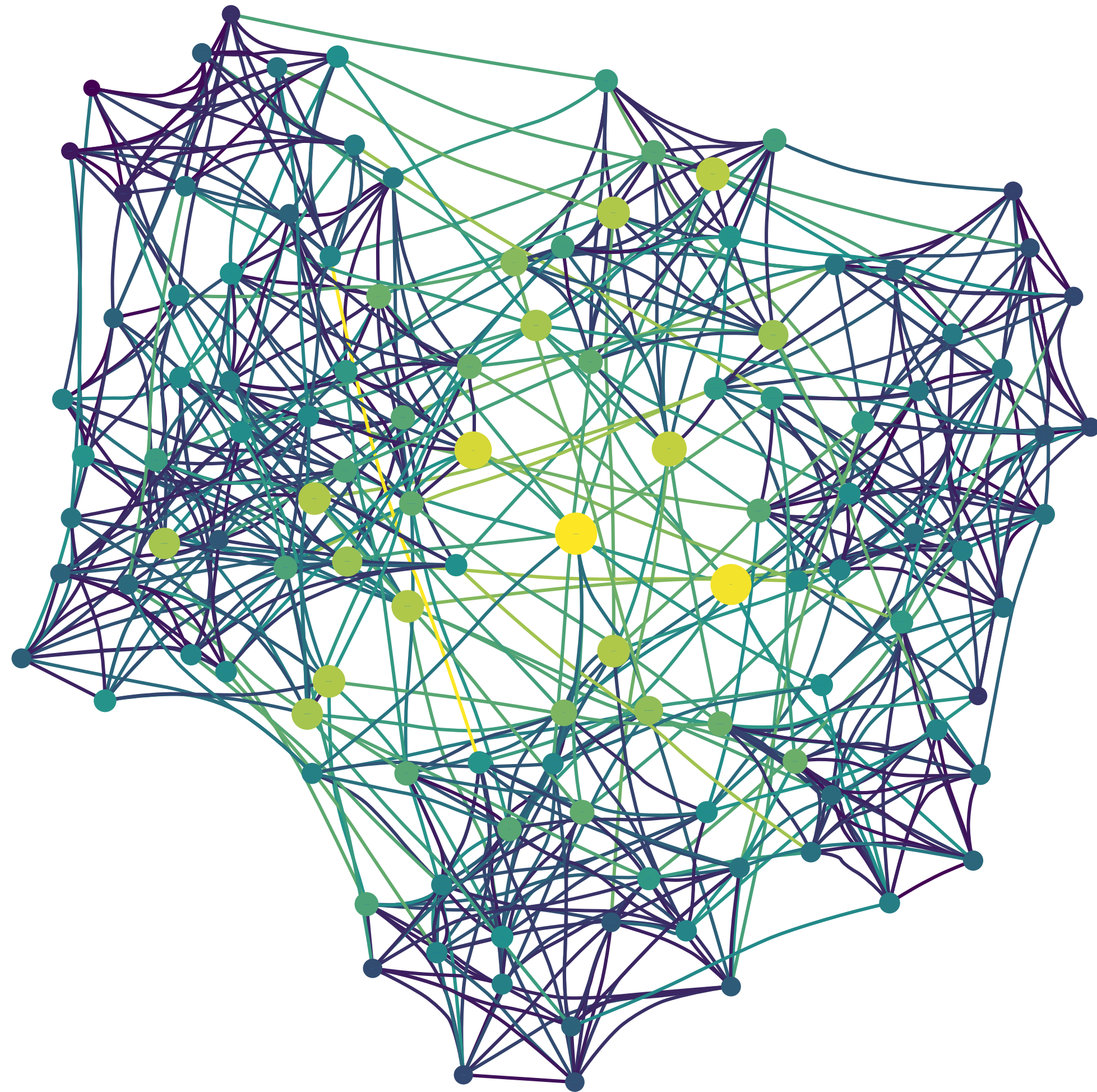
$M \times 2$  matrix

Alice	Bob
Bob	Carol
Bob	Dani
⋮	⋮

Need **identifiers** for nodes and *two delimiter symbols*



# Network data are simple



Store graph topology → need to define the **nodes** (vertices) and the **links** (edges):

$$G = (V, E), |V| = N, |E| = M$$

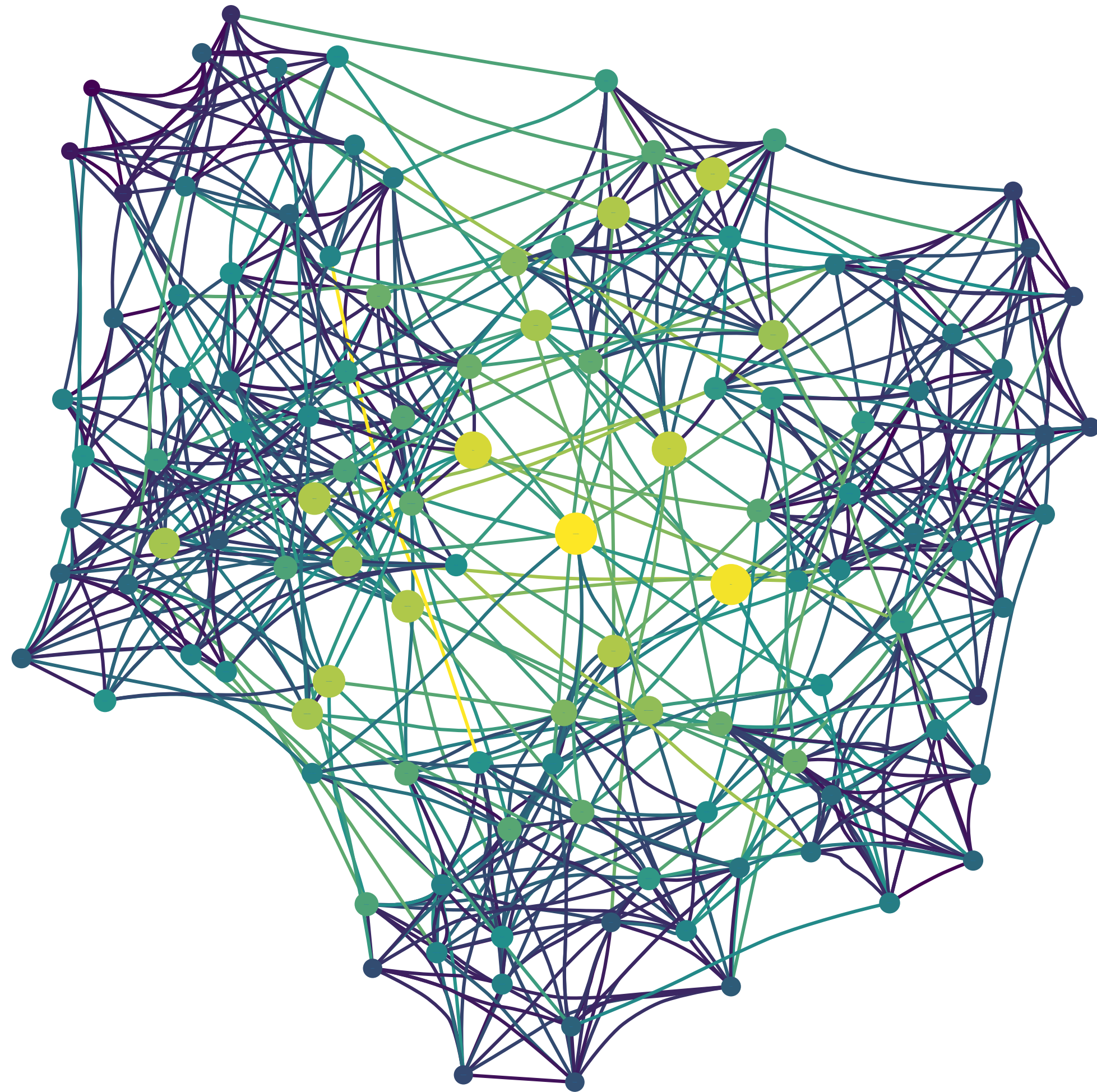
Adjacency list:

(ragged)

Alice	Bob		
Bob	Carol	Dani	
Carol	Bob	Erik	Fan
⋮			

May be harder to process in some programming languages

# Network data are simple



Store graph topology → need to define the **nodes** (vertices) and the **links** (edges):

$$G = (V, E), |V| = N, |E| = M$$

Adjacency  
Matrix:

0	1	0	...
0	0	1	...
0	1	0	...
⋮	⋮	⋮	⋱

# Network data are simple

Store graph topology → need to define the **nodes** (vertices) and the **links** (edges):

$$G = (V, E), |V| = N, |E| = M$$

## GraphML

Complex but more flexible

```
<?xml version="1.0" encoding="UTF-8"?>
<graphml xmlns="http://graphml.graphdrawing.org/xmlns"
  xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance"
  xsi:schemaLocation="http://graphml.graphdrawing.org/xmlns
    http://graphml.graphdrawing.org/xmlns/1.0/graphml.xsd">
  <graph id="G" edgedefault="undirected">
    <node id="n0"/>
    <node id="n1"/>
    <node id="n2"/>
    <node id="n3"/>
    <node id="n4"/>
    <node id="n5"/>
    <node id="n6"/>
    <node id="n7"/>
    <edge source="n0" target="n2"/>
    <edge source="n1" target="n2"/>
    <edge source="n2" target="n3"/>
    <edge source="n3" target="n5"/>
    <edge source="n3" target="n4"/>
    <edge source="n4" target="n6"/>
    <edge source="n6" target="n5"/>
    <edge source="n5" target="n7"/>
  </graph>
</graphml>
```

# Data surrounding network

What about **extra attributes**?

$$G = (V, E, X)$$

$X$  = **attributes**, node labels or colors, timestamps

Can also have *edge* attributes

Edgelist

Alice	Bob	e1
Bob	Carol	e2
Bob	Dani	e3
⋮	⋮	

attributes

Node attribute list

Alice	x11	x12
Bob	x21	x22
Carol	x31	x32
⋮	⋮	⋮

attributes

# Data surrounding network

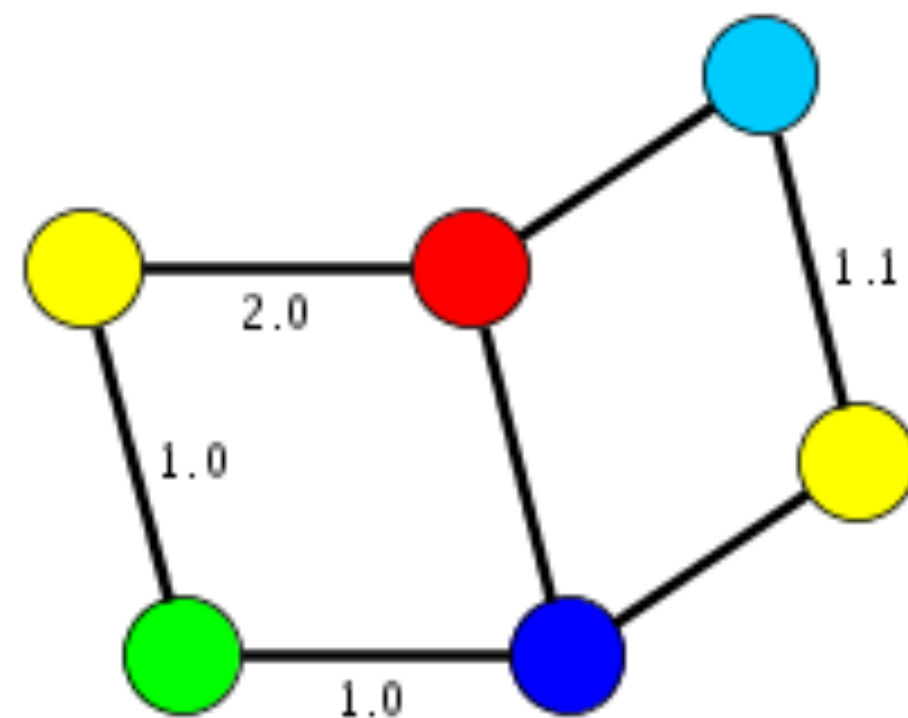
What about **extra attributes**?

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Can also have *edge* attributes

GraphML



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<?xml version="1.0" encoding="UTF-8"?>
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  xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance"
  xsi:schemaLocation="http://graphml.graphdrawing.org/xmlns
    http://graphml.graphdrawing.org/xmlns/1.0/graphml.xsd">
  <key id="d0" for="node" attr.name="color" attr.type="string">
    <default>yellow</default>
  </key>
  <key id="d1" for="edge" attr.name="weight" attr.type="double"/>
  <graph id="G" edgedefault="undirected">
    <node id="n0">
      <data key="d0">green</data>
    </node>
    <node id="n1"/>
    <node id="n2">
      <data key="d0">blue</data>
    </node>
    <node id="n3">
      <data key="d0">red</data>
    </node>
    <node id="n4"/>
    <node id="n5">
      <data key="d0">turquoise</data>
    </node>
    <edge id="e0" source="n0" target="n2">
      <data key="d1">1.0</data>
    </edge>
    <edge id="e1" source="n0" target="n1">
      <data key="d1">1.0</data>
```

# Network data structures

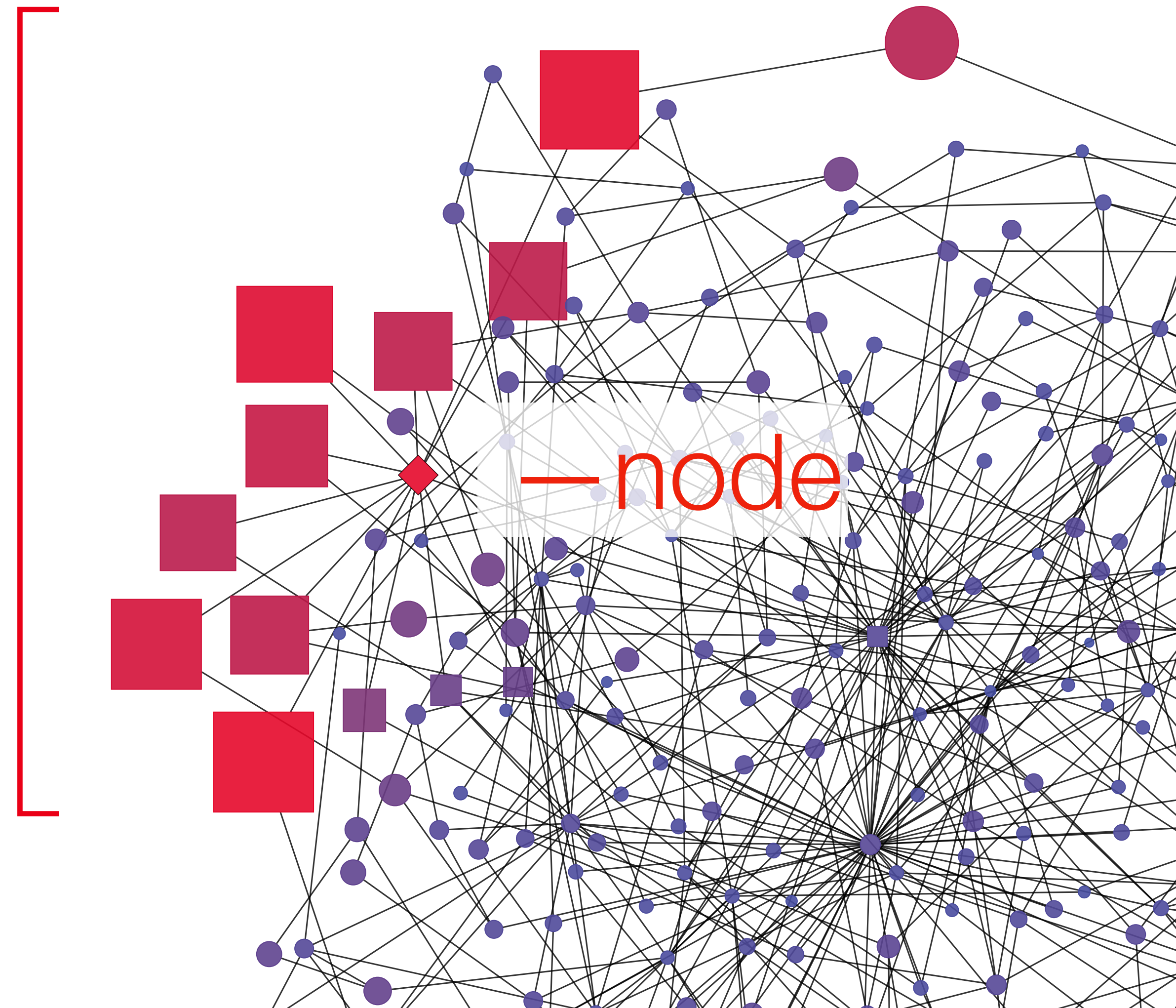
To perform computations on a network, need a computable representation

```
node2neighbors = ...
```

```
print(node2neighbors['Alice'])  
{'Bob', 'Carol'}
```

neighbors

— node



# Network libraries

It's a good exercise to build your own data structures or even library, but in practice: lots of existing libraries

<https://networkx.github.io>

<https://igraph.org>

<https://graph-tool.skewed.de>


## NetworkX

Software for complex networks

Stable (notes)  
2.2 — September 2018  
[download](#) | [doc](#) | [pdf](#)

Latest (notes)  
2.3 development  
[github](#) | [doc](#) | [pdf](#)

NetworkX is a Python package for the creation, manipulation, and study of the structure, dynamics, and functions of complex networks.





## igraph – The network analysis package

igraph is a collection of network analysis tools with the emphasis on **efficiency, portability** and ease of use. igraph is **open source** and free. igraph can be programmed in **R, Python, Mathematica** and **C/C++**.

[igraph R package](#) | [python-igraph](#) | [IGraph/M](#) | [igraph C library](#)



## graph-tool

Efficient network analysis

### What is graph-tool?

Graph-tool is an efficient **Python** module for manipulation and statistical analysis of **graphs** (a.k.a. **networks**). Contrary to most other python modules with similar functionality, the core data structures and algorithms are implemented in **C++**, with extensive use of template **metaprogramming**, based heavily on the **Boost Graph Library**. This confers it a level of **performance** that is comparable (both in memo



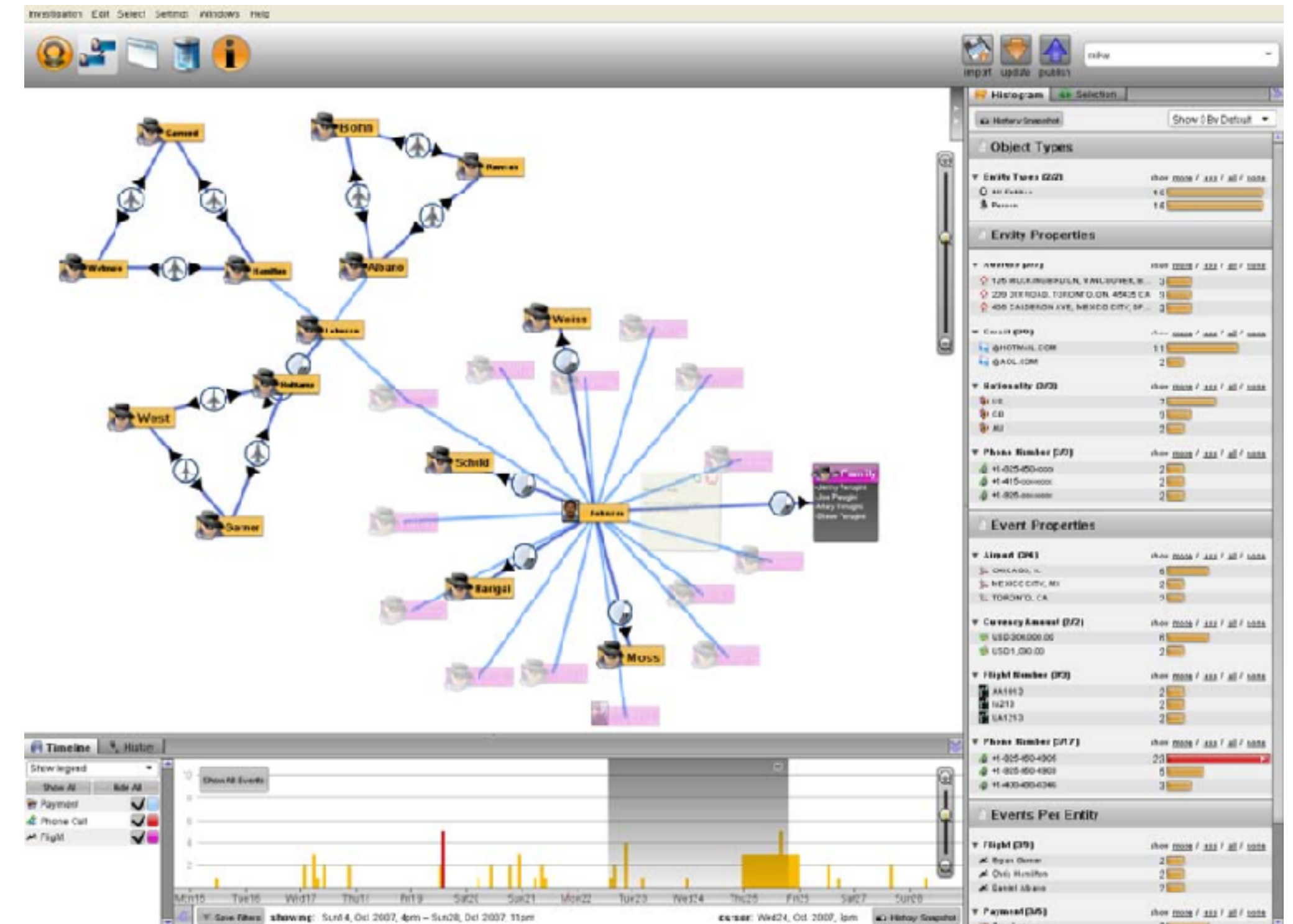
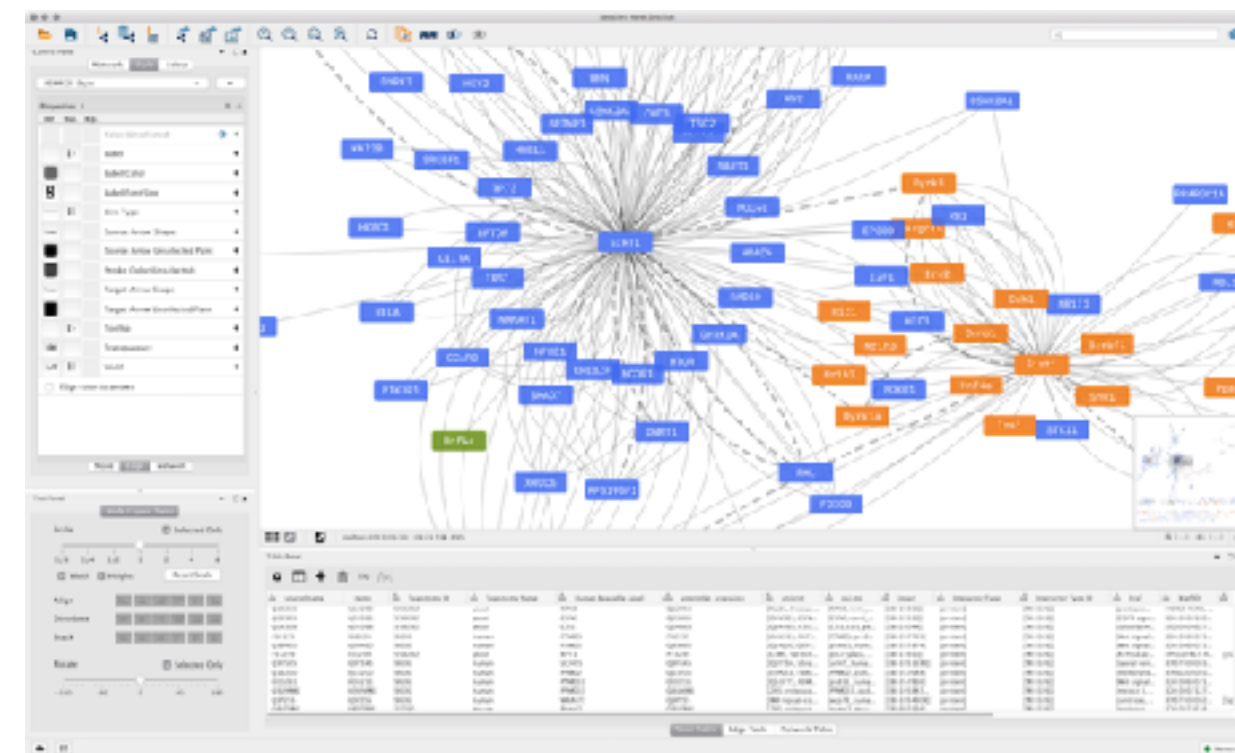
recent versions have graph algorithms (+ always have adjacency matrix)

# Graphical Interfaces and dashboards

I prefer to handle networks **computationally**, writing and running code—expressive, provenance

Interactive interfaces easier to get started but then you max out quickly!

Can be good for visualizations

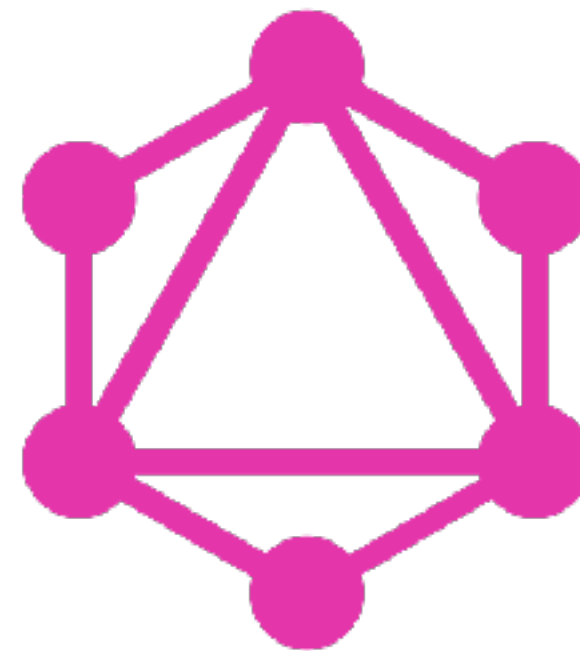




# Graph databases — Big Data



GraphQL



databases: relational  
key-value  
document  
graph  
⋮



(semantic web)



<https://neo4j.com>  
<https://jena.apache.org/>  
<http://graphdb.ontotext.com>  
<https://graphql.org>

# Graph databases — Big Data

Applications of Graph DBs:

Knowledge graphs — semantic web

Fraud detection — real time

Recommendations (Netflix, Amazon)

Graph DBs best for real-time, high-volume, *local* operations

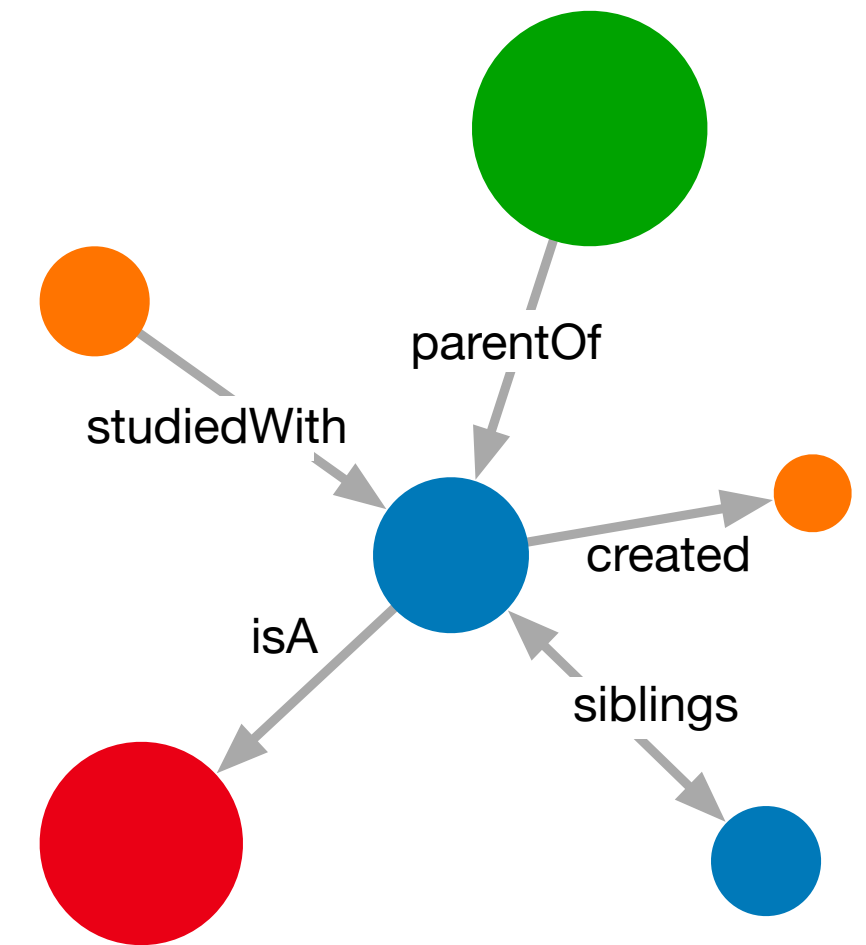
# Graph databases — Big Data

Applications of Graph DBs:

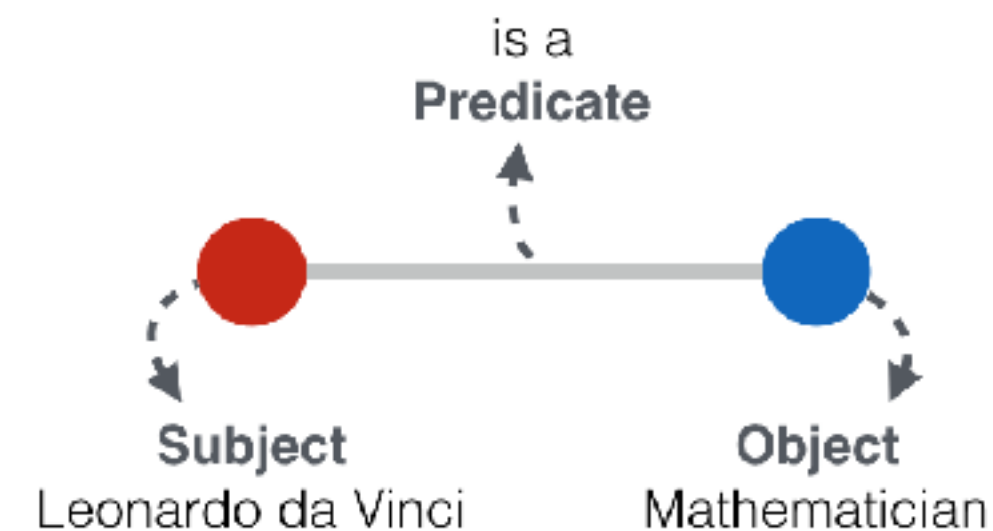
Knowledge graphs — semantic web  
Fraud detection — real time  
Recommendations (Netflix, Amazon)

Graph DBs best for real-time, high-volume, *local* operations

Knowledge Graph



Triplestore/RDF:



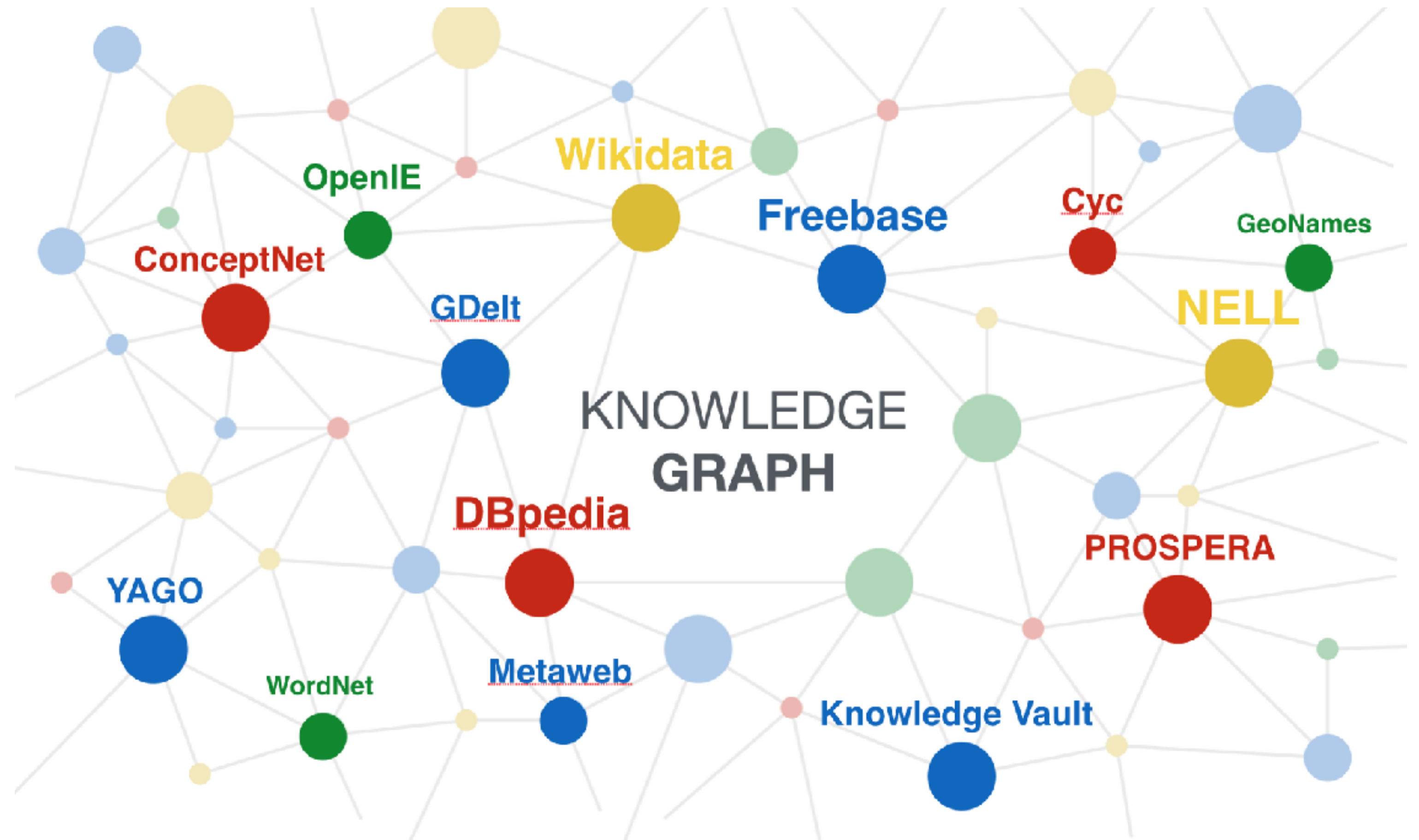
<Leonardo da Vinci> <is a> <Mathematician>  
<Diabetes Genes> <encodes> <Leptin>  
<Visigoths> <conquered> <Ostrogoths>  
<Barack Obama> <born in> <Hawaii>  
<Harry Potter> <is a> <Fictional Character>  
<Mount Everest> <elevation> <8,848 meters>  
<Magic> <is> <Real>

# Graph databases—Big Data

## Some Knowledge Graphs

Dataset	Triples	Size
<a href="#">Wikidata (2018-09-11)</a>	7.2B	28GB
<a href="#">DBPedia 2016-04 English</a>	1B	13GB
<a href="#">DBLP 2017</a>	882M	1GB
<a href="#">Freebase</a>	2B	11GB
<a href="#">YAGO2s Knowledge Base</a>	159M	903MB
<a href="#">WordNet 3.1</a>	5.5M	23MB

Courtesy: [rdfhdt.org](http://rdfhdt.org)

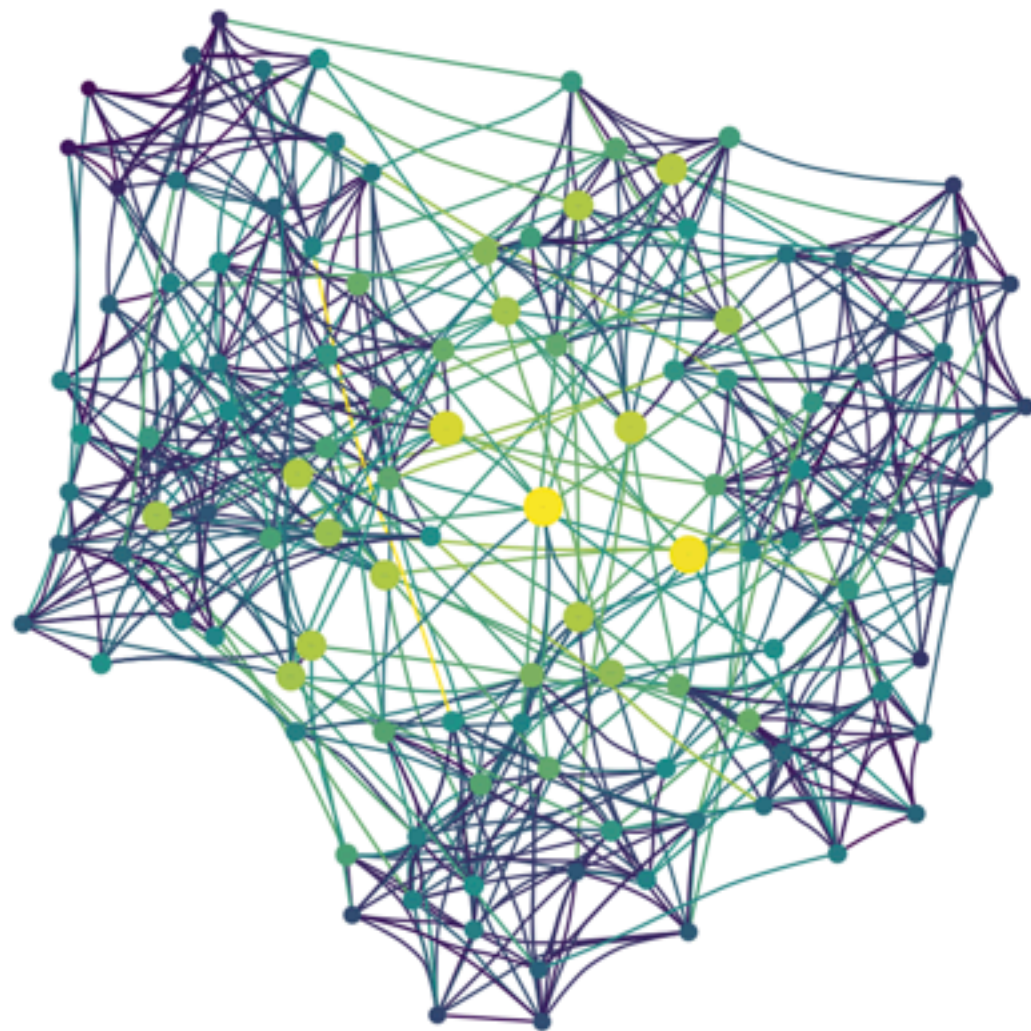


Courtesy: [Sebastian Dery](#)

**Network data are not simple**

# There is an **upstream task**

## Network data are simple



- Looks like a complicated object
- Lots of measures, metrics, and algorithms to quantify and understand it
- But from a data perspective, very little to implement

What **defines** your network?

Criteria for nodes?

Criteria for **links**?

(Is a network even a good idea?)

Only simple *after* addressing these questions (if you need to)

# Example: social network from mobile phone data

OPEN ACCESS Freely available online



## Collective Response of Human Populations to Large-Scale Emergencies

James P. Bagrow<sup>1,2\*,9</sup>, Dashun Wang<sup>1,2,9</sup>, Albert-László Barabási<sup>1,2,3</sup>

## Link communities reveal multiscale complexity in networks

Yong-Yeol Ahn<sup>1,2\*</sup>, James P. Bagrow<sup>1,2\*</sup> & Sune Lehmann<sup>3,4\*</sup>

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# Example: social network from mobile phone data

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PLOS one

## Collective Response of Human Populations to Large-Scale Emergencies

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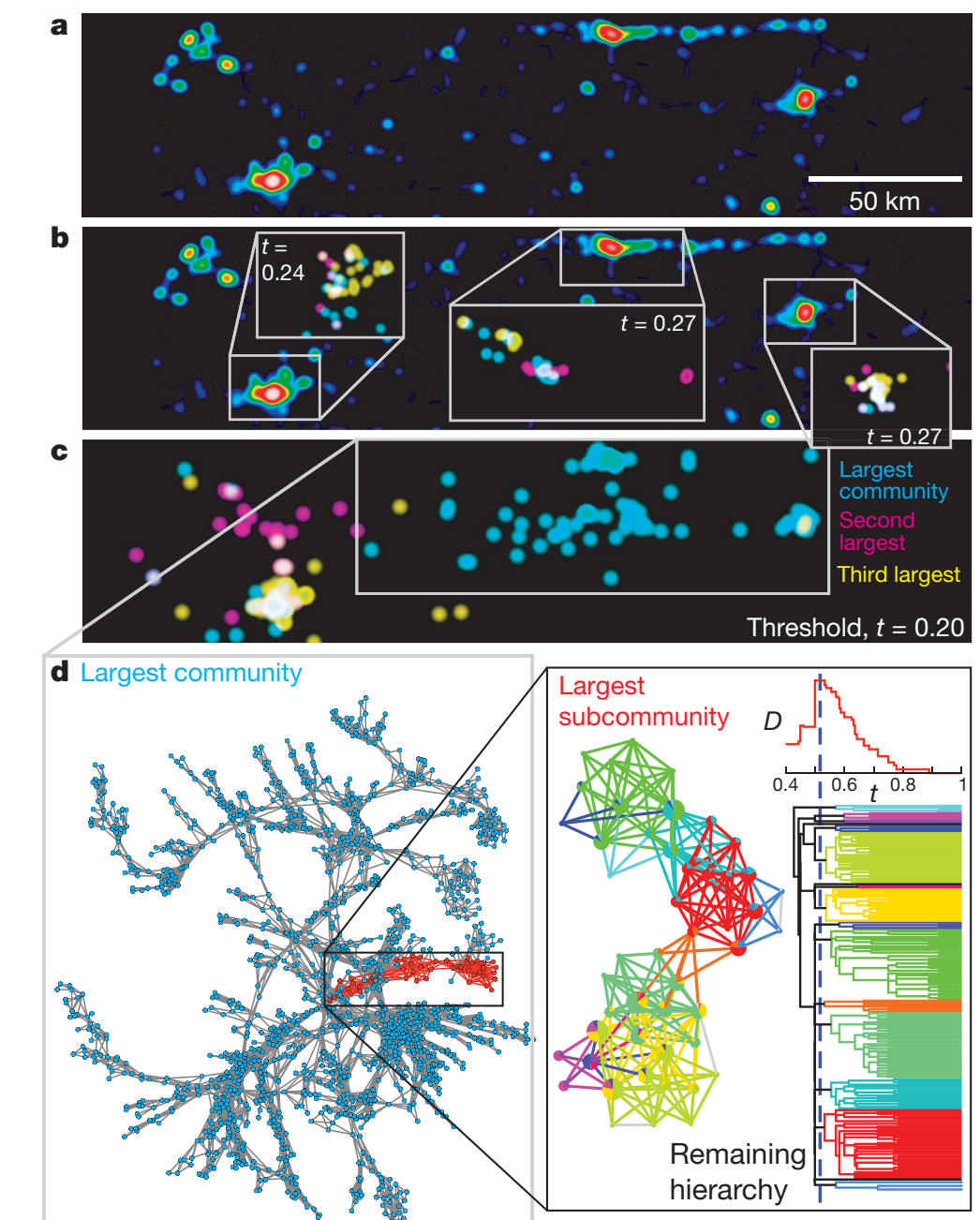
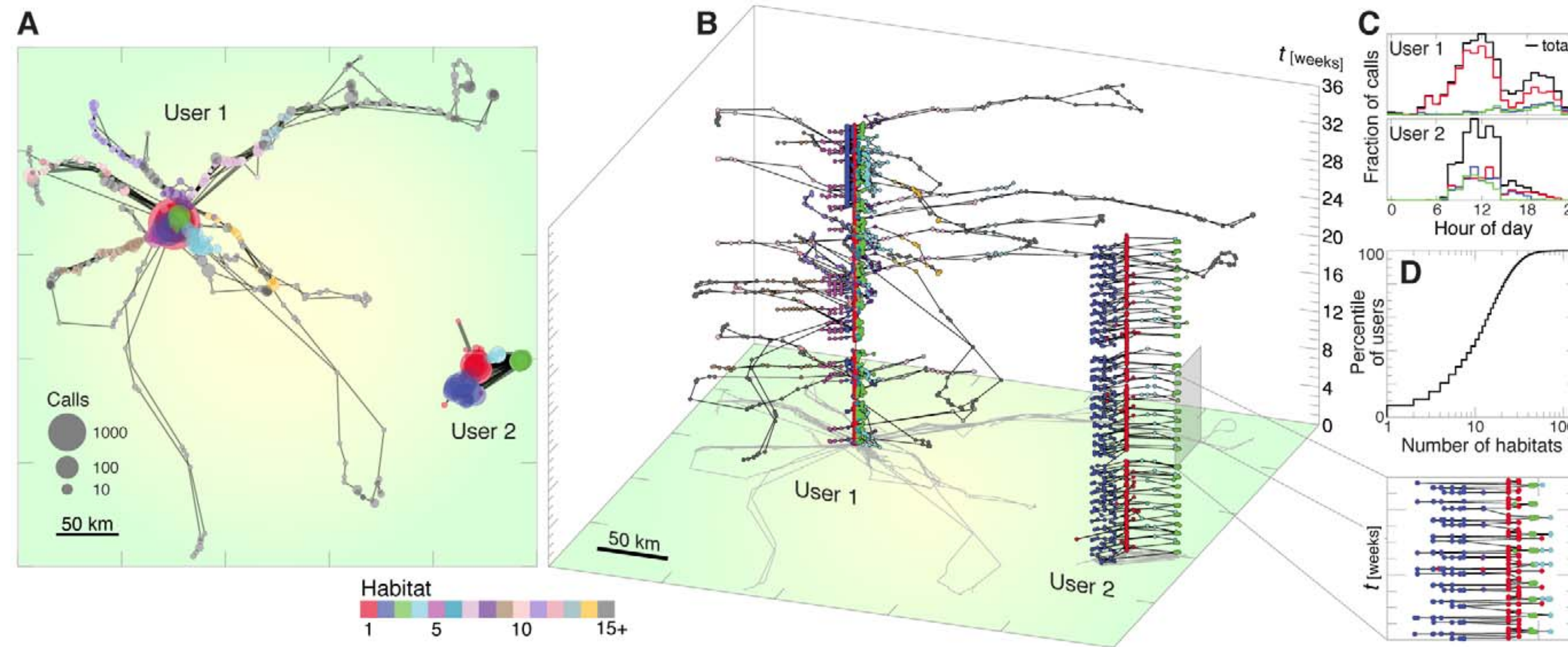
PLOS one

## Mesoscopic Structure and Social Aspects of Human Mobility

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spatial social network

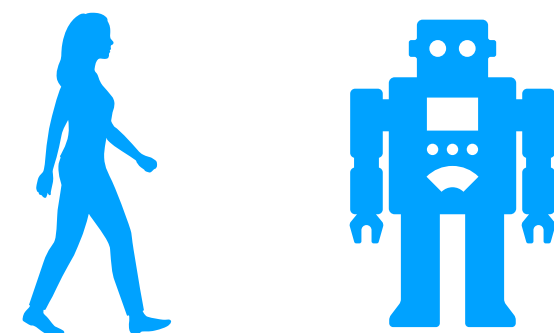


# Example: social network from mobile phone data

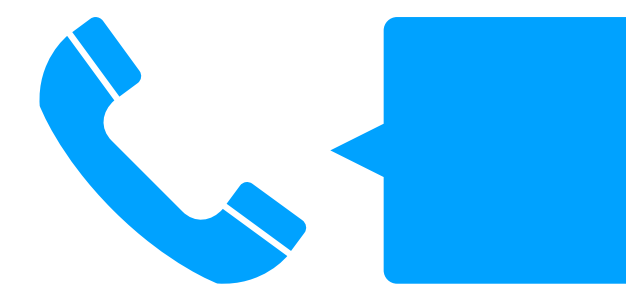
Extracted from deidentified **Call Detail Record** (CDR) files

What **defines** your network?

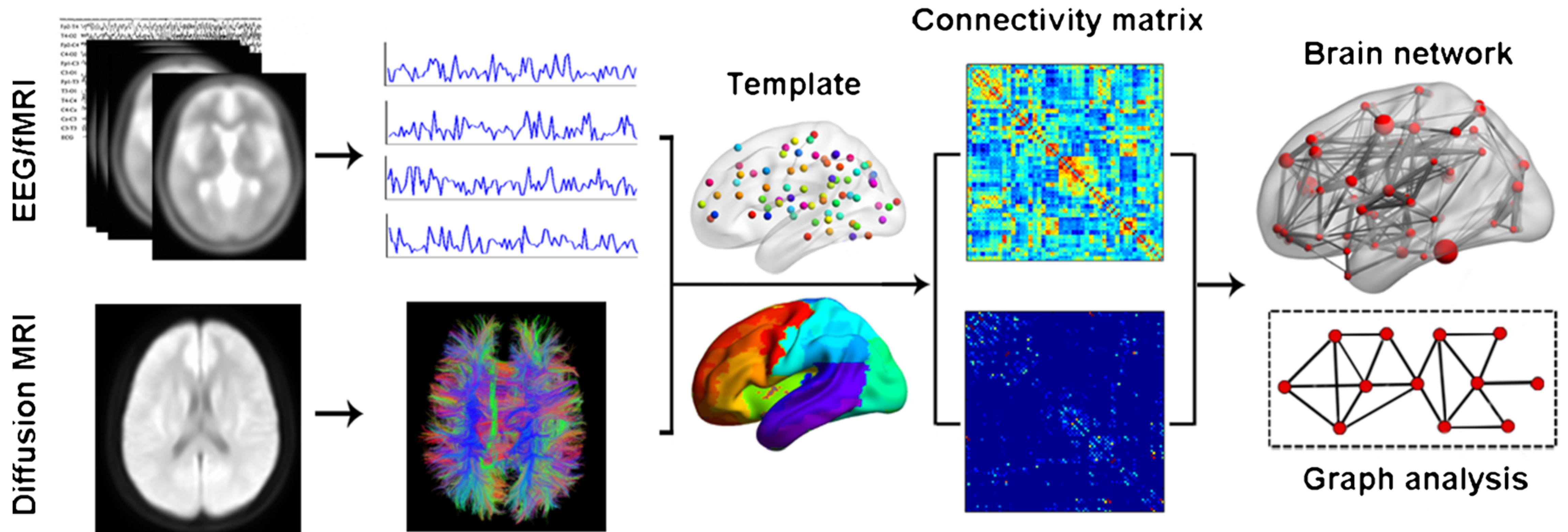
Criteria for nodes?



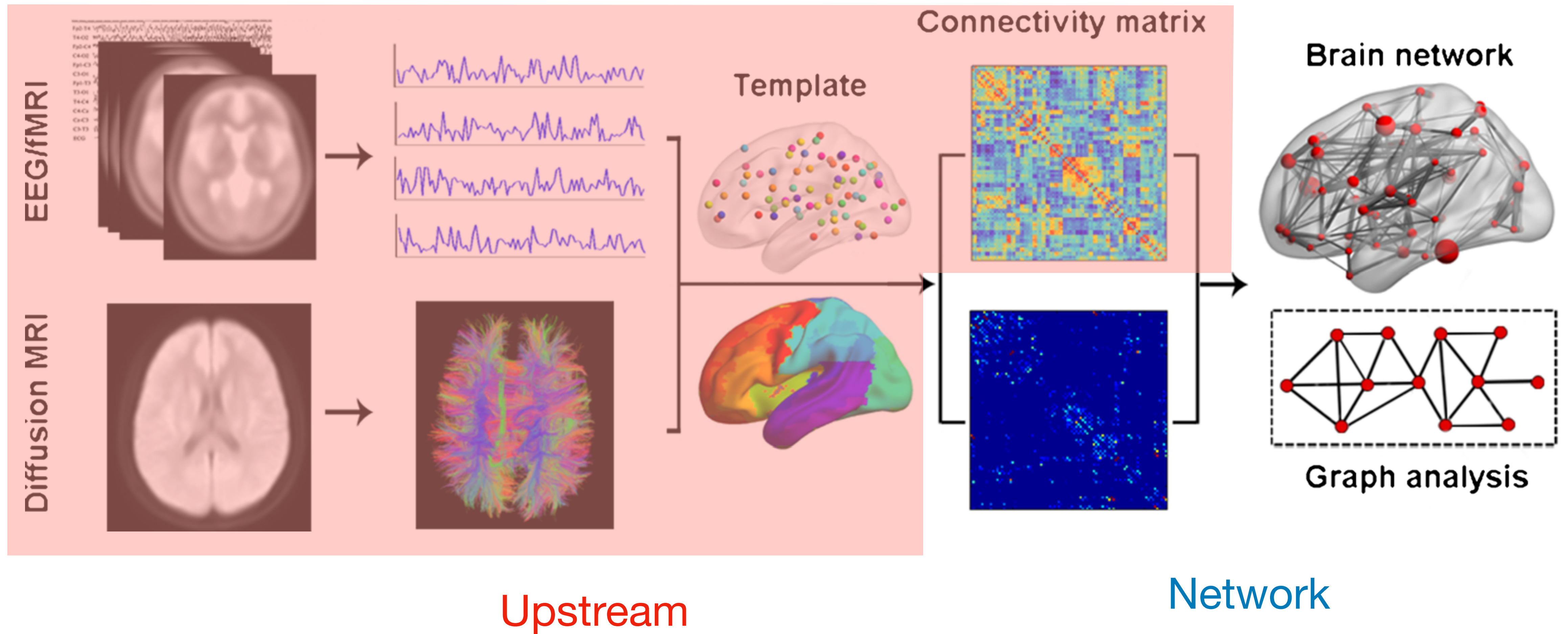
Criteria for links?



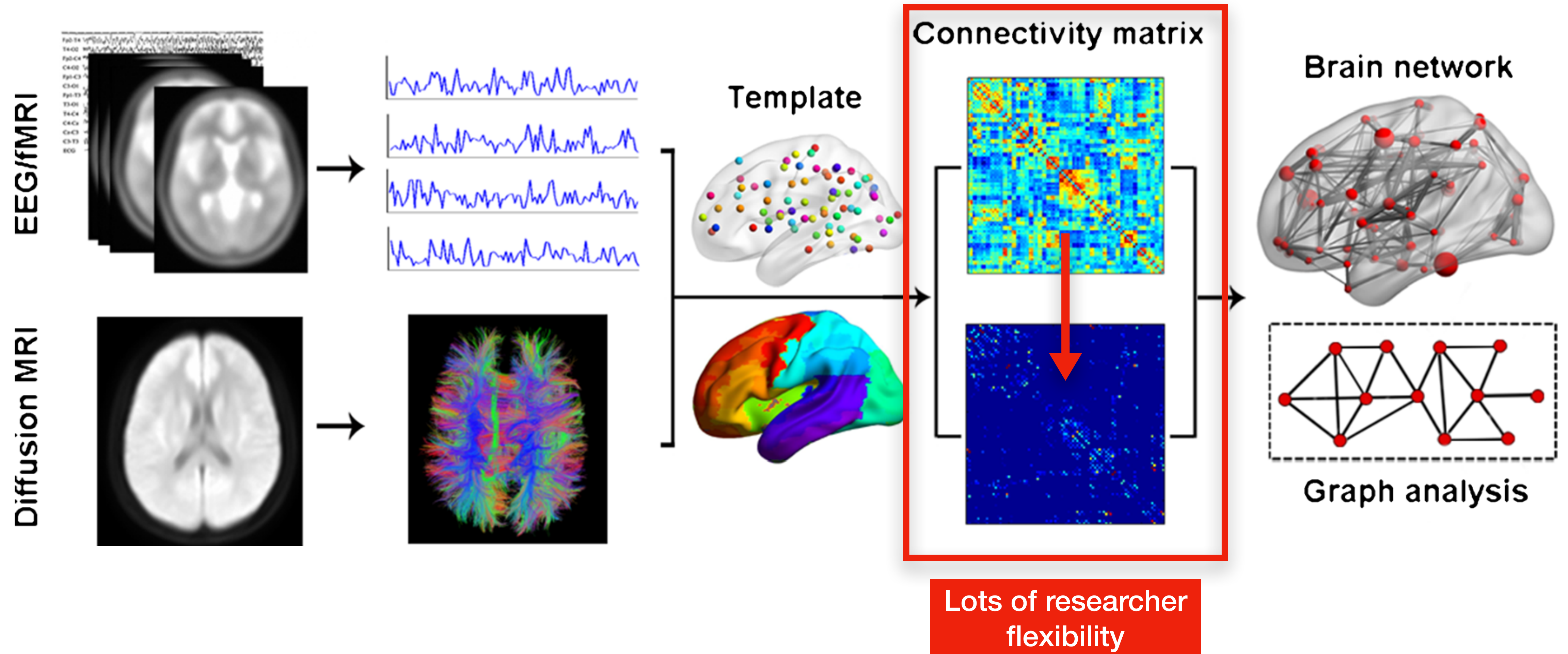
# Example: brain networks



# Example: brain networks



# Example: brain networks



# There is an upstream task

What's the best network (there may be more than one)?

*“Diseaseome”*

Define nodes

Define edges (hyper-edges?)

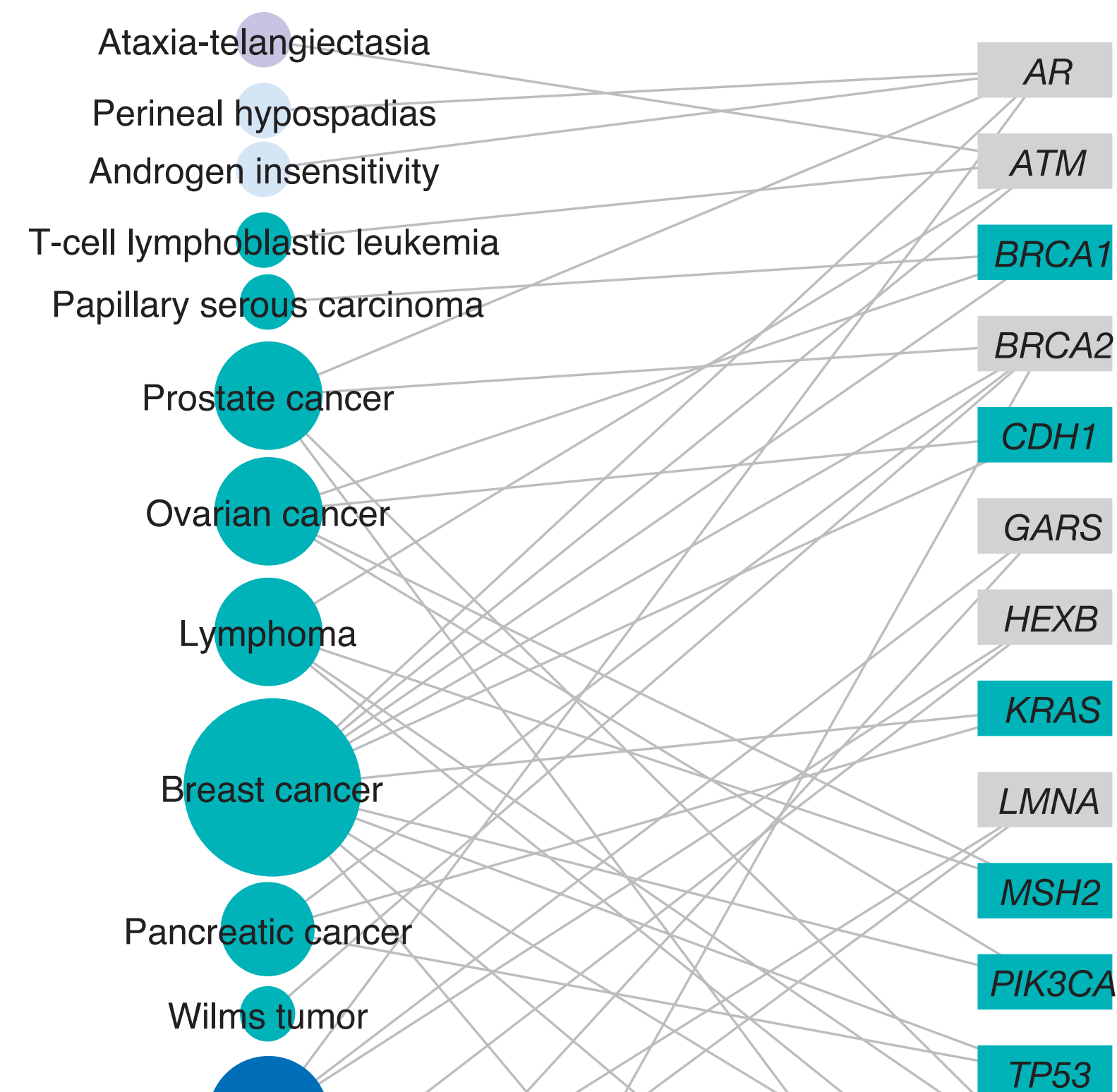
Directed?

Weighted?

Use a **bipartite representation** or project down?

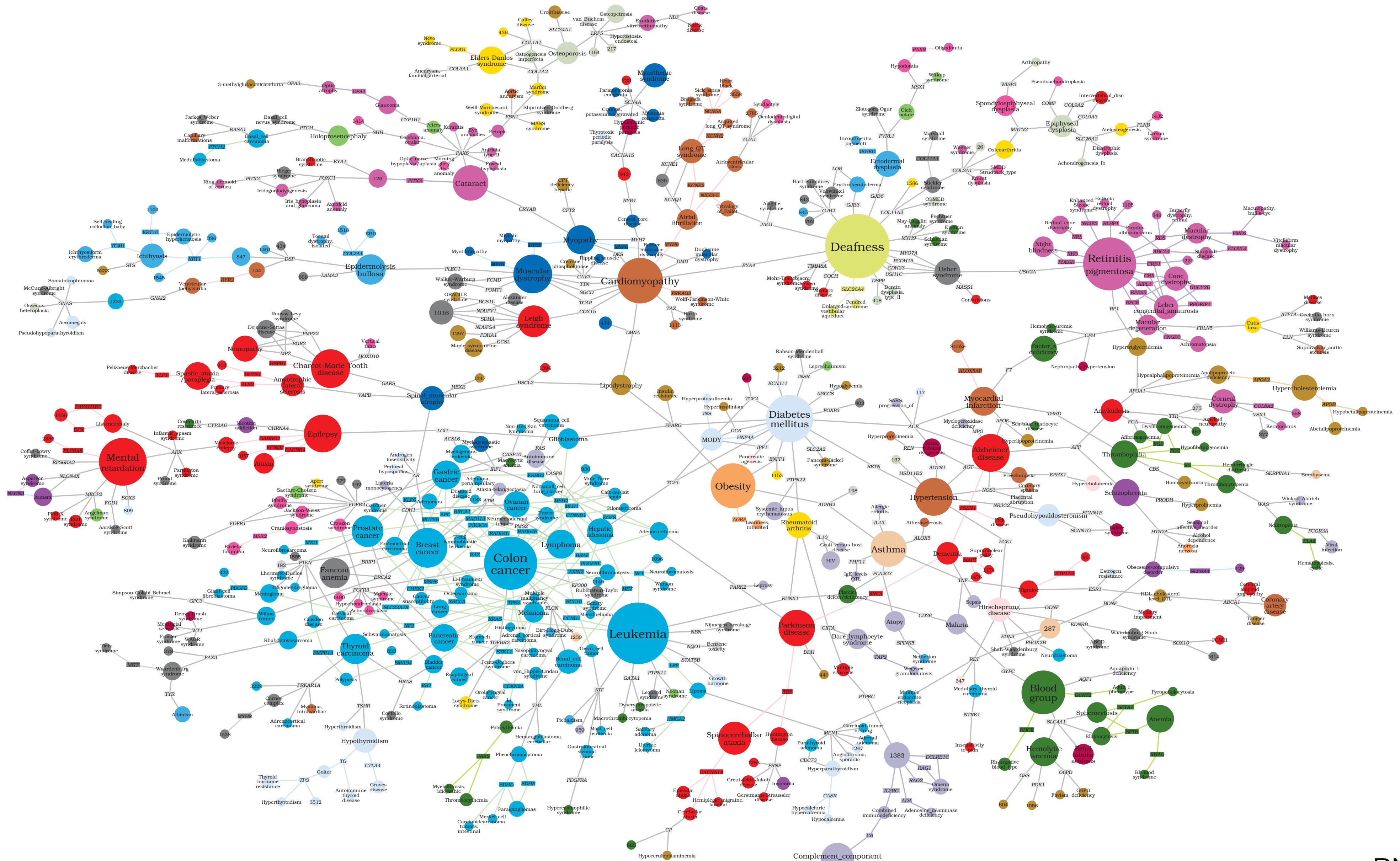
disease phenome

disease genome



# The human disease network

Goh K-I, Cusick ME, Valle D, Childs B, Vidal M, Barabási A-L (2007) *Proc Natl Acad Sci USA* 104:8685-8690



Goh et al.  
PNAS (2007)

# Case study: gathering a bipartite network

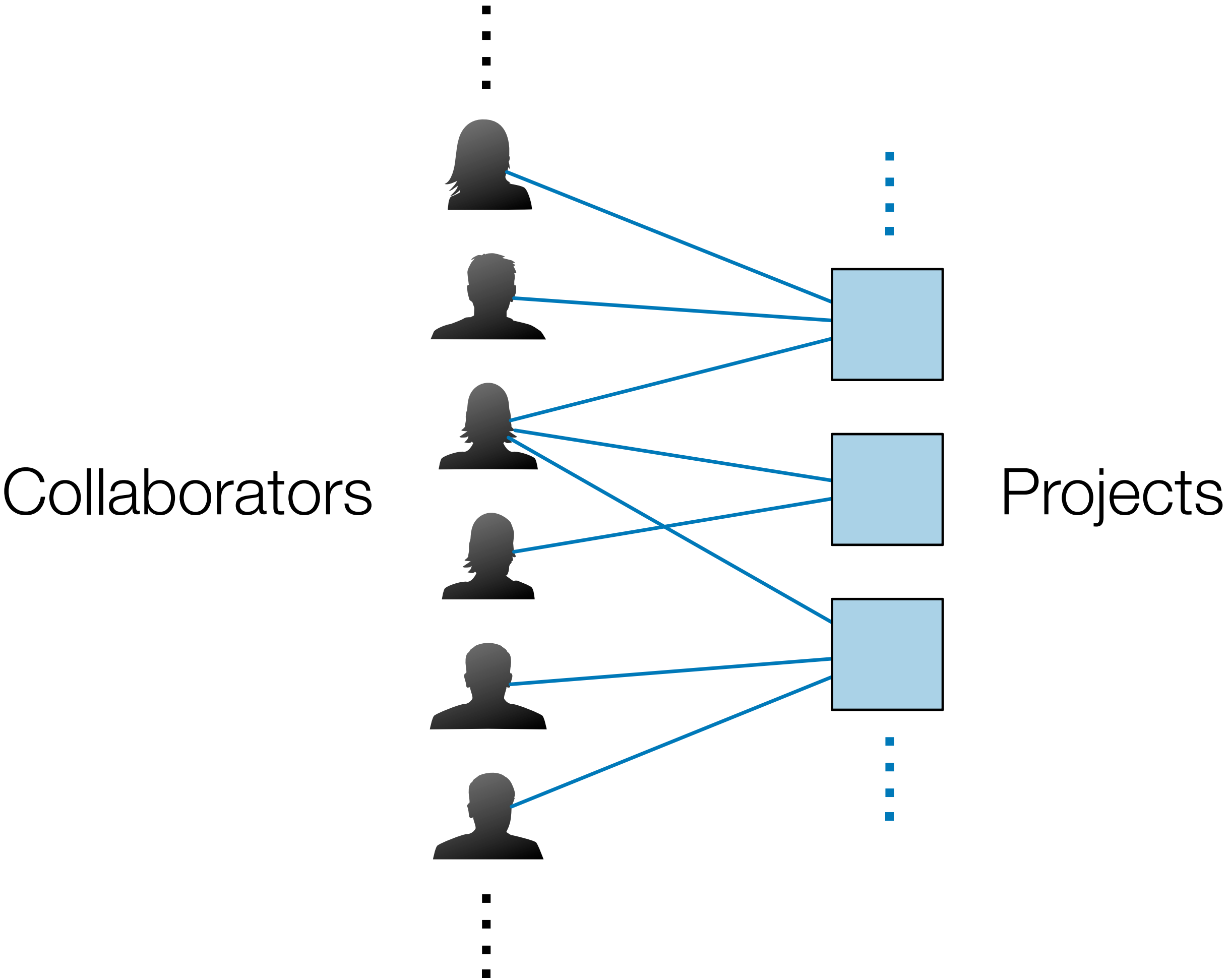
Understanding the group dynamics and success of teams

---

Michael Klug<sup>1</sup> and James P. Bagrow<sup>1,2,3</sup>

---

teams of collaborators



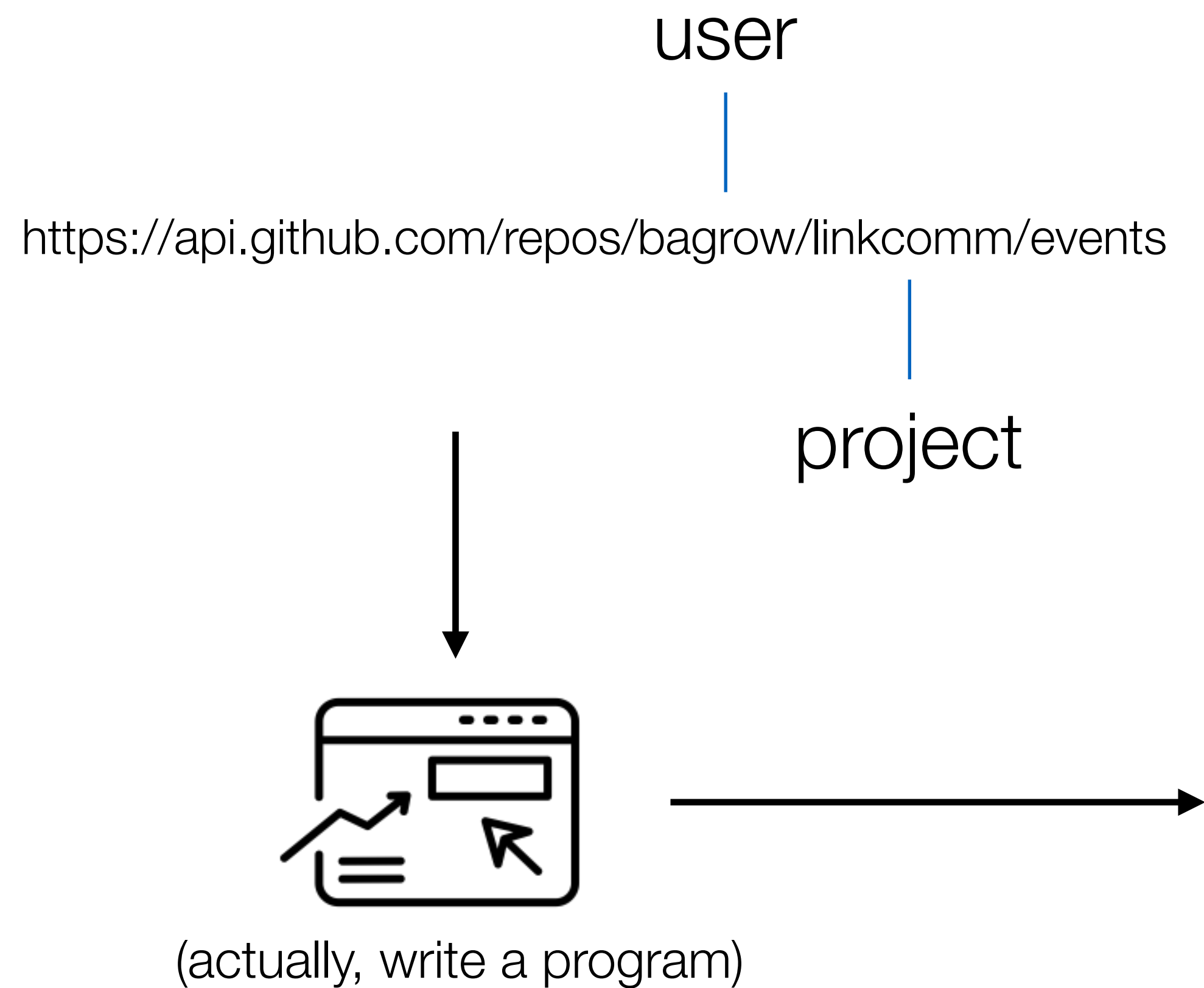
## Building this network from the data

GitHub provides an [API](#) that lets you access the activities (events) of users as they make changes to code, join different teams, etc.



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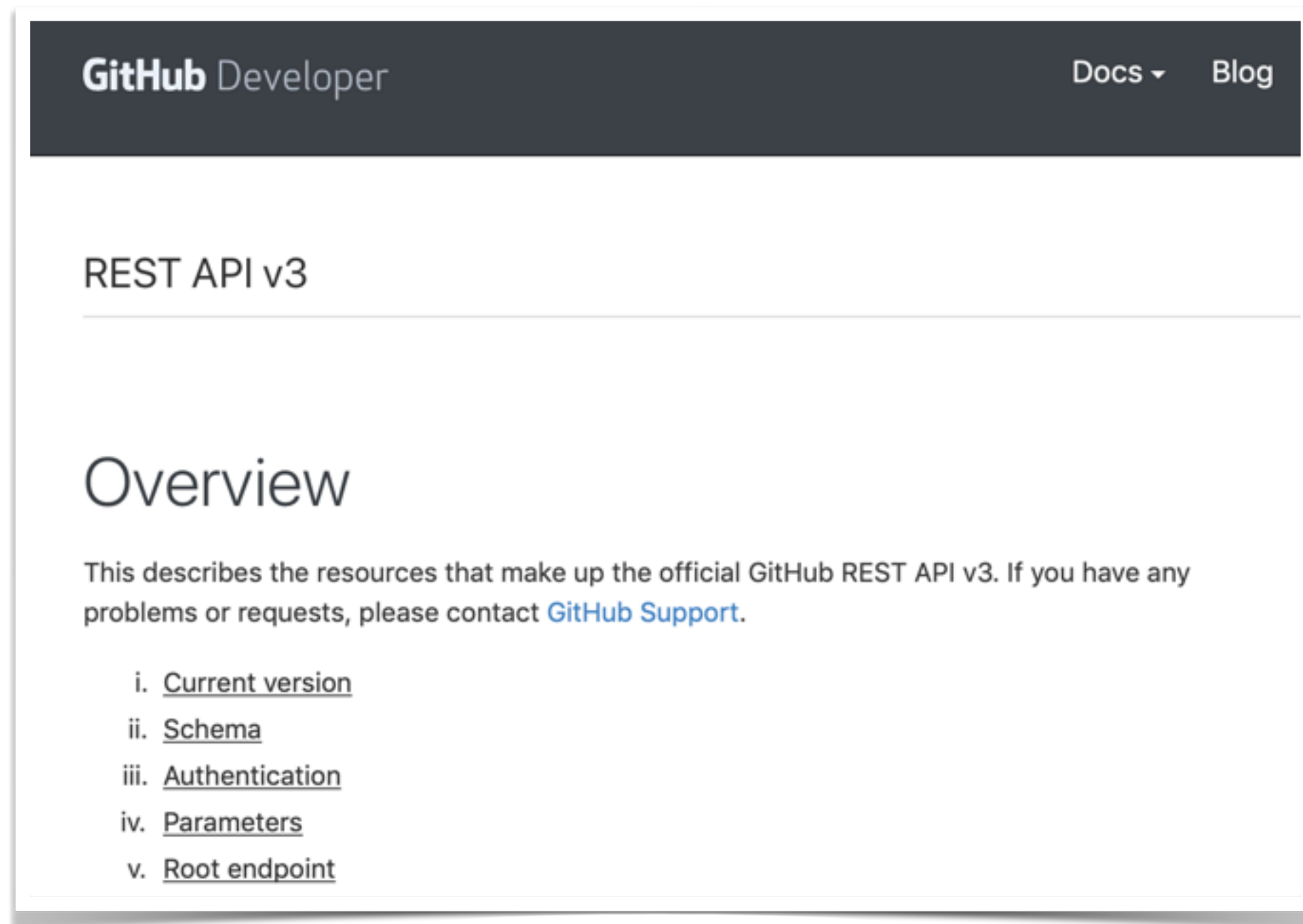


```
...
{
  "id": "8401895651",
  "type": "PushEvent",
  "actor": {
    "login": "bagrow",
    "display_login": "bagrow",
    "gravatar_id": "",
    "url": "https://api.github.com/users/bagrow",
  },
  "repo": {
    "id": 904212,
    "name": "bagrow/linkcomm",
    "url": "https://api.github.com/repos/bagrow/linkcomm"
  },
  "payload": {
    "action": "started"
  },
  "public": true,
  "created_at": "2018-10-11T03:33:42Z"
}
...
```

# Building this network from the data

GitHub provides an [API](#) that lets you access the activities (events) of users as they make changes to code, join different teams, etc.

## JSON data



<https://developer.github.com/v3/>

```
•
•
•
{
  "id": "8401895651",
  "type": "PushEvent",
  "actor": {
    "login": "bagrow",
    "display_login": "bagrow",
    "gravatar_id": "",
    "url": "https://api.github.com/users/bagrow",
  },
  "repo": {
    "id": 904212,
    "name": "bagrow/linkcomm",
    "url": "https://api.github.com/repos/bagrow/linkcomm"
  },
  "payload": {
    "action": "started"
  },
  "public": true,
  "created_at": "2018-10-11T03:33:42Z"
}
•
•
•
```

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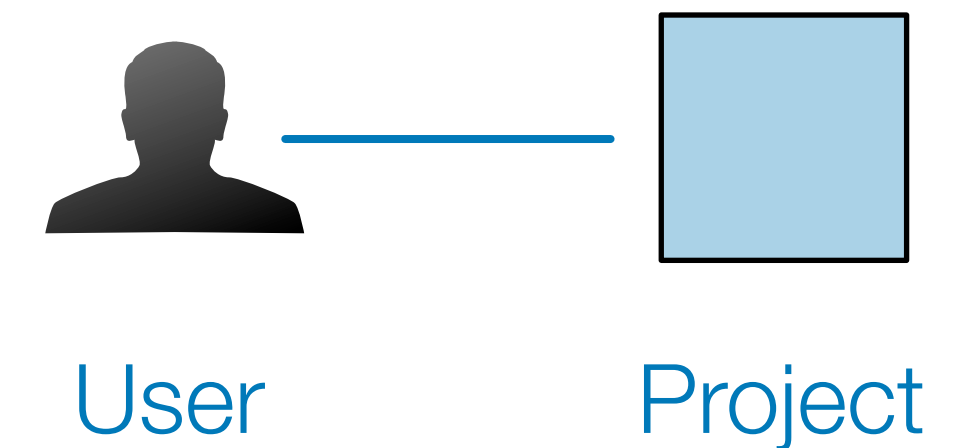
```
      :
      :
      {
Code updated ——— "id": "8401895651",
User          ——— "type": "PushEvent",
              "actor": {
                "login": "bagrow",
                "display_login": "bagrow",
                "gravatar_id": "",
                "url": "https://api.github.com/users/bagrow",
              },
Project      ——— },
              "repo": {
                "id": 904212,
                "name": "bagrow/linkcomm",
                "url": "https://api.github.com/repos/bagrow/linkcomm"
              },
              "payload": {
                "action": "started"
              },
              "public": true,
              "created_at": "2018-10-11T03:33:42Z"
      }
      :
      :
```

# Building this network from the data

GitHub provides an [API](#) that lets you access the activities (events) of users as they make changes to code, join different teams, etc.

```
      ⋮  
      {  
Code updated ——— "id": "8401895651",  
User ——— "type": "PushEvent",  
              "actor": {  
              "login": "bagrow",  
              "display_login": "bagrow",  
              "gravatar_id": "",  
              "url": "https://api.github.com/users/bagrow",  
Project ——— },  
              "repo": {  
              "id": 904212,  
              "name": "bagrow/linkcomm",  
              "url": "https://api.github.com/repos/bagrow/linkcomm"  
              },  
              "payload": {  
              "action": "started"  
              },  
              "public": true,  
              "created_at": "2018-10-11T03:33:42Z"  
      }  
      ⋮
```

Insert link into bipartite graph



# Building this network from the data

GitHub provides an [API](#) that lets you access the activities (events) of users as they make changes to code, join different teams, etc.

🤔 Are "PushEvents" meaningful?

🤔 Are node IDs?

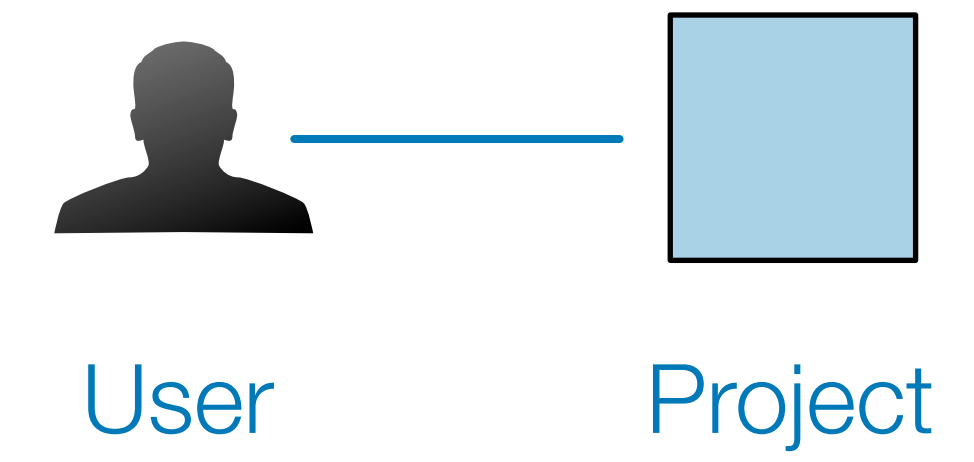
```
⋮
{
  "id": "8401895651",
  "type": "PushEvent",
  "actor": {
    "login": "bagrow",
    "display_login": "bagrow",
    "gravatar_id": "",
    "url": "https://api.github.com/users/bagrow",
  },
  "repo": {
    "id": 904212,
    "name": "bagrow/linkcomm",
    "url": "https://api.github.com/repos/bagrow/linkcomm"
  },
  "payload": {
    "action": "started"
  },
  "public": true,
  "created_at": "2018-10-11T03:33:42Z"
}
⋮
```

Code updated

User

Project

Insert link into bipartite graph



## Building this network from the data

To build the entire network requires **scraping** their API:

- probably too slow
- API provider will probably **block you**

Solutions:

- Give up on getting the entire network and **work locally**; **snowball sample**?
- Find another source of data:

# Building this network from the data

To build the entire network requires **scraping** their API:

- probably too slow
- API provider will probably **block you**

Solutions:

- Give up on getting the entire network and **work locally**; **snowball sample**?
- Find another source of data:



GitHub provides **20+ event types**, which range from new commits and fork events, to opening new tickets, commenting, and adding members to a project. These events are aggregated into hourly archives, which you can access with any HTTP client:

#### Query

#### Command

Activity for 1/1/2015 @ 3PM UTC

```
wget http://data.gharchive.org/2015-01-01-15.json.gz
```

Activity for 1/1/2015

```
wget http://data.gharchive.org/2015-01-01-{0..23}.json.gz
```

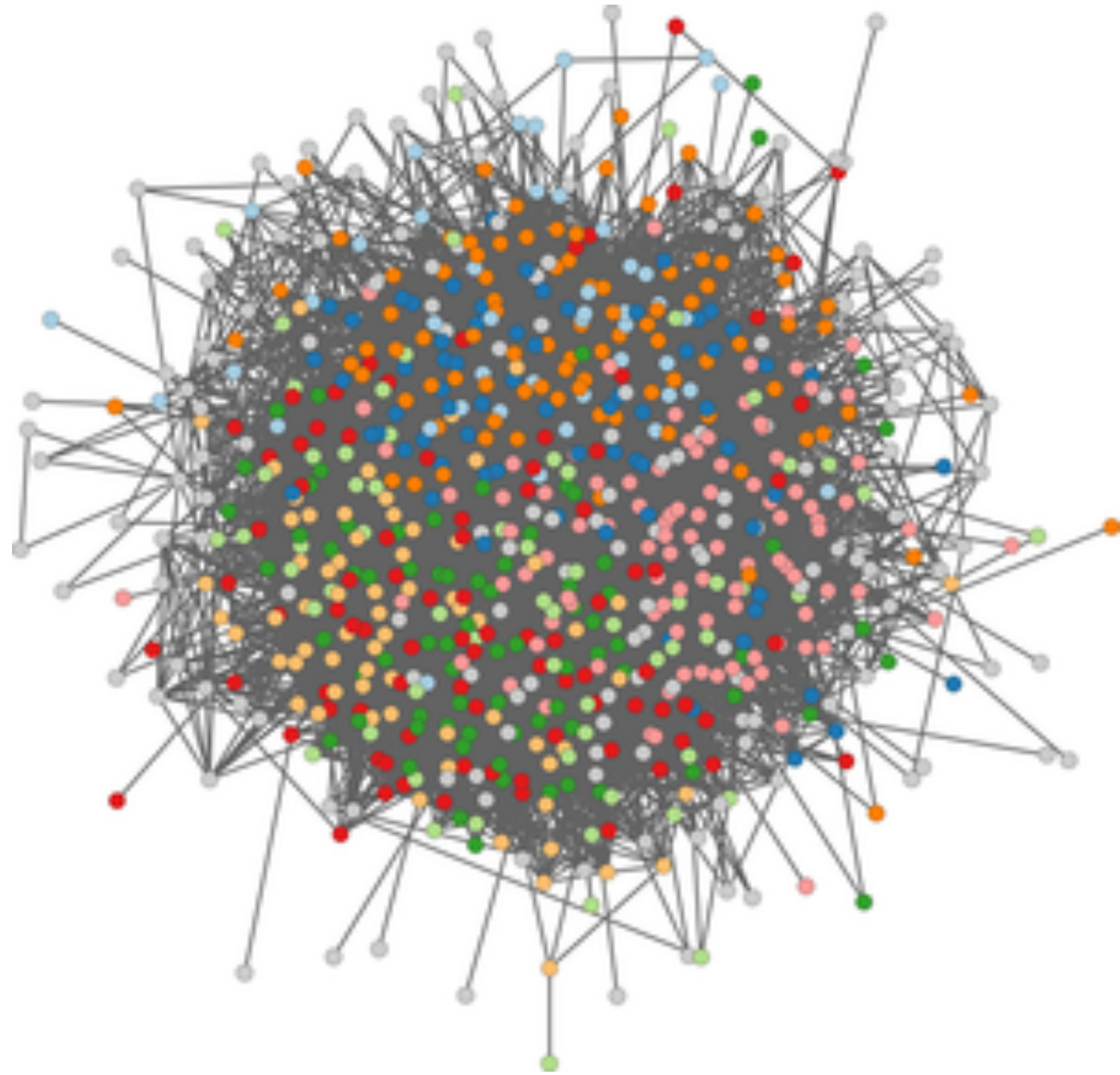
Activity for all of January 2015

```
wget http://data.gharchive.org/2015-01-{01..31}-{0..23}.json.gz
```

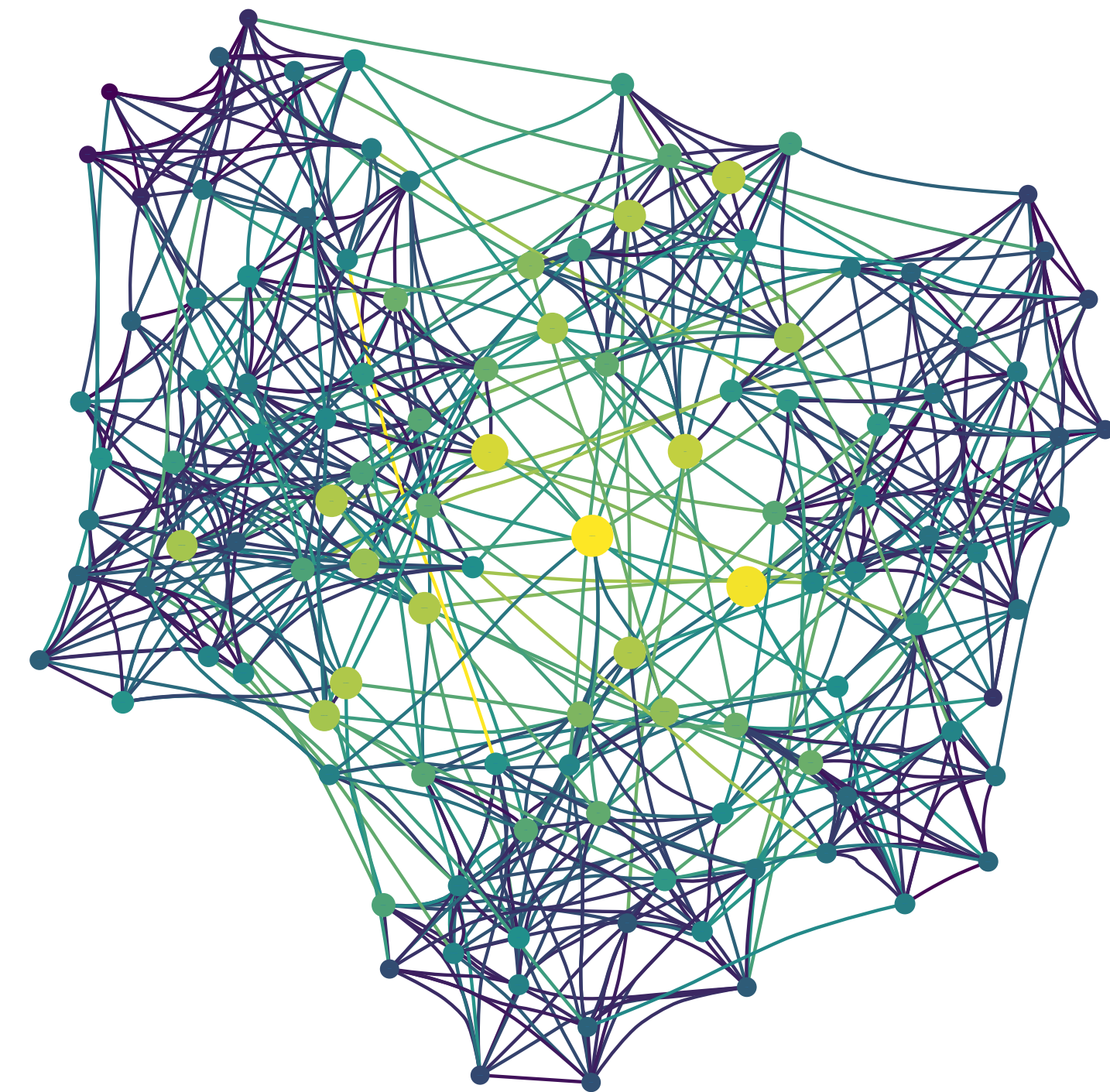
Common task: thinning



# Common task: thinning



vs.



# Common task: thinning (subsetting)

*Sometimes* necessary to remove spurious links and/or nodes

Remove singleton nodes?

Remove nodes with degree  $< k$

→ k-cores

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 Temporal network?

- Keep nodes/links of a certain **age**
- Consider a certain **time window**
- But how to pick? 🤔

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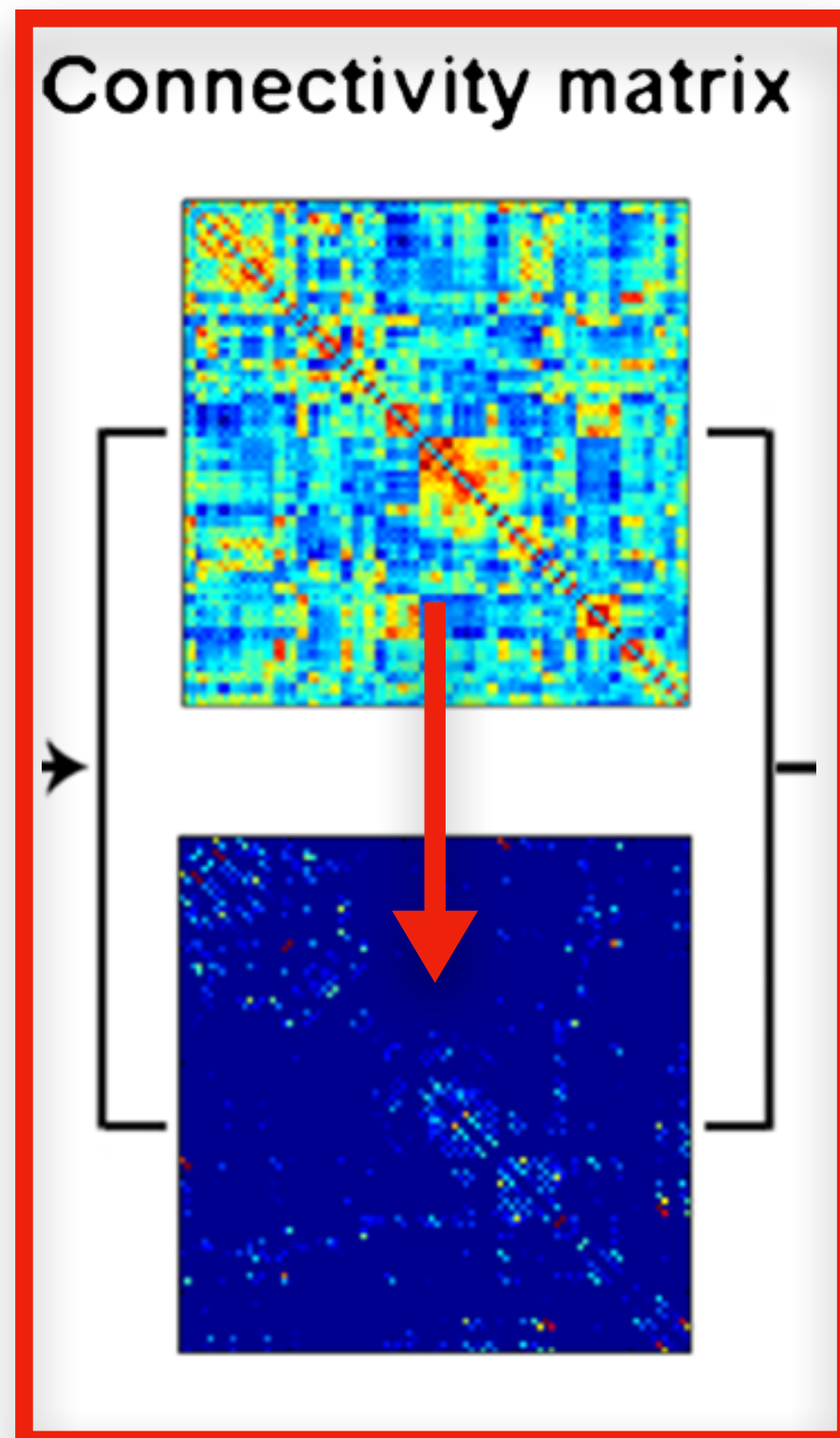


Choices depend on problem area, type of data, and your scientific goals

# Common task: thinning

Network is very dense, lots of potentially spurious edges

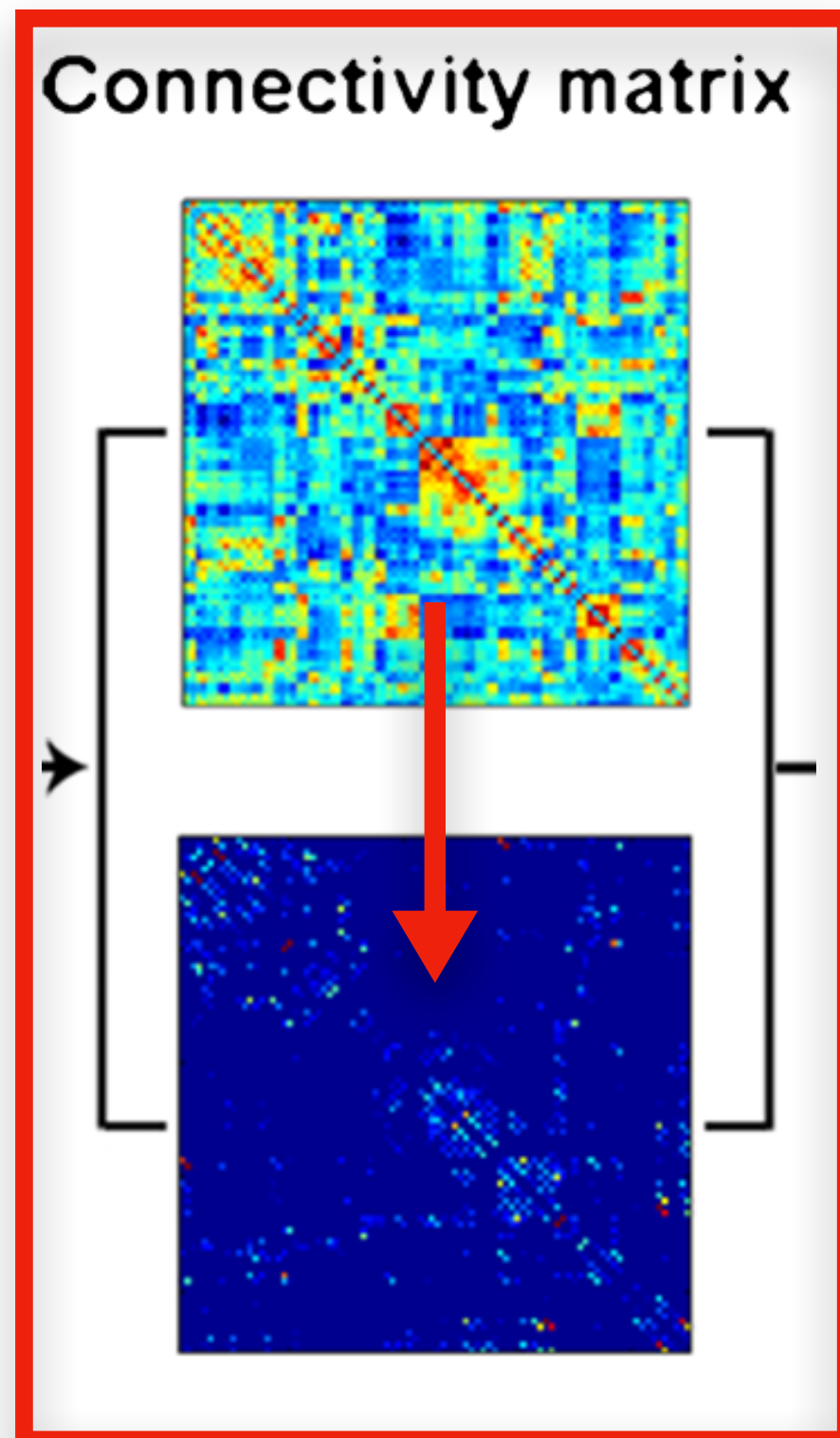
**How to sparsify?**



# Common task: thinning

Network is very dense, lots of potentially spurious edges

**How to sparsify?**



Threshold this matrix?



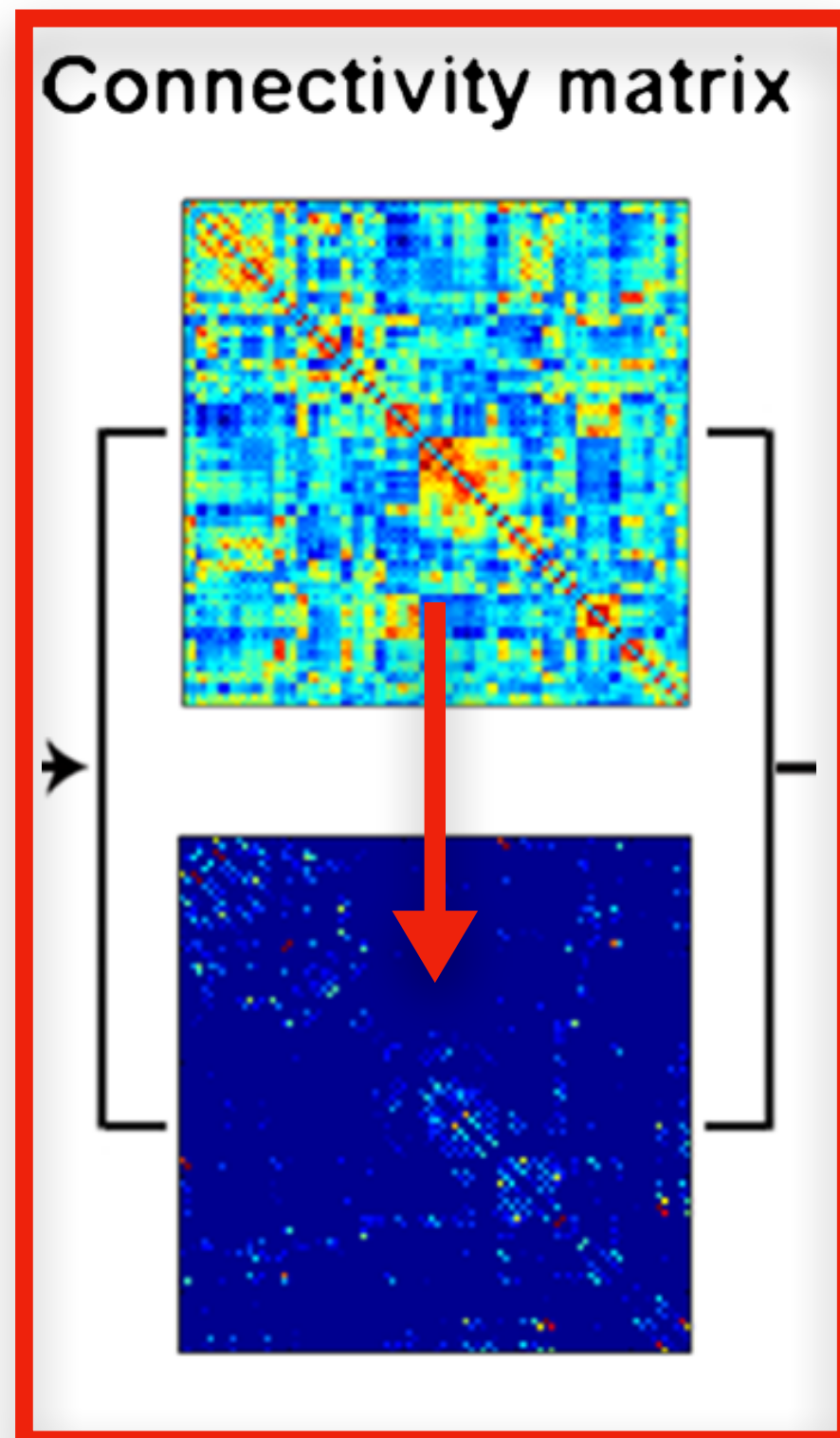
Edge  $(i,j)$  exists if  $w_{ij} > \text{cutoff}$

weighted network

# Common task: thinning

Network is very dense, lots of potentially spurious edges

**How to sparsify?**

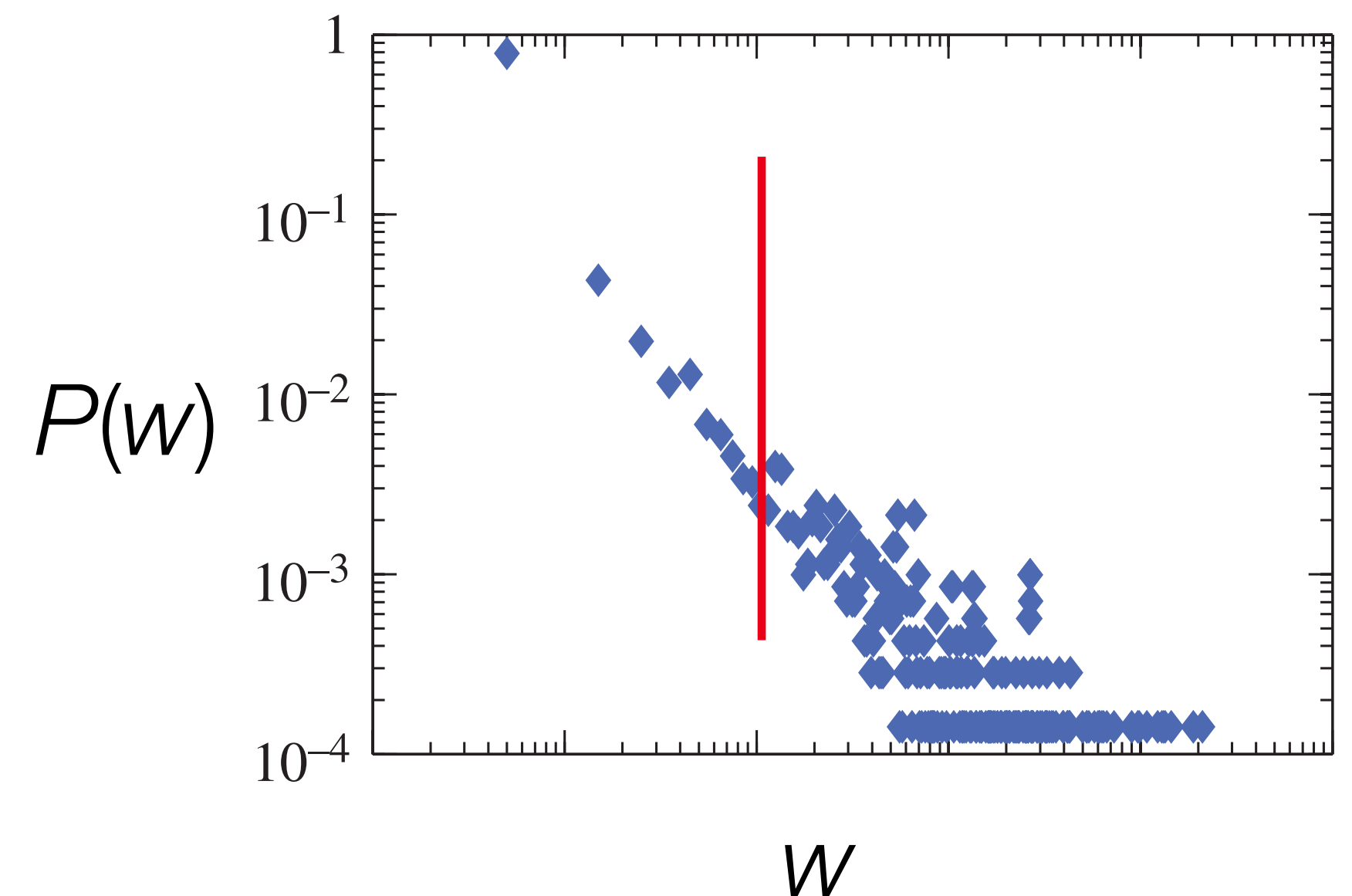


Threshold this matrix?



Edge  $(i,j)$  exists if  $w_{ij} >$  **cutoff**

weighted network



# Common task: thinning

Idea: Use a **local threshold**

## **Extracting the multiscale backbone of complex weighted networks**

M. Ángeles Serrano<sup>a,1</sup>, Marián Boguñá<sup>b</sup>, and Alessandro Vespignani<sup>c,d</sup>



# Common task: thinning

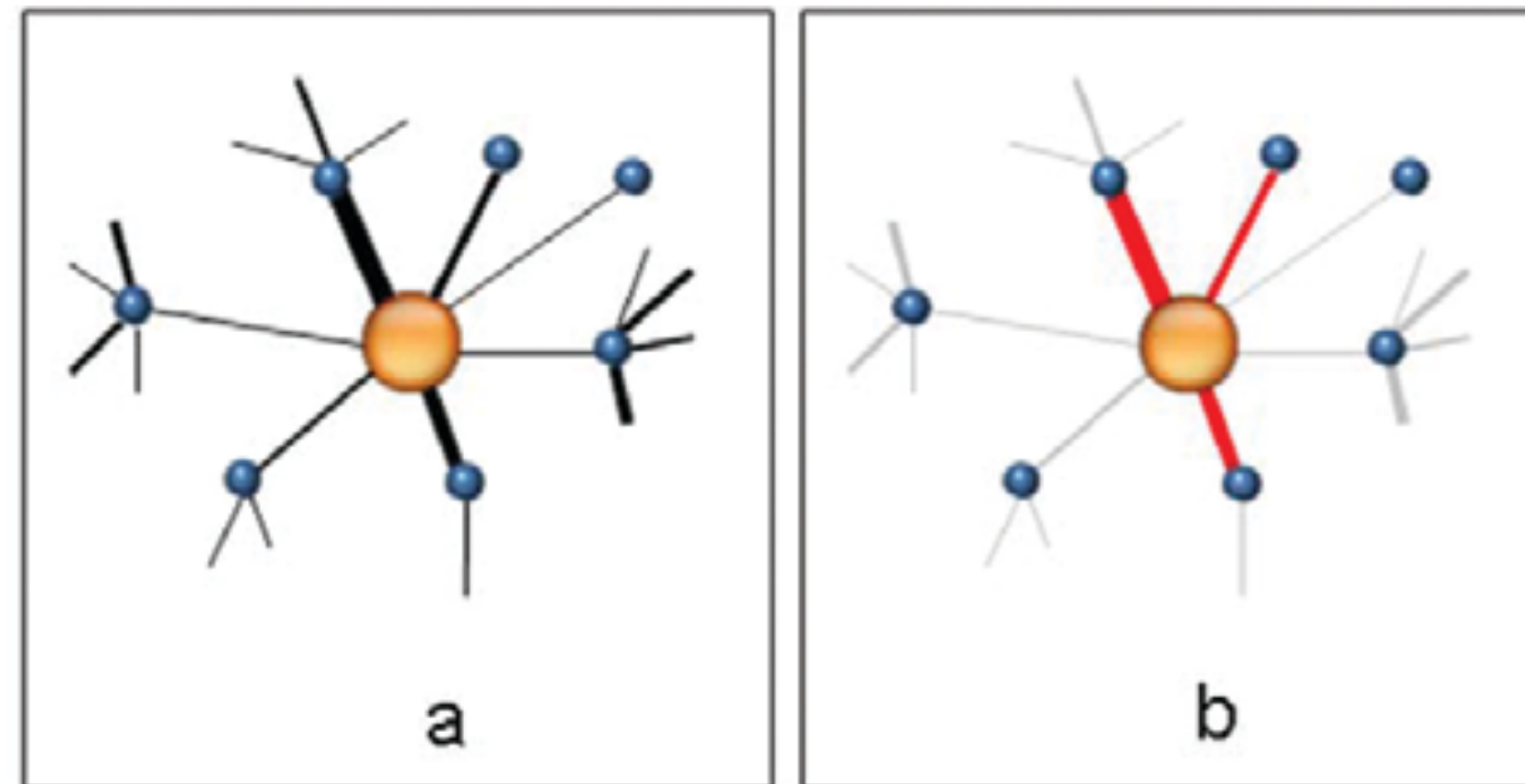
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## Extracting the multiscale backbone of complex weighted networks

M. Ángeles Serrano<sup>a,1</sup>, Marián Boguñá<sup>b</sup>, and Alessandro Vespignani<sup>c,d</sup>

Normalize weights in the neighborhood of a node:

$$p_{ij} = \frac{w_{ij}}{\sum_j w_{ij}}$$



# Common task: thinning

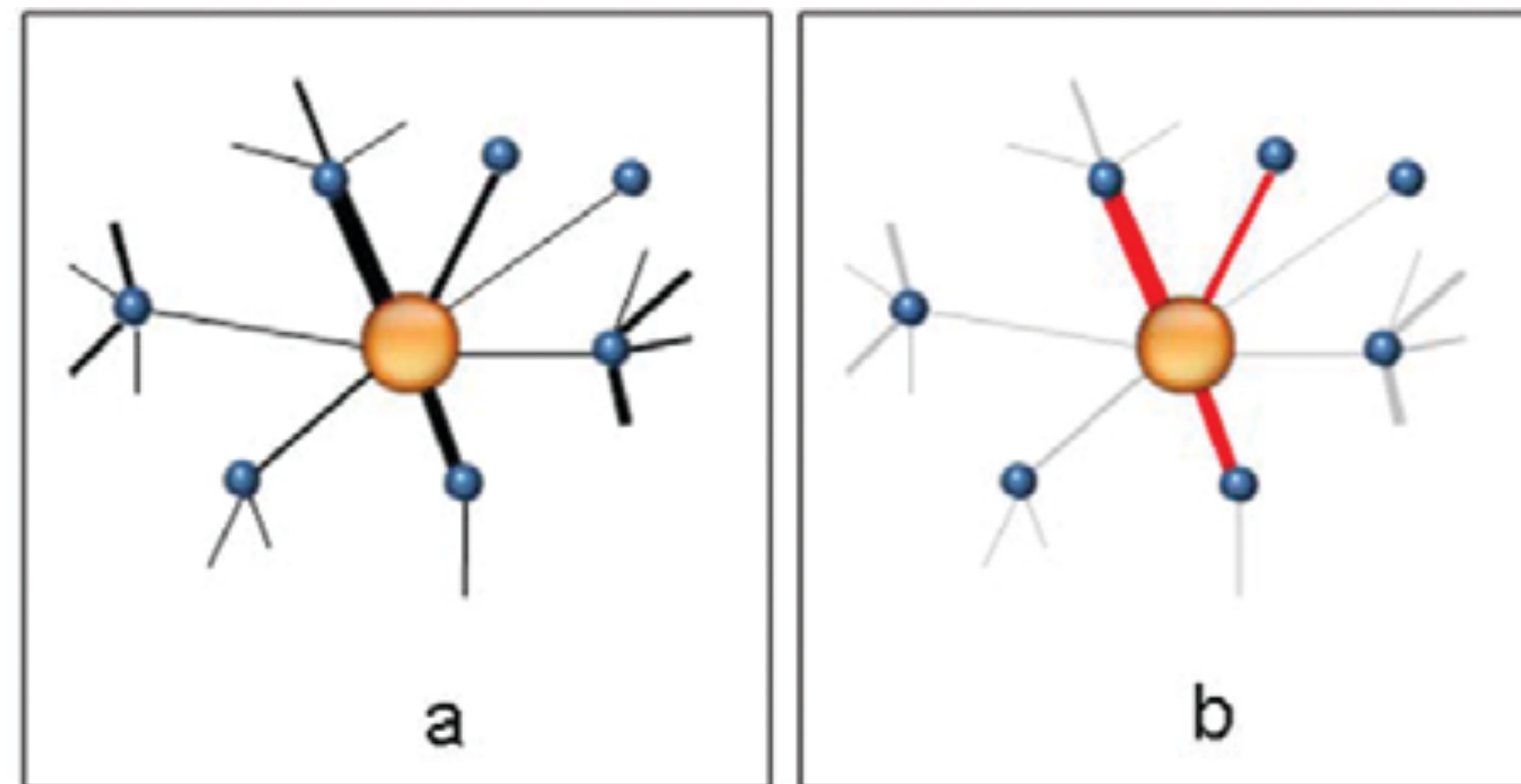
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$$p_{ij} = \frac{w_{ij}}{\sum_j w_{ij}}$$



Keep  $(i,j)$  with statistically significant values  $p_{ij}$

How?

# Common task: thinning

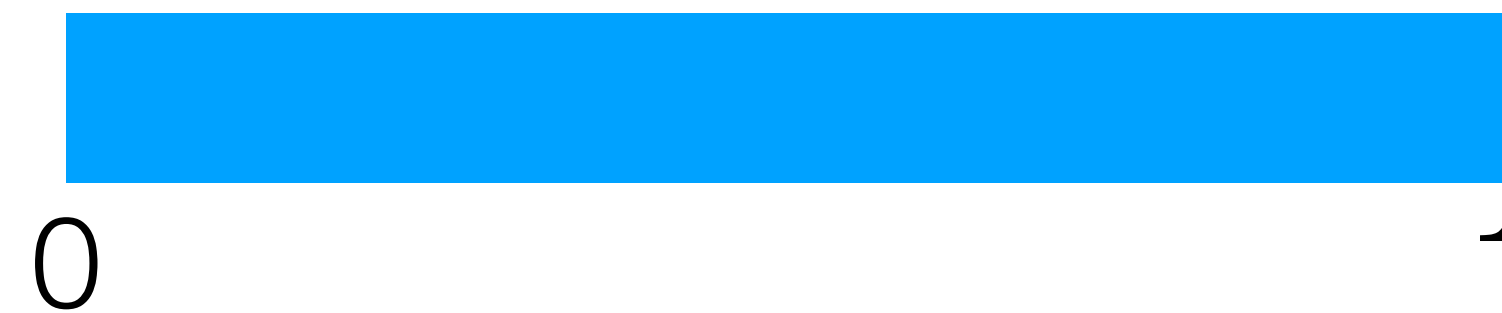
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Because  $p_{ij}$  sum to 1, imagine dropping  $k_i - 1$  points uniformly at random onto  $[0, 1]$

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M. Ángeles Serrano<sup>a,1</sup>, Marián Boguñá<sup>b</sup>, and Alessandro Vespignani<sup>c,d</sup>



What's the prob of getting a gap between points at least as big as the observed  $p_{ij}$ ?

# Common task: thinning

Idea: Use a **local threshold**

Normalize weights in the neighborhood of a node:

$$p_{ij} = \frac{w_{ij}}{\sum_j w_{ij}}$$

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M. Ángeles Serrano<sup>a,1</sup>, Marián Boguñá<sup>b</sup>, and Alessandro Vespignani<sup>c,d</sup>



Keep edges where:

$$1 - (k_i - 1) \int_0^{p_{ij}} (1 - x)^{k_i - 2} dx = (1 - p_{ij})^{k_i - 1} < \alpha$$

# Common task: thinning

```
import networkx # http://networkx.github.io

def extract_backbone(G, weights, alpha):
    keep_graph = networkx.Graph()
    for i in G:
        neighbors = G[i]
        k = len(neighbors)
        if k > 1:
            W = sum( weights[i,j] for j in neighbors )
            for j in neighbors:
                pij = 1.0*weights[i,j]/W
                if (1-pij)**(k-1) < alpha: # edge significant
                    keep_graph.add_edge( i,j )
    return keep_graph
```

Easy to implement!



# Common task: thinning

## *Robustness and modular structure in networks*

JAMES P. BAGROW

*Mathematics & Statistics, University of Vermont, Burlington, VT, USA*

*and*

*Center for Complex Network Research, Northeastern University, Boston, MA, USA*

*(e-mail: james.bagrow@uvm.edu)*

SUNE LEHMANN

*DTU Informatics, Technical University of Denmark, Kgs Lyngby, Denmark*

*and*

*College of Computer and Information Science, Northeastern University, Boston, MA, USA*

*(e-mail: sljo@dtu.dk)*

YONG-YEOL AHN

*School of Informatics & Computing, Indiana University, Bloomington IN, USA*

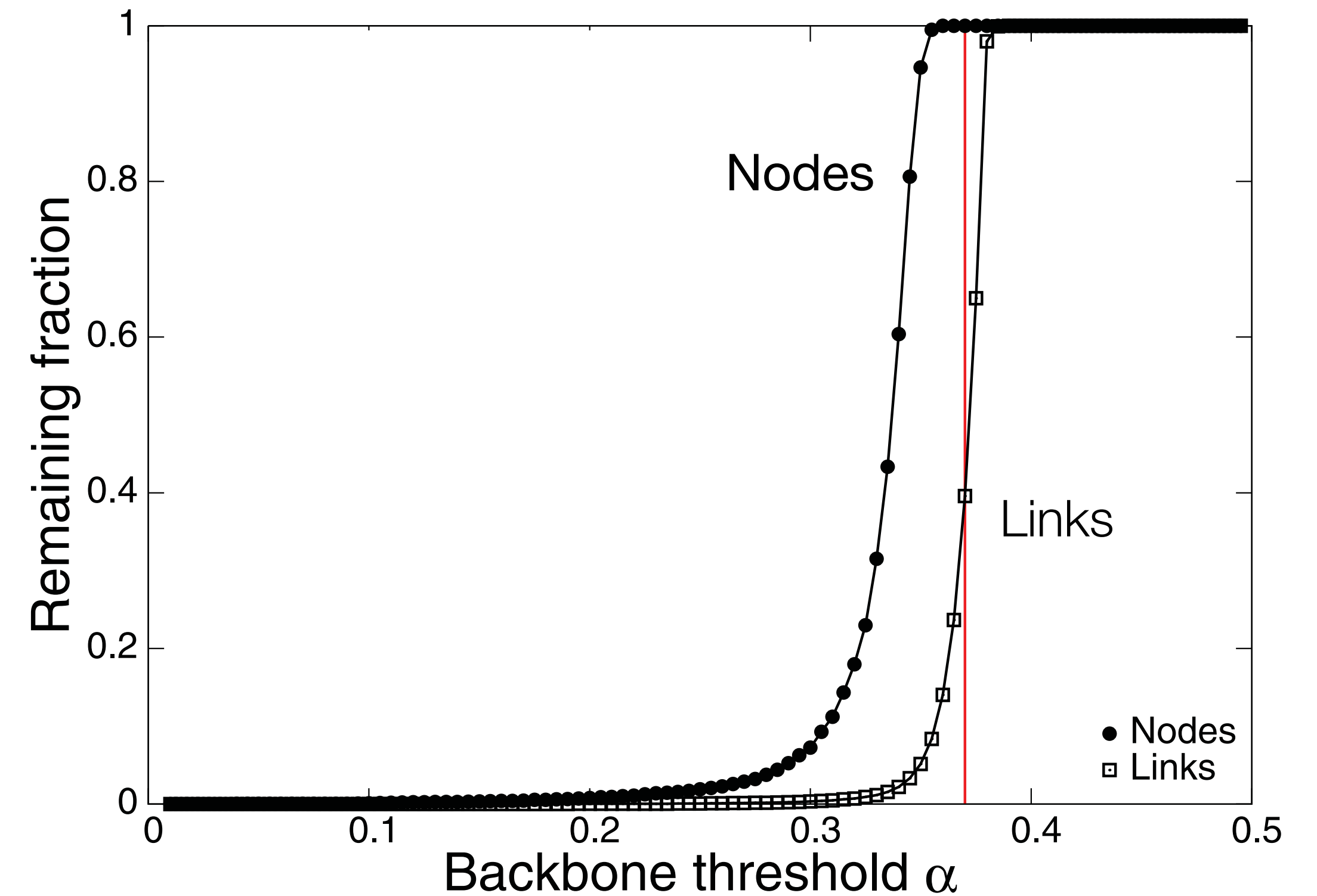
*and*

*Center for Complex Network Research, Northeastern University, Boston, MA, USA*

*(e-mail: yyahn@indiana.edu)*

Example where I used the method

Applied to fMRI data



*If an analysis depends on a parameter, be sure to explore values of that parameter*



Case study:

Nodes are ambiguous

## Inferring the size of the causal universe: features and fusion of causal attribution networks

Daniel Berenberg<sup>1,2</sup> and James P. Bagrow<sup>3,2,\*</sup>

<sup>1</sup>Department of Computer Science, University of Vermont, Burlington, VT, United States

<sup>2</sup>Vermont Complex Systems Center, University of Vermont, Burlington, VT, United States

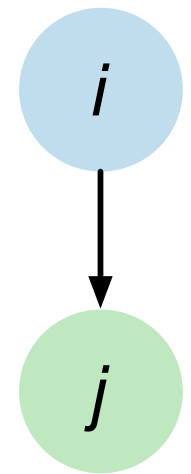
<sup>3</sup>Department of Mathematics & Statistics, University of Vermont, Burlington, VT, United States

\*Corresponding author. Email: [james.bagrow@uvm.edu](mailto:james.bagrow@uvm.edu), Homepage: [bagrow.com](http://bagrow.com)

December 14, 2018

Crowdsourced **knowledge graphs**

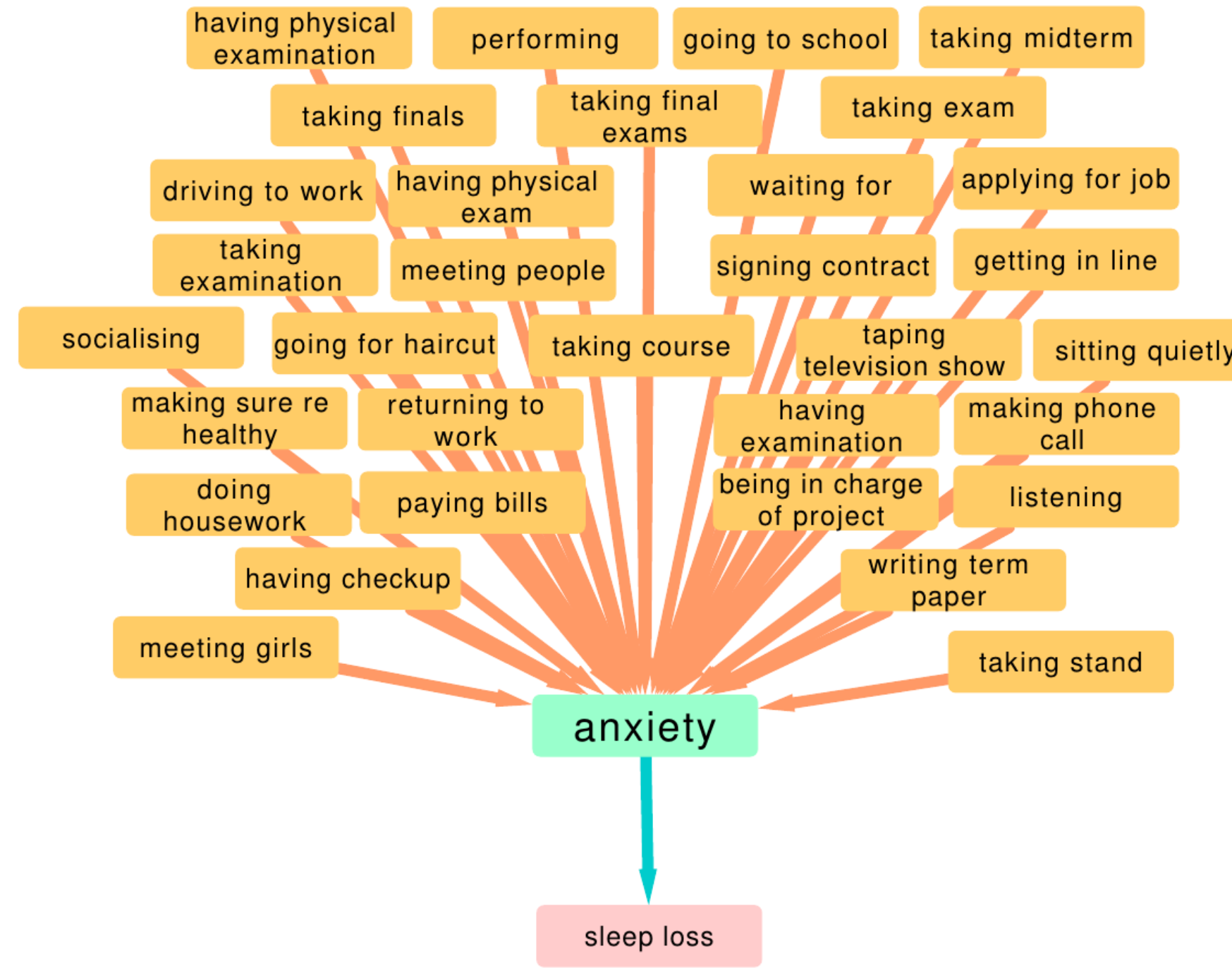
# Knowledge graphs



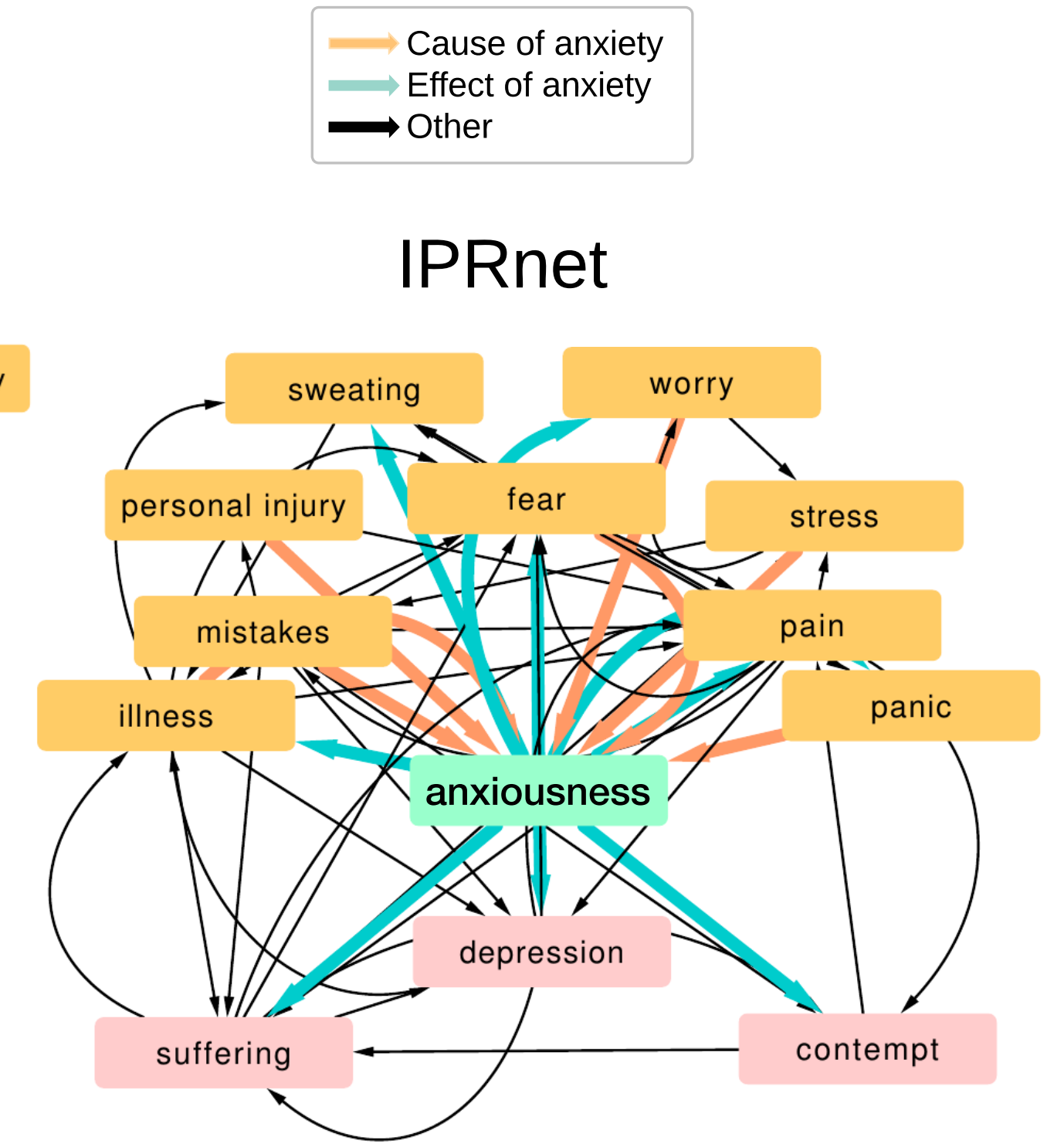
$s_i = \text{"anxiety"}$

$s_j = \text{"sleep loss"}$

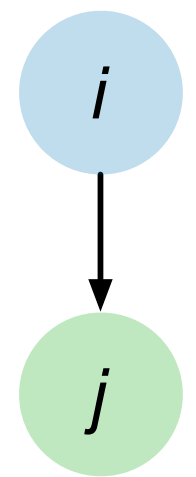
## ConceptNet



## IPRnet

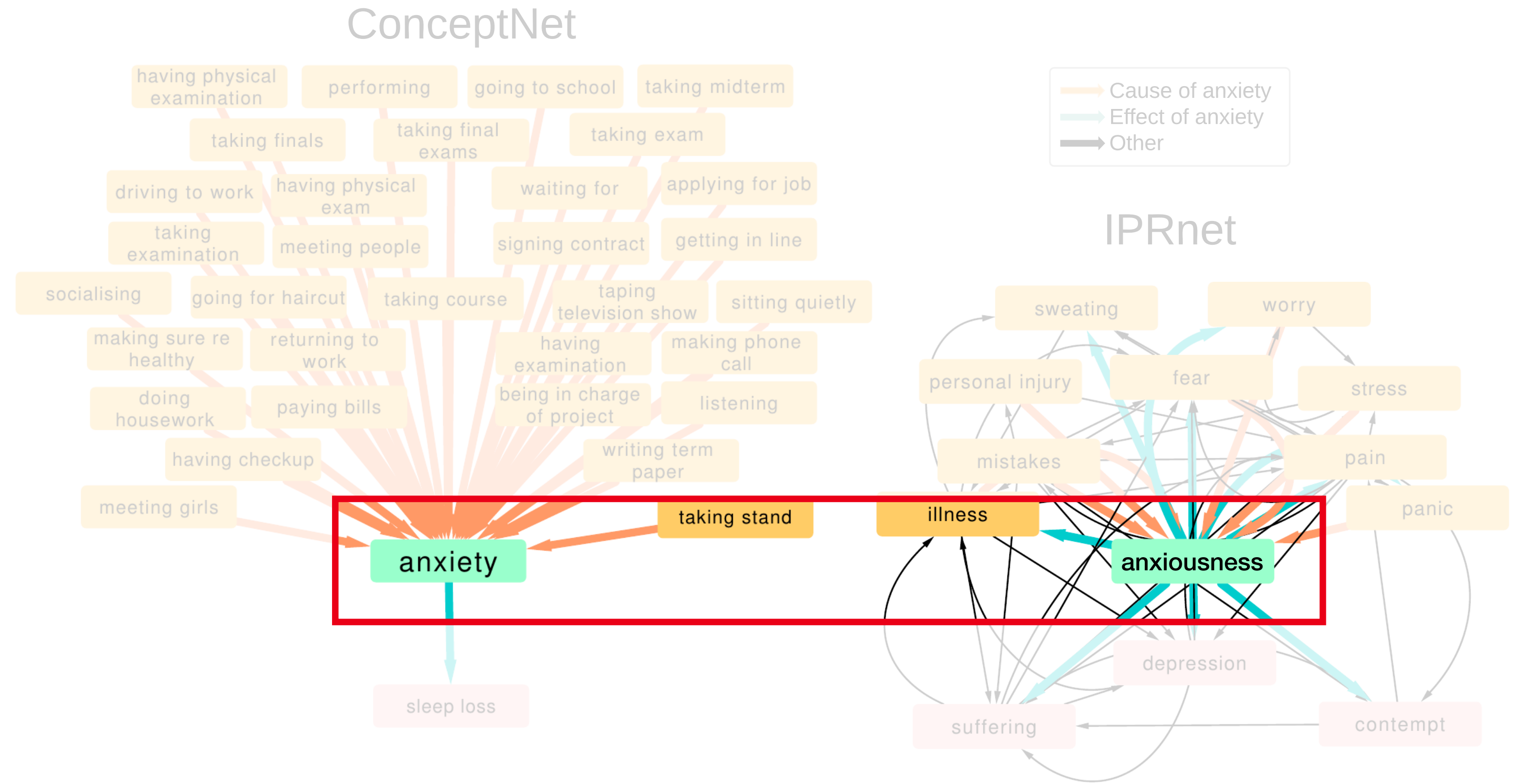


# Knowledge graphs



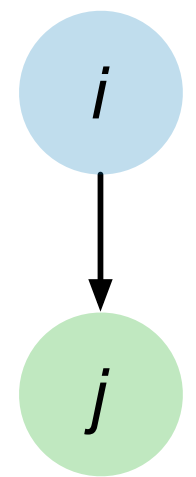
$s_i = \text{"anxiety"}$

$s_j = \text{"sleep loss"}$



Nodes are identified *only* by these text...  
Could be ambiguous, even within one network...

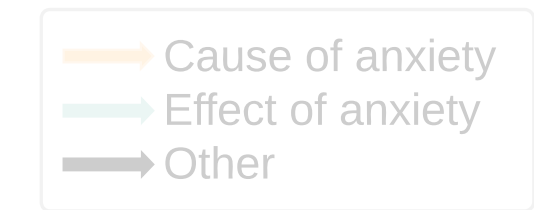
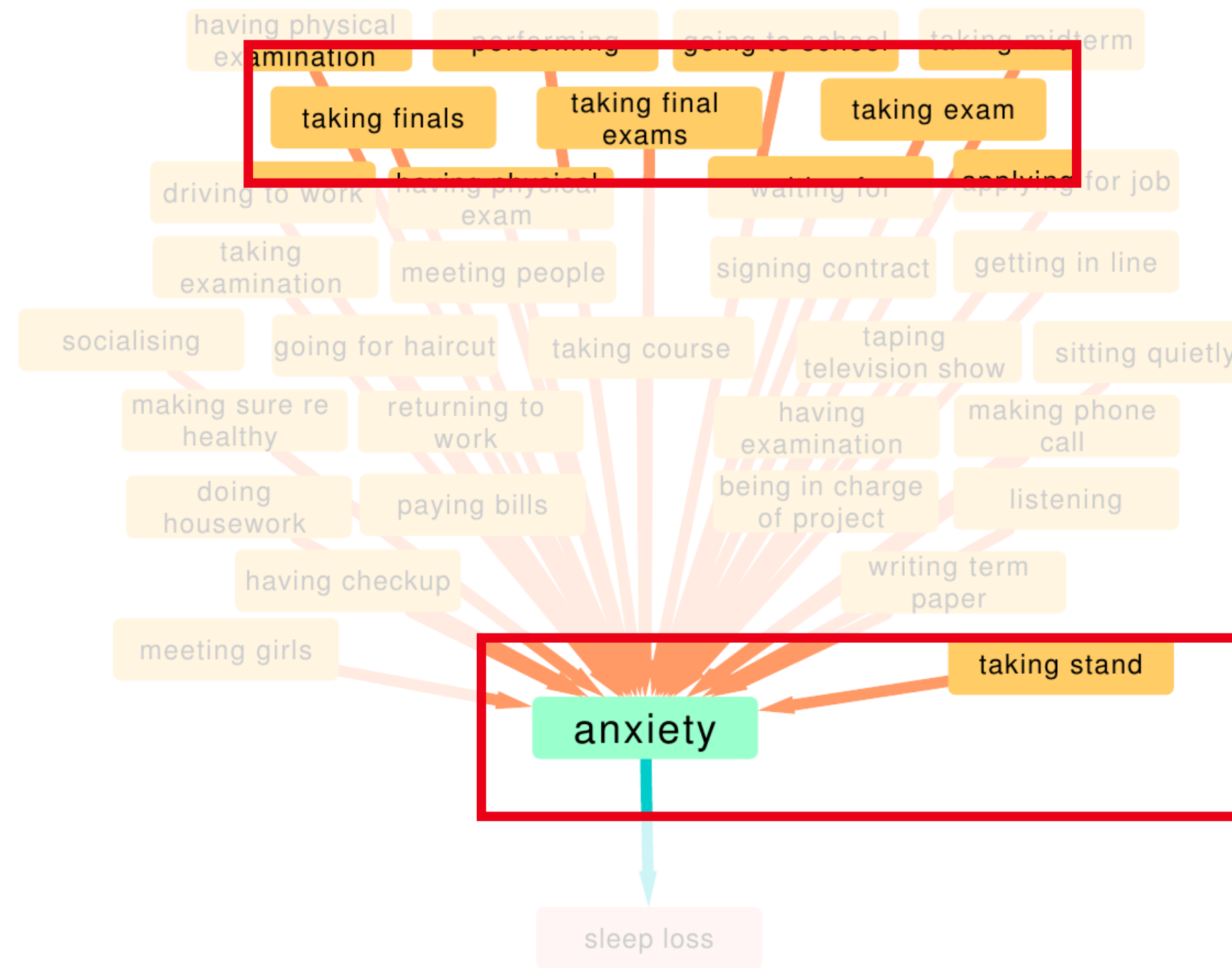
# Knowledge graphs



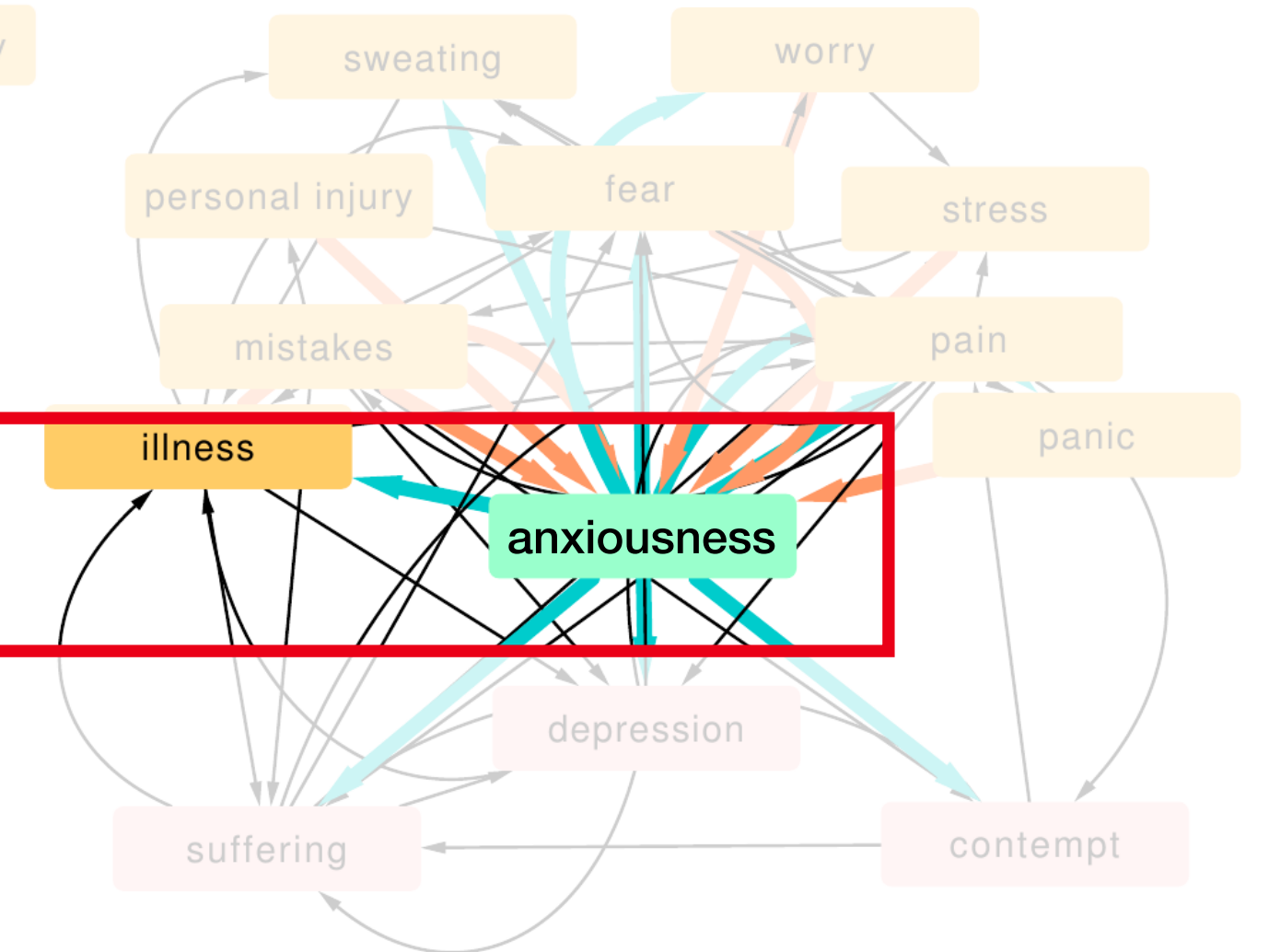
$s_i = \text{"anxiety"}$

$s_j = \text{"sleep loss"}$

ConceptNet

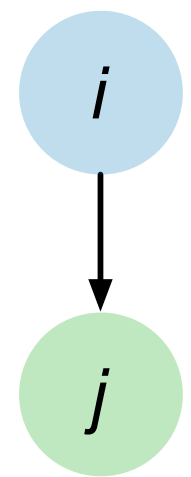


IPRnet



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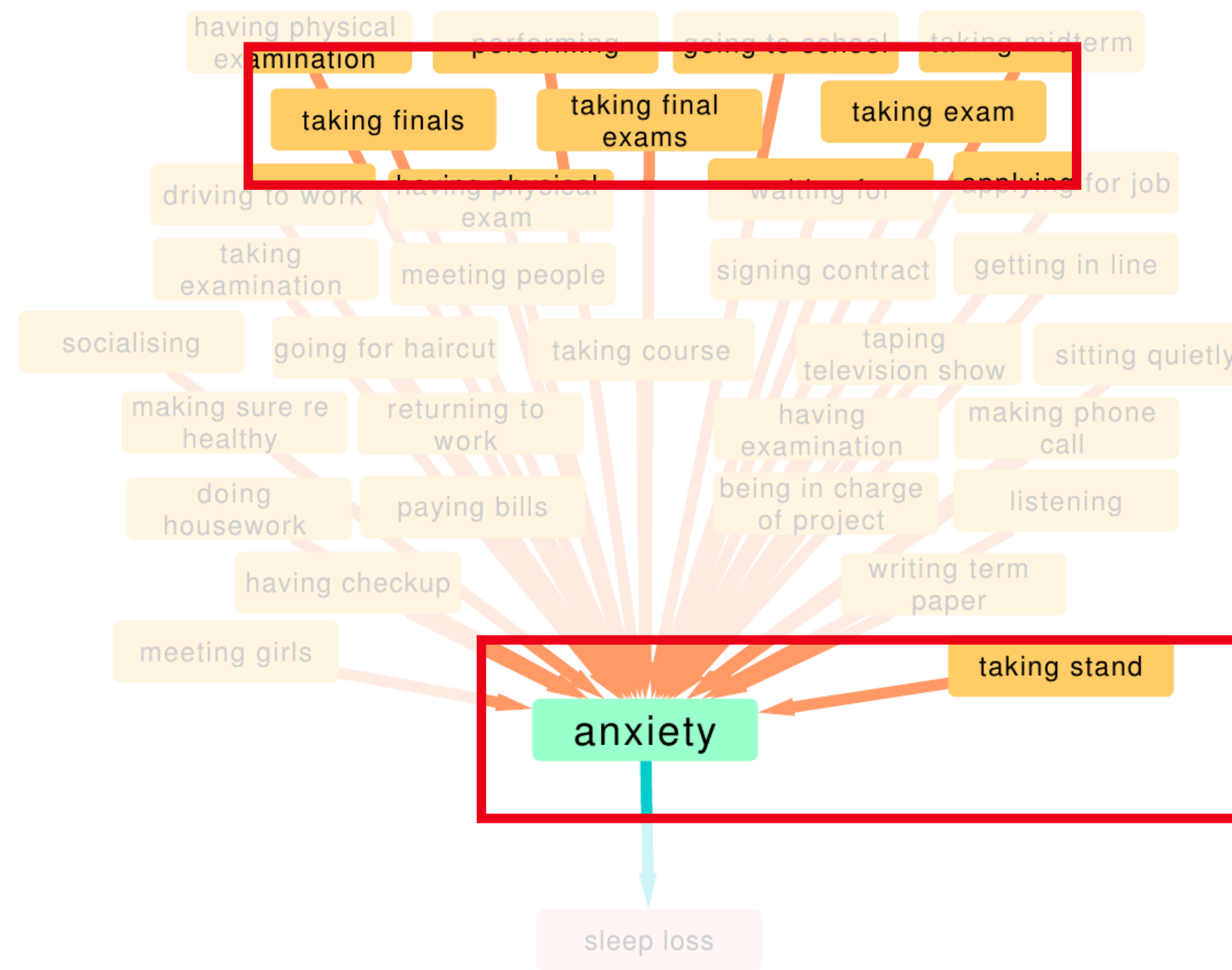
# Knowledge graphs



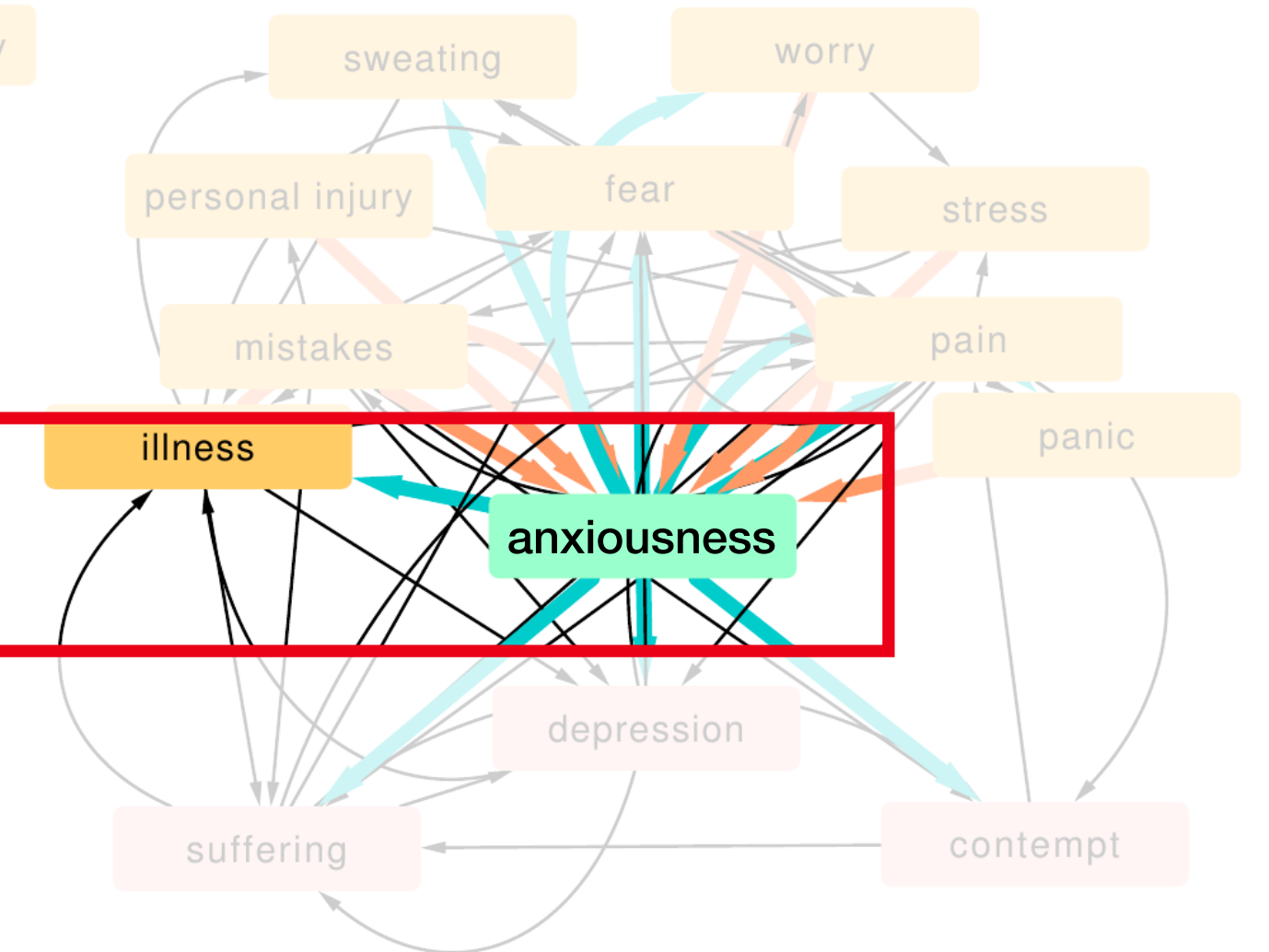
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ConceptNet



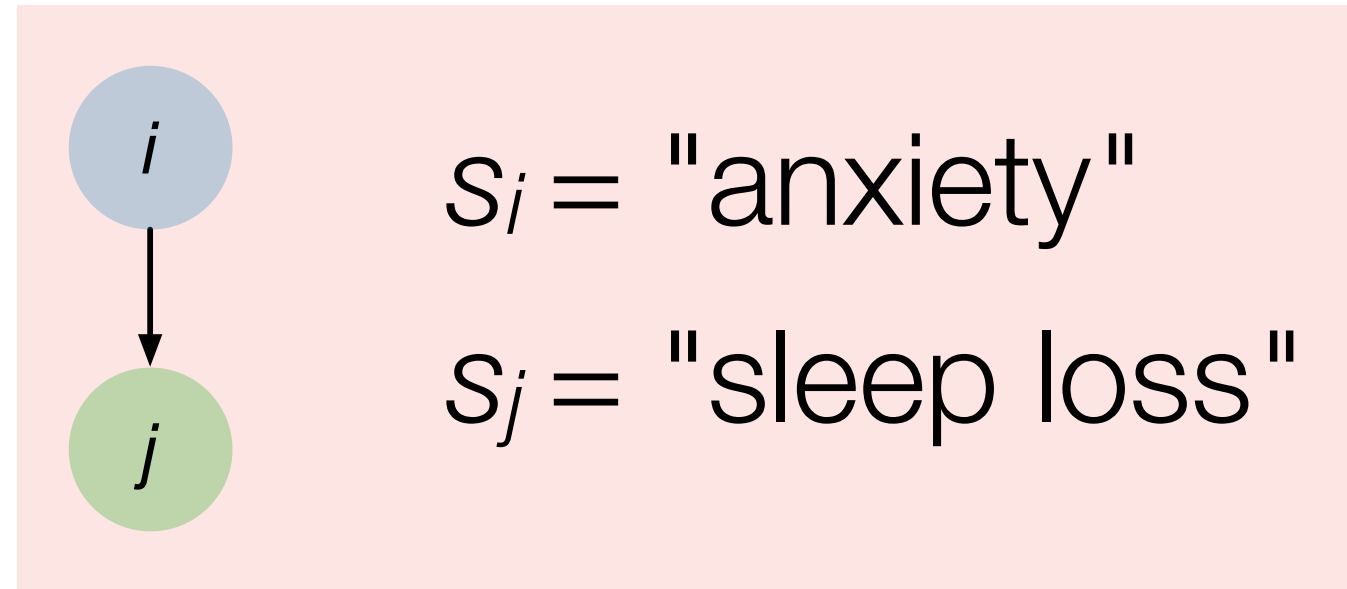
IPRnet



Nodes are identified *only* by these text...  
Could be ambiguous, even within one network...

Can we combine these different networks together?

# NetFUSES: Network FUsion with SEmantic Similarity



Threshold  $S(s_i, s_j) \geq t \quad i, j \in V_1 \cup V_2$

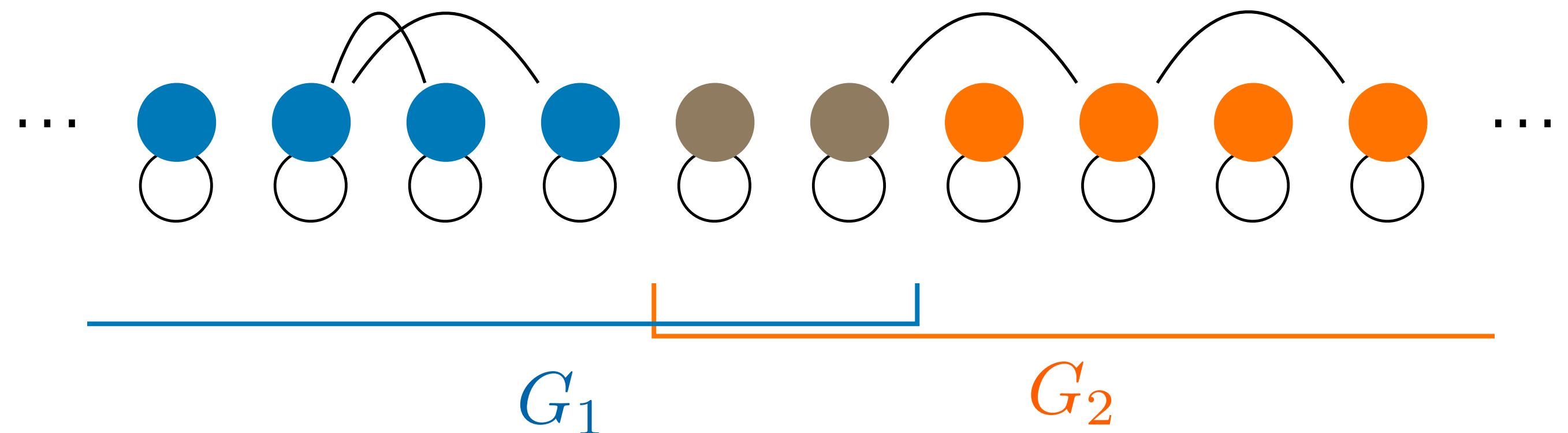
Define a **semantic similarity**  $S$  between sentences:

$$S(s_i, s_j) \leq 1$$

$$S(s_i, s_i) = 1$$

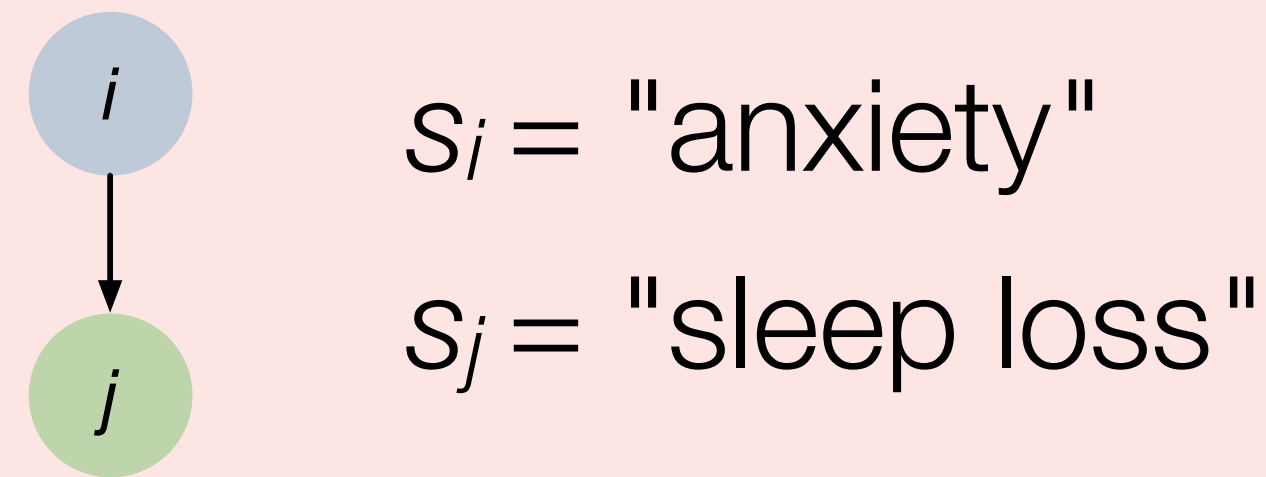
$$S(s_i, s_j) = S(s_j, s_i)$$

edges of a *fusion indicator graph*:



Fuse nodes using connected components

# NetFUSES: Network FUsion with SEmantic Similarity



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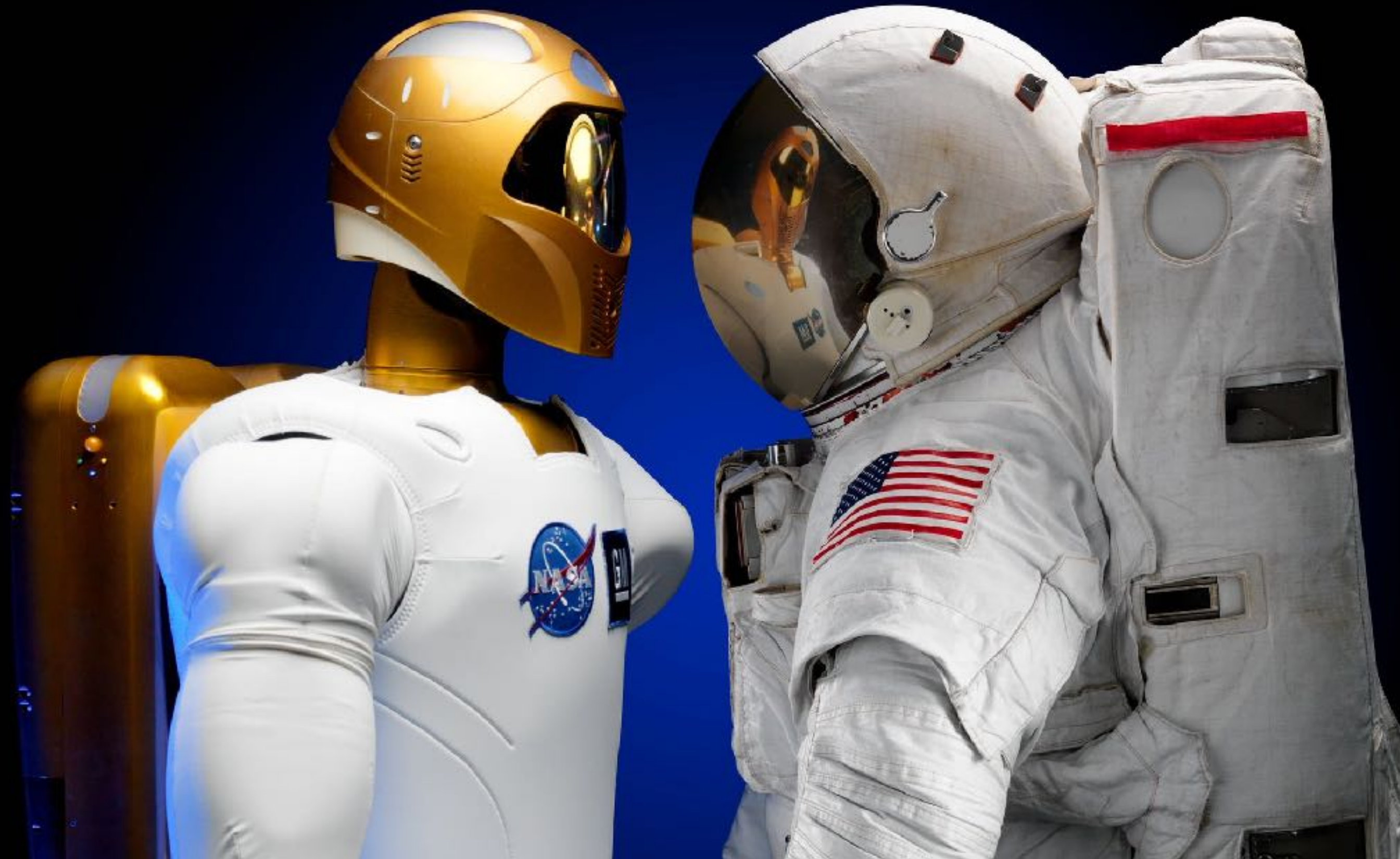
edges of a *fusion indicator graph*:

... **How to measure semantic similarity of text?** ...

*Fuse nodes using connected components*

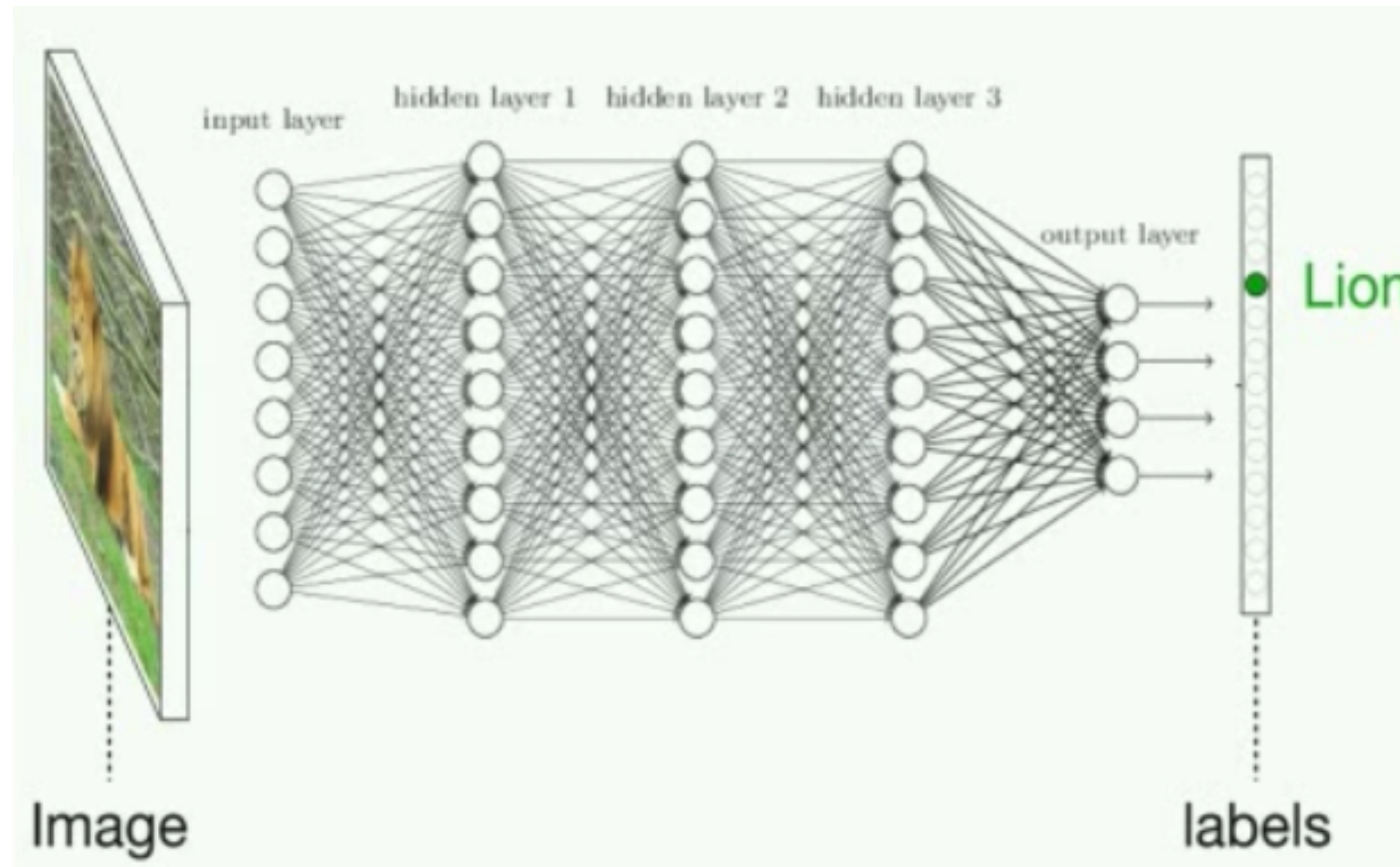
# Machine Learning

(How to measure semantic similarity of text?)





# Measuring semantic similarity with neural networks



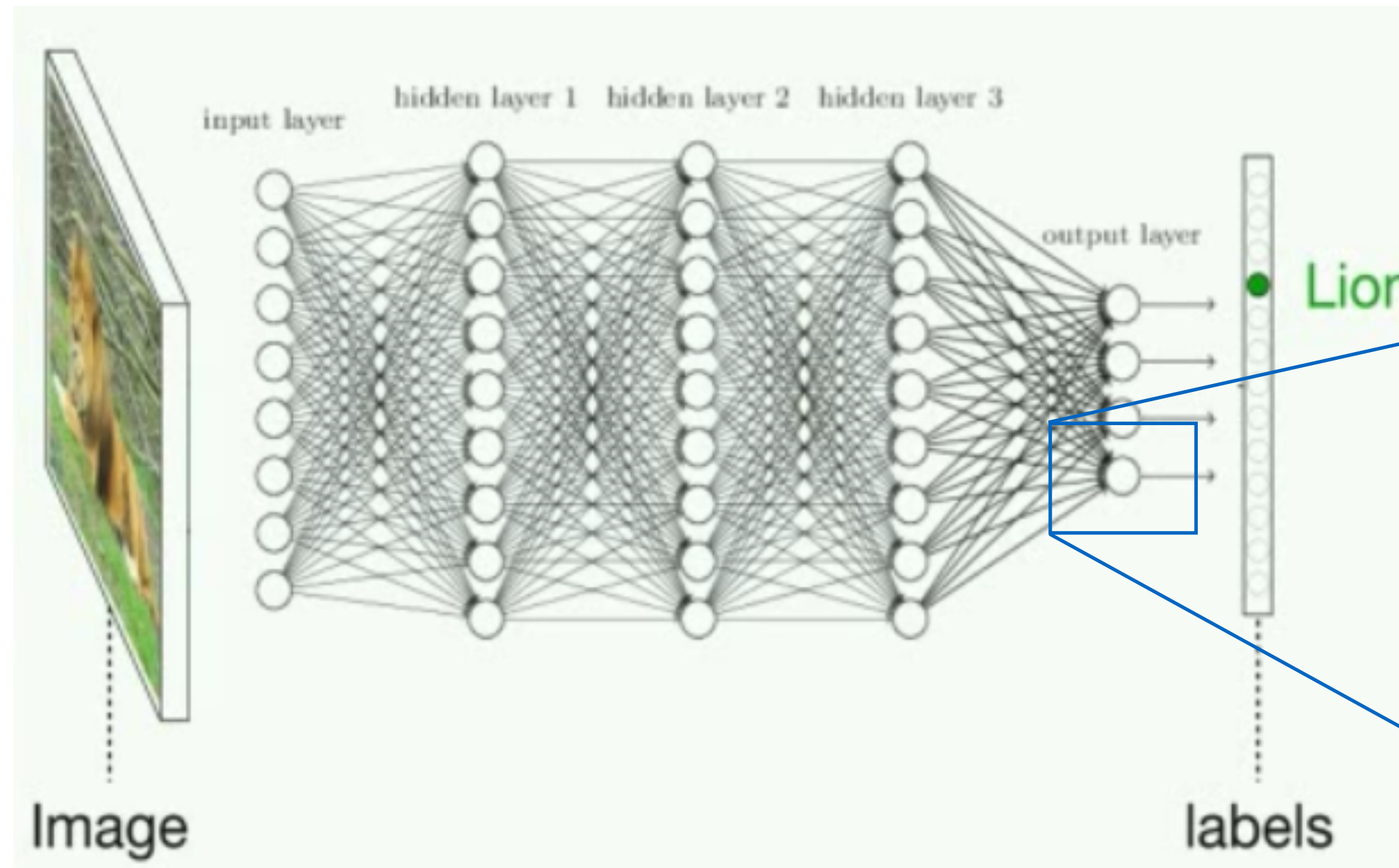
[Image: Jeff Clune](#)

Example: image classification

using training data: labeled images

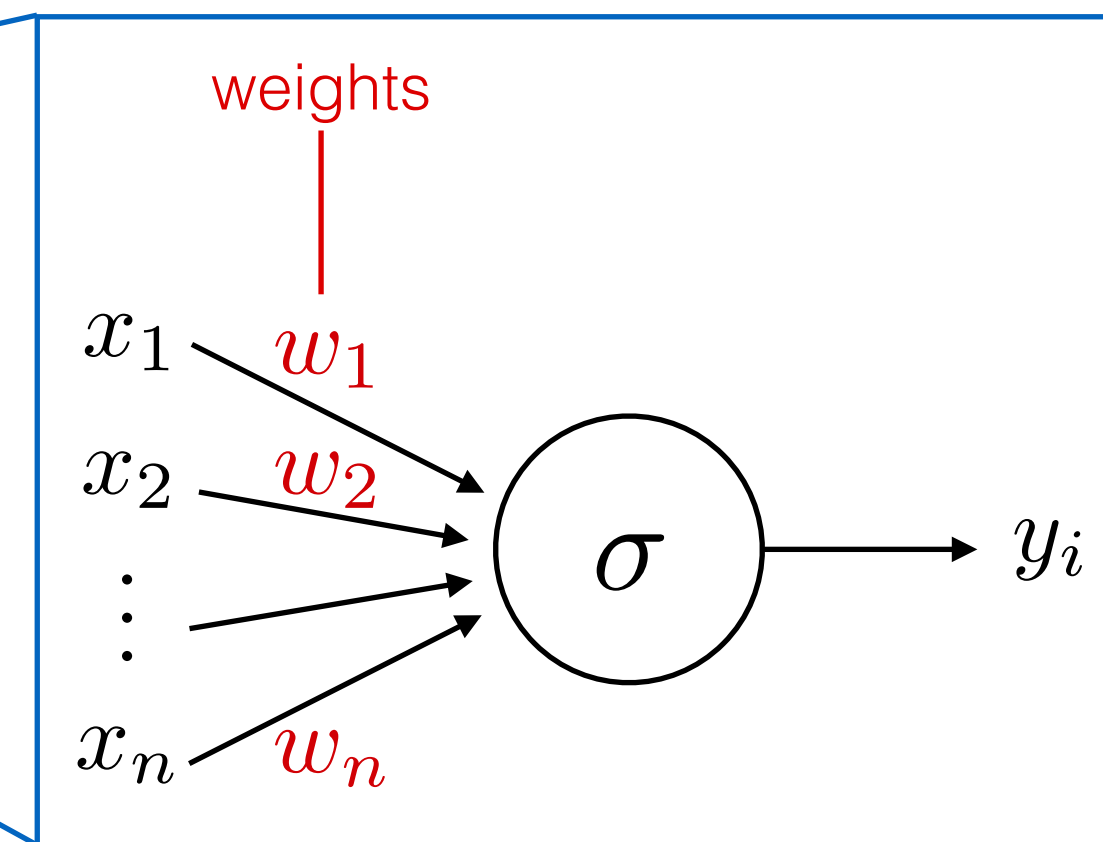
..., (  , 'lion'), ...

# Measuring semantic similarity with neural networks



[Image: Jeff Clune](#)

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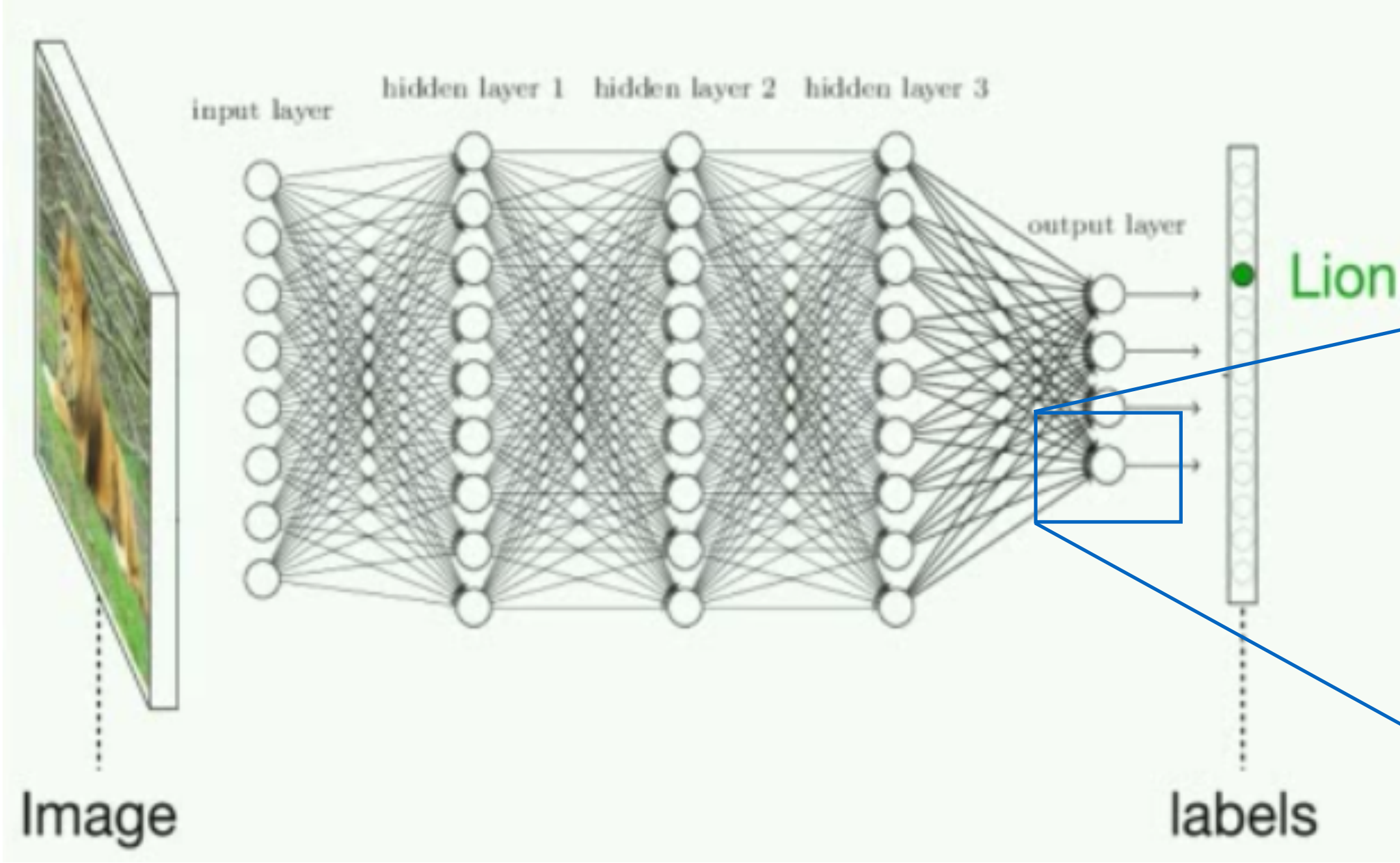


$$y = \sigma(\mathbf{w}^T \mathbf{x})$$

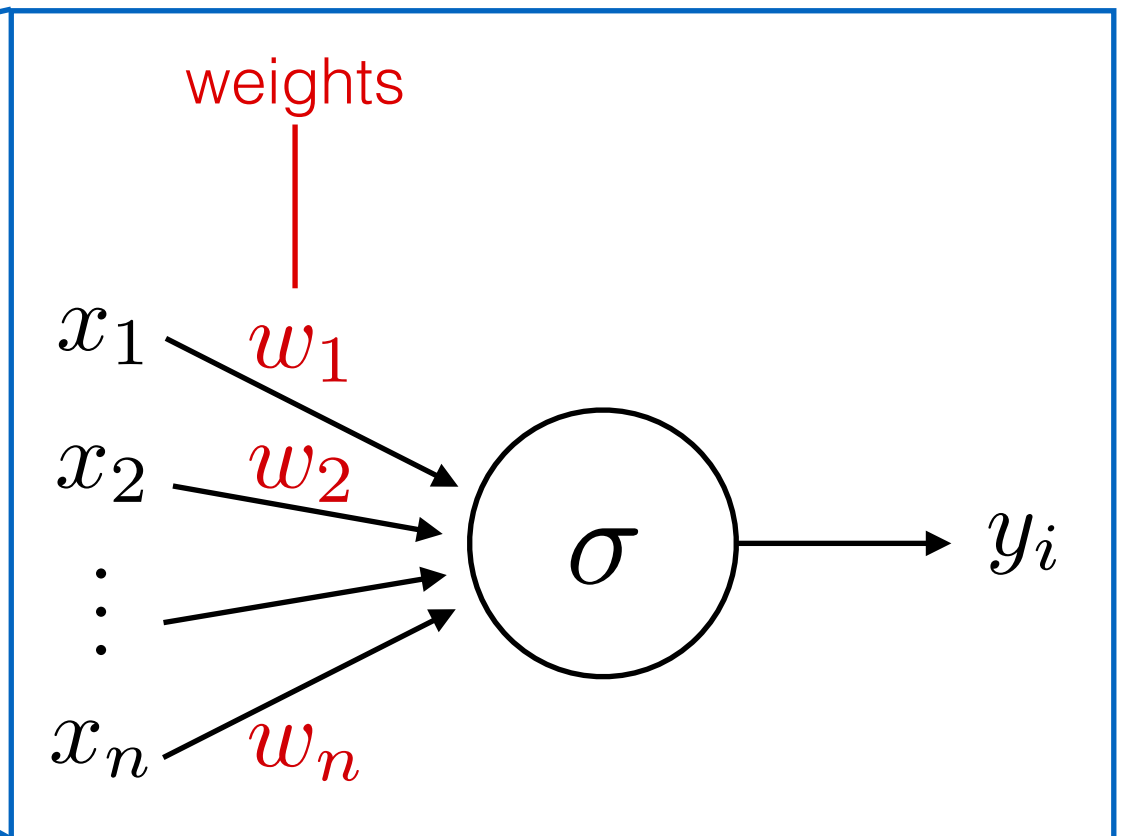
using training data: labeled images

..., ( , 'lion'), ...

# Measuring semantic similarity with neural networks



Example: image classification



$$y = \sigma(\mathbf{w}^T \mathbf{x})$$

[Image: Jeff Clune](#)

using training data: labeled images

What training data can we use for text?

..., (  , 'lion'), ...

“You shall know a word by the company  
it keeps.”

–JR Firth

Distributional Semantics

“You shall know a word by the company  
it keeps.”

–JR Firth

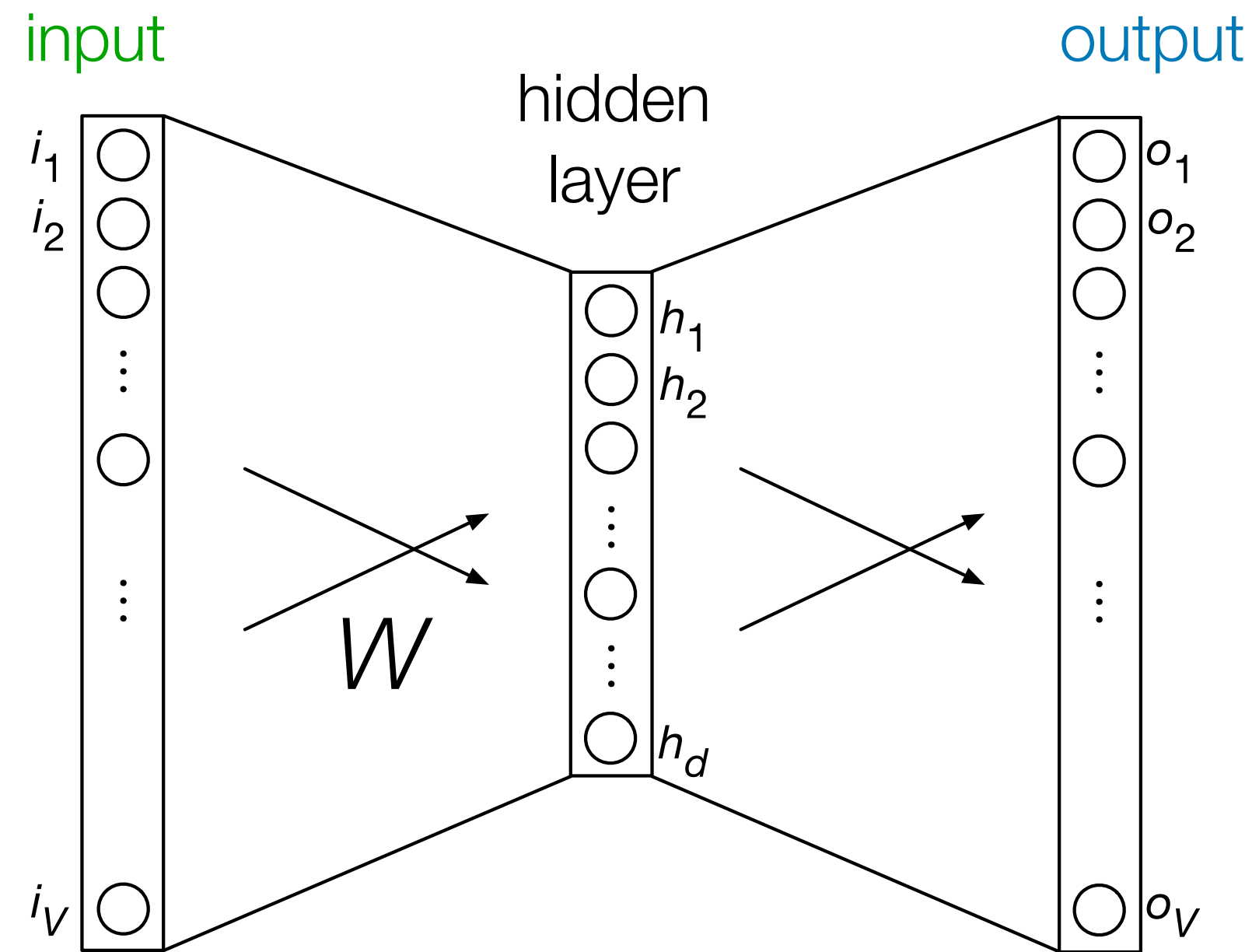
## Distributional Semantics

... worlds are yours except europa attempt no landings there ...

Turn *large* text corpus into collection  
of **word-context** pairs

Predict **word**  
from **context**

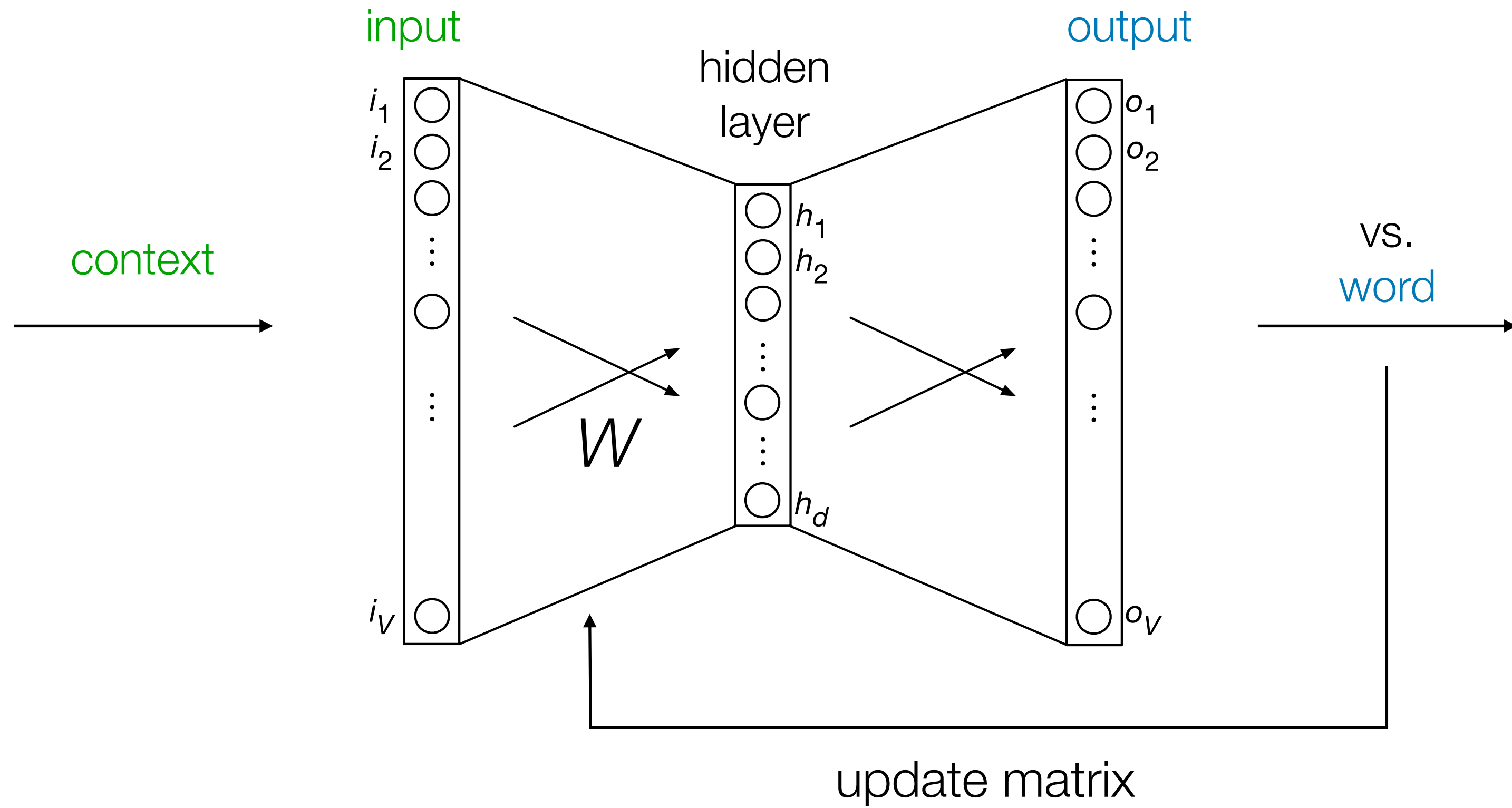
*Training data*



(Or predict **context**  
from **word**!)

Predict **word**  
from **context**

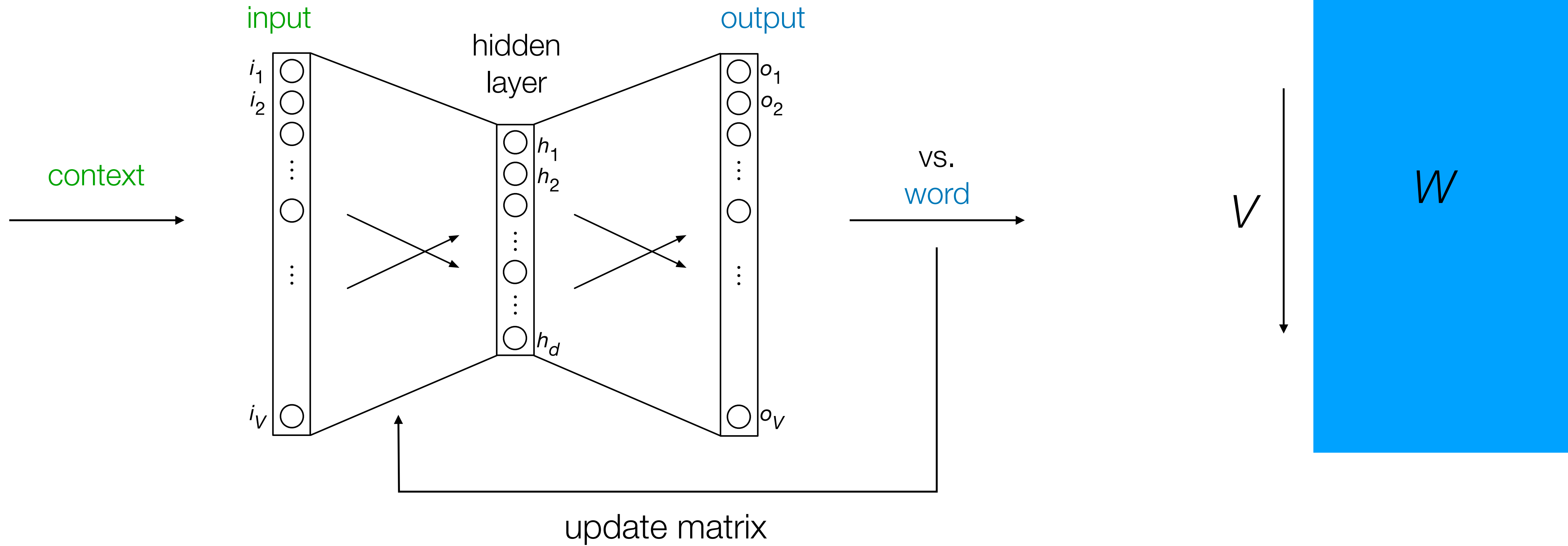
*Training data*



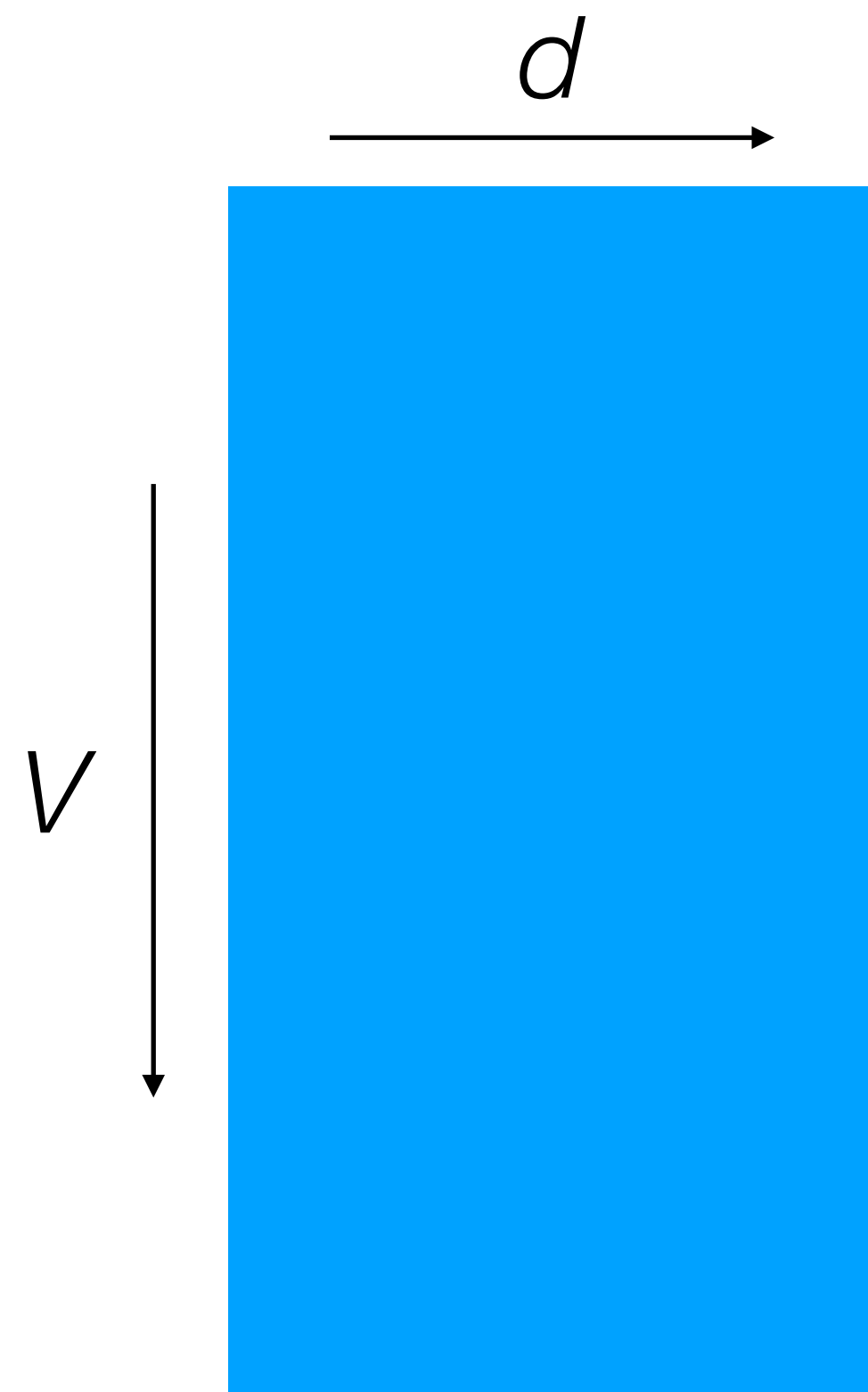
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*Training data*

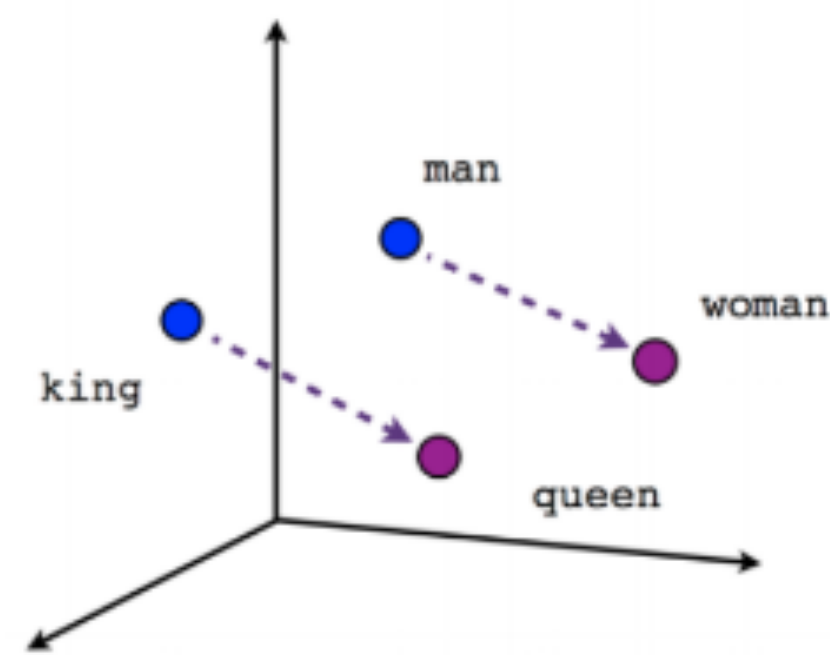




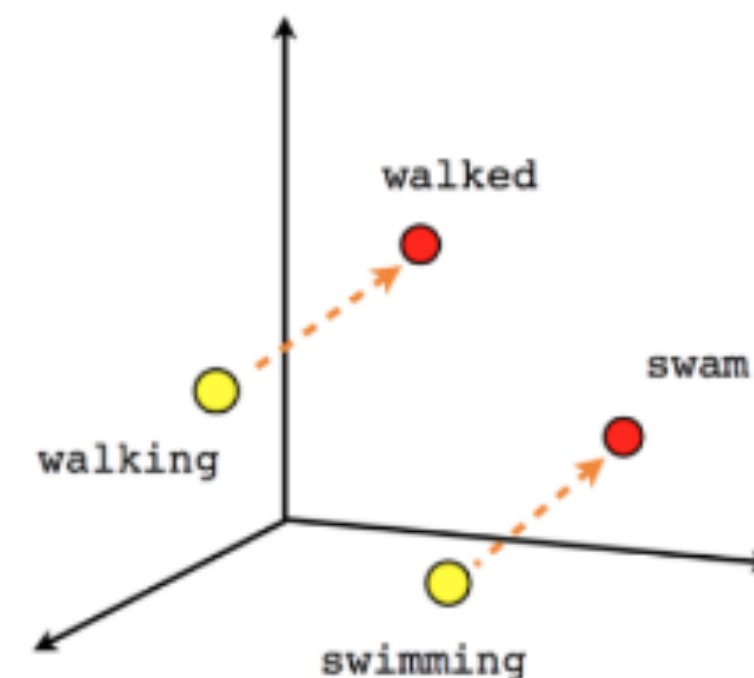


— Each row is an  $d$ -dimensional *word vector*

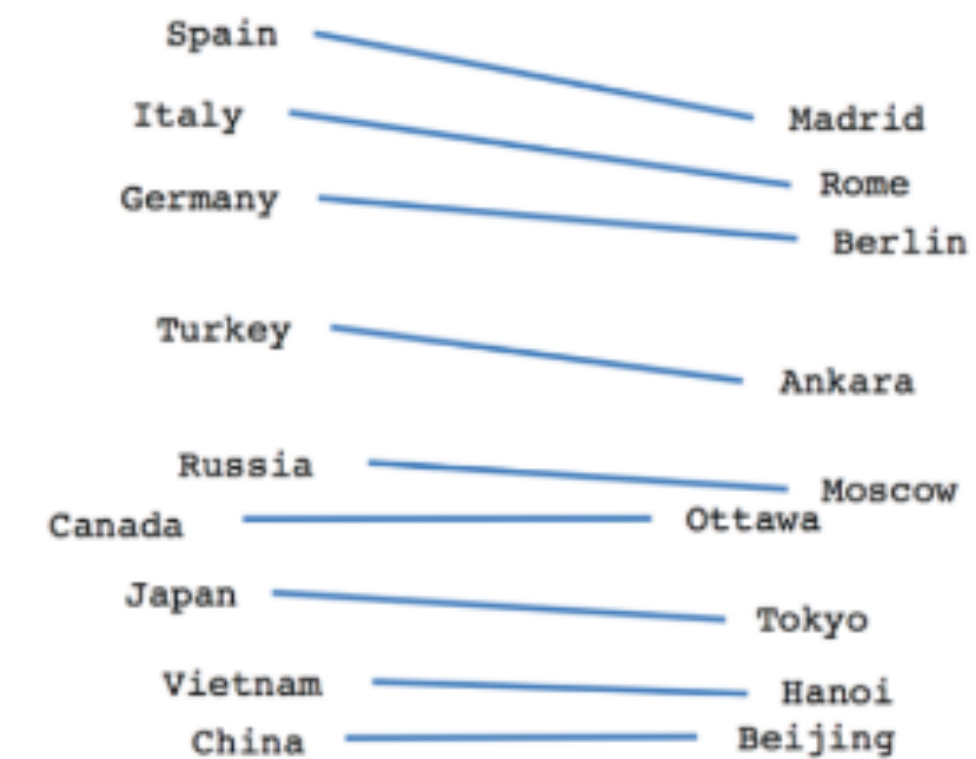
vectors encode semantics



Male-Female



Verb tense



Country-Capital

If this sounds like SVD,  
you're not crazy....

$$M \sim \log \frac{P(w, c)}{P(w)P(c)}$$

$$M = U\Sigma V^T$$

$$M \approx M_d = U_d \Sigma_d V_d^T$$

$$W^{\text{SVD}} = U_d \Sigma_d$$

---

## Neural Word Embedding as Implicit Matrix Factorization

---

**Omer Levy**  
Department of Computer Science  
Bar-Ilan University  
omerlevy@gmail.com

**Yoav Goldberg**  
Department of Computer Science  
Bar-Ilan University  
yoav.goldberg@gmail.com

Neural network implicitly performs  
*weighted* factorization of  $M$

Embedding words in vector spaces  
has taken the world by storm

Google Scholar

Distributed **representations of words** and phrases  
[T Mikolov](#), [I Sutskever](#), [K Chen](#), [GS Corrado](#)... - Advances in neural

The recently introduced continuous Skip-gram model is an efficient method for learning high quality distributed vector representations that capture a large number of semantic word relationships. In this paper we present several improvements to the model.

☆  Cited by 24838 Related articles All 32 versions Import

word vectors, sentence vectors, *thought*  
vectors...

Lots of natural language processing **applications**  
including **semantic similarity**:

$$S(s_i, s_j) = \frac{\mathbf{v}_i \cdot \mathbf{v}_j}{\|\mathbf{v}_i\| \|\mathbf{v}_j\|}$$

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☆  Cited by 24838 Related articles All 32 versions Import

word vectors, sentence vectors, *thought* vectors...

Lots of natural language processing **applications** including **semantic similarity**:

$$S(s_i, s_j) = \frac{\mathbf{v}_i \cdot \mathbf{v}_j}{\|\mathbf{v}_i\| \|\mathbf{v}_j\|}$$

Must be approached with **caution**

## Semantics derived automatically from language corpora contain human-like biases

Aylin Caliskan,<sup>1\*</sup> Joanna J. Bryson,<sup>1,2\*</sup> Arvind Narayanan<sup>1\*</sup>

"[...] word vectors contain stereotypes matching those documented with the [Implicit Association Test]"

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## ConceptNet Numberbatch

### ConceptNet at SemEval-2017 Task 2: Extending Word Embeddings with Multilingual Relational Knowledge

Robyn Speer

Joanna Lowry-Duda

### Neural language representations predict outcomes of scientific research

James P. Bagrow<sup>1,2,\*</sup>, Daniel Berenberg<sup>3,2</sup>, and Joshua Bongard<sup>3,2</sup>

<sup>1</sup>Department of Mathematics & Statistics, University of Vermont, Burlington, VT, United States

<sup>2</sup>Vermont Complex Systems Center, University of Vermont, Burlington, VT, United States

<sup>3</sup>Department of Computer Science, University of Vermont, Burlington, VT, United States

\*Corresponding author. Email: [james.bagrow@uvm.edu](mailto:james.bagrow@uvm.edu), Homepage: [bagrow.com](http://bagrow.com)

May 17, 2018

# Machine Learning for Networks

# DeepWalk: Online Learning of Social Representations

Bryan Perozzi  
Stony Brook University  
Department of Computer  
Science

Rami Al-Rfou  
Stony Brook University  
Department of Computer  
Science

Steven Skiena  
Stony Brook University  
Department of Computer  
Science

{bperozzi, ralrfou, skiena}@cs.stonybrook.edu

word embedding (word2vec):

... worlds are yours except **europa** attempt no landings there ...

# DeepWalk: Online Learning of Social Representations

Bryan Perozzi  
Stony Brook University  
Department of Computer  
Science

Rami Al-Rfou  
Stony Brook University  
Department of Computer  
Science

Steven Skiena  
Stony Brook University  
Department of Computer  
Science

{bperozzi, ralrfou, skiena}@cs.stonybrook.edu

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DeepWalk:

$[\dots, v_{i-2}, v_{i-1}, v_i, v_{i+1}, v_{i+2}, \dots]$

- Take a short **random walk** on the graph
- record the visited sequence of vertices
- treat vertices as words and do embedding!



# DeepWalk: Online Learning of Social Representations

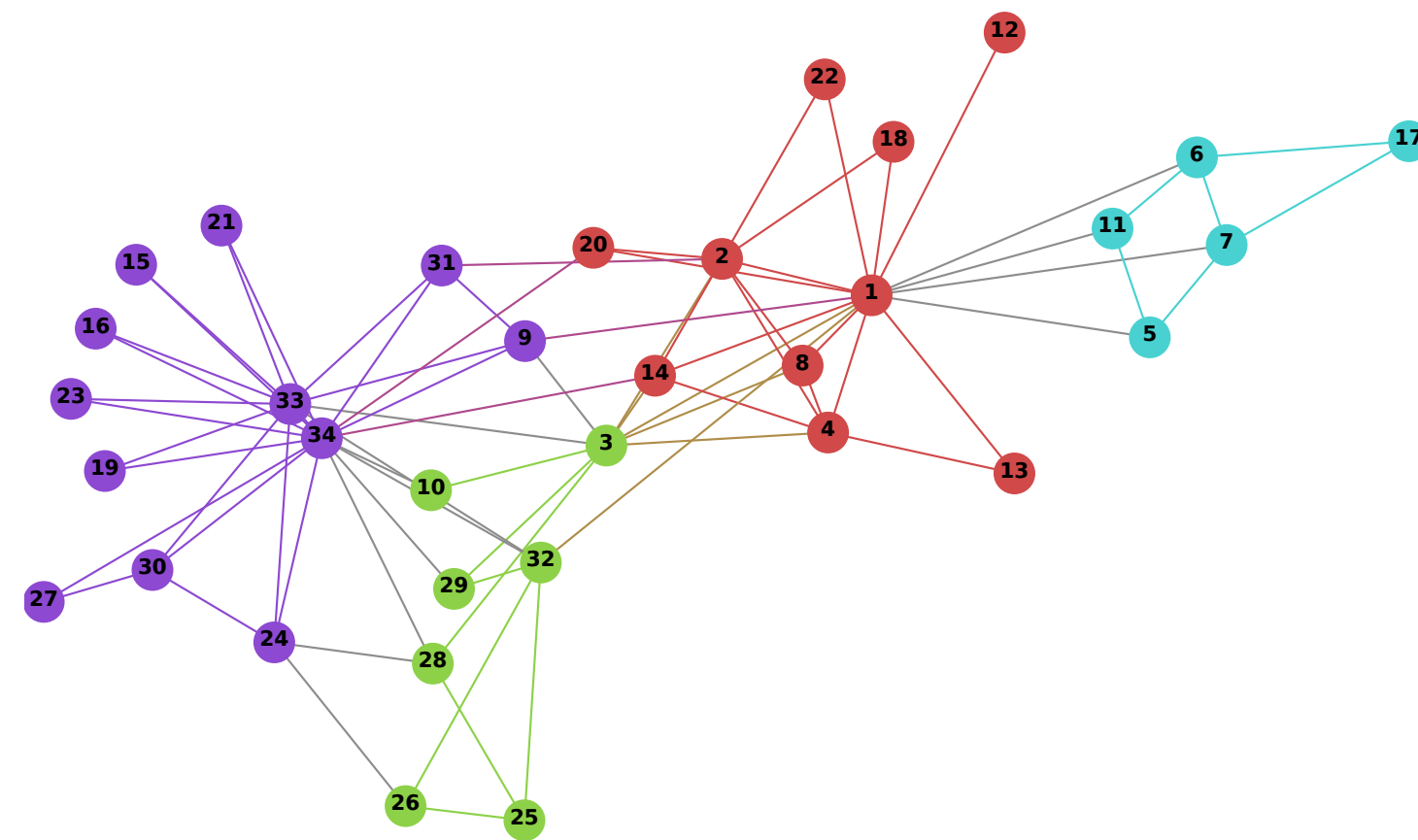
Bryan Perozzi  
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Science

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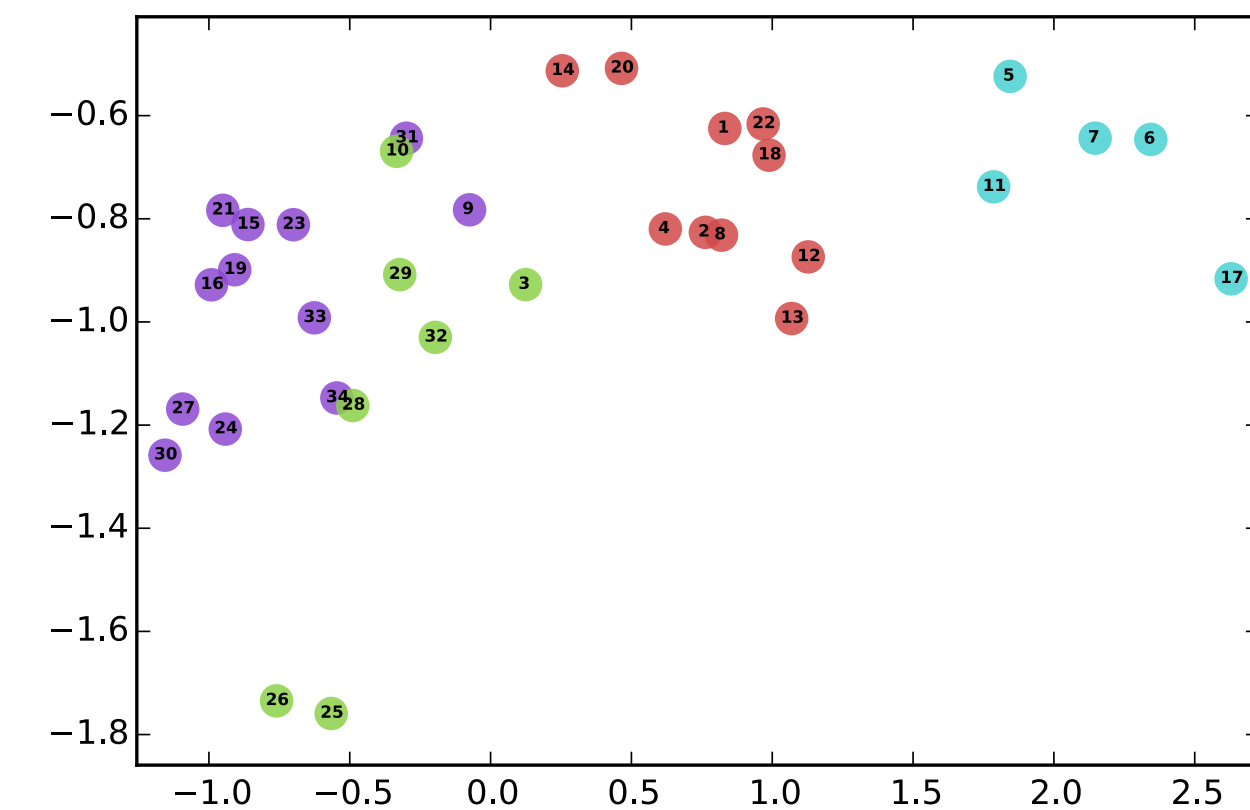
Steven Skiena  
Stony Brook University  
Department of Computer  
Science

{bperozzi, ralrfou, skiena}@cs.stonybrook.edu

DeepWalk:



(a) Input: Karate Graph



(b) Output: Representation

Is it also a **matrix factorization** problem? Yes!

## **Network Embedding as Matrix Factorization: Unifying DeepWalk, LINE, PTE, and node2vec**

Jiezhong Qiu<sup>†\*</sup>, Yuxiao Dong<sup>‡</sup>, Hao Ma<sup>‡</sup>, Jian Li<sup>#</sup>, Kuansan Wang<sup>‡</sup>, and Jie Tang<sup>†</sup>

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**Table 1: The matrices that are implicitly approximated and factorized by DeepWalk, LINE, PTE, and node2vec.**

Algorithm	Matrix
DeepWalk	$\log \left( \text{vol}(G) \left( \frac{1}{T} \sum_{r=1}^T (D^{-1}A)^r \right) D^{-1} \right) - \log b$
LINE	$\log \left( \text{vol}(G) D^{-1} A D^{-1} \right) - \log b$
PTE	$\log \left( \begin{bmatrix} \alpha \text{vol}(G_{ww})(D_{\text{row}}^{ww})^{-1} A_{ww} (D_{\text{col}}^{ww})^{-1} \\ \beta \text{vol}(G_{dw})(D_{\text{row}}^{dw})^{-1} A_{dw} (D_{\text{col}}^{dw})^{-1} \\ \gamma \text{vol}(G_{lw})(D_{\text{row}}^{lw})^{-1} A_{lw} (D_{\text{col}}^{lw})^{-1} \end{bmatrix} \right) - \log b$
node2vec	$\log \left( \frac{\frac{1}{2T} \sum_{r=1}^T \left( \sum_u X_{w,u} P_{c,w,u}^r + \sum_u X_{c,u} P_{w,c,u}^r \right)}{(\sum_u X_{w,u})(\sum_u X_{c,u})} \right) - \log b$

Notations in DeepWalk and LINE are introduced below. See detailed notations for PTE and node2vec.

— Many methods besides DeepWalk

Random walks are a fundamental concept when studying networks

## Random walks and diffusion on networks

Naoki Masuda<sup>a,\*</sup>, Mason A. Porter<sup>b,c,d</sup>, Renaud Lambiotte<sup>c</sup>

<sup>a</sup> Department of Engineering Mathematics, University of Bristol, Bristol, UK

<sup>b</sup> Department of Mathematics, University of California Los Angeles, Los Angeles, USA

<sup>c</sup> Mathematical Institute, University of Oxford, Oxford, UK

<sup>d</sup> CABDyN Complexity Centre, University of Oxford, Oxford, UK

ARTICLE INFO

ABSTRACT

5.	Applications.....	
5.1.	Search on networks.....	
5.2.	Ranking.....	
5.2.1.	PageRank.....	
5.2.2.	Laplacian centrality.....	
5.2.3.	TempoRank.....	
5.2.4.	Random-walk betweenness centrality.....	
5.2.5.	Discrete-choice models.....	
5.3.	Community detection.....	
5.3.1.	Markov-stability formulation of modularity.....	
5.3.2.	Walktrap.....	
5.3.3.	InfoMap.....	
5.3.4.	Local community detection.....	
5.3.5.	Multilayer modularity.....	
5.4.	Core-periphery structure.....	
5.5.	Diffusion maps.....	
5.6.	Respondent-driven sampling.....	
5.7.	Consensus probability and time of voter models.....	
5.8.	DeGroot model.....	

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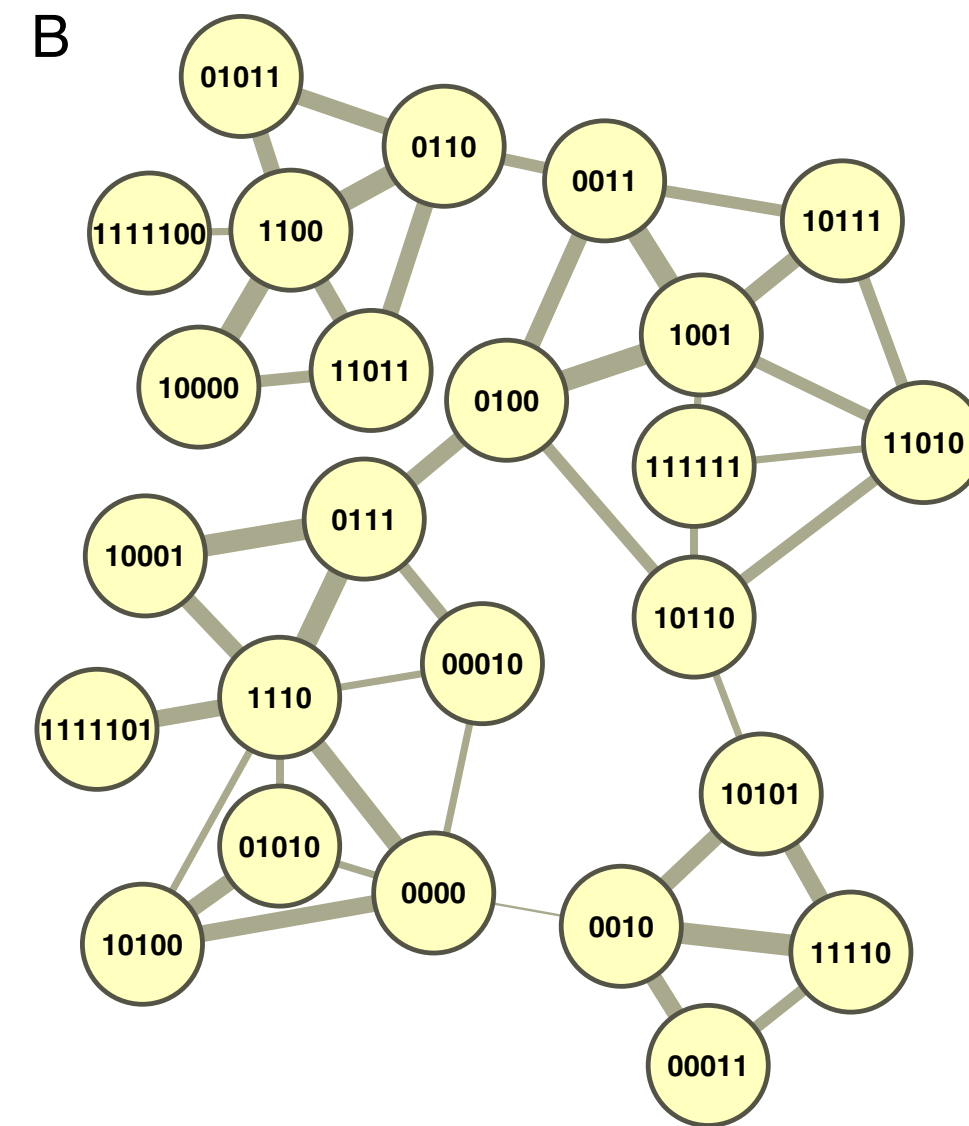
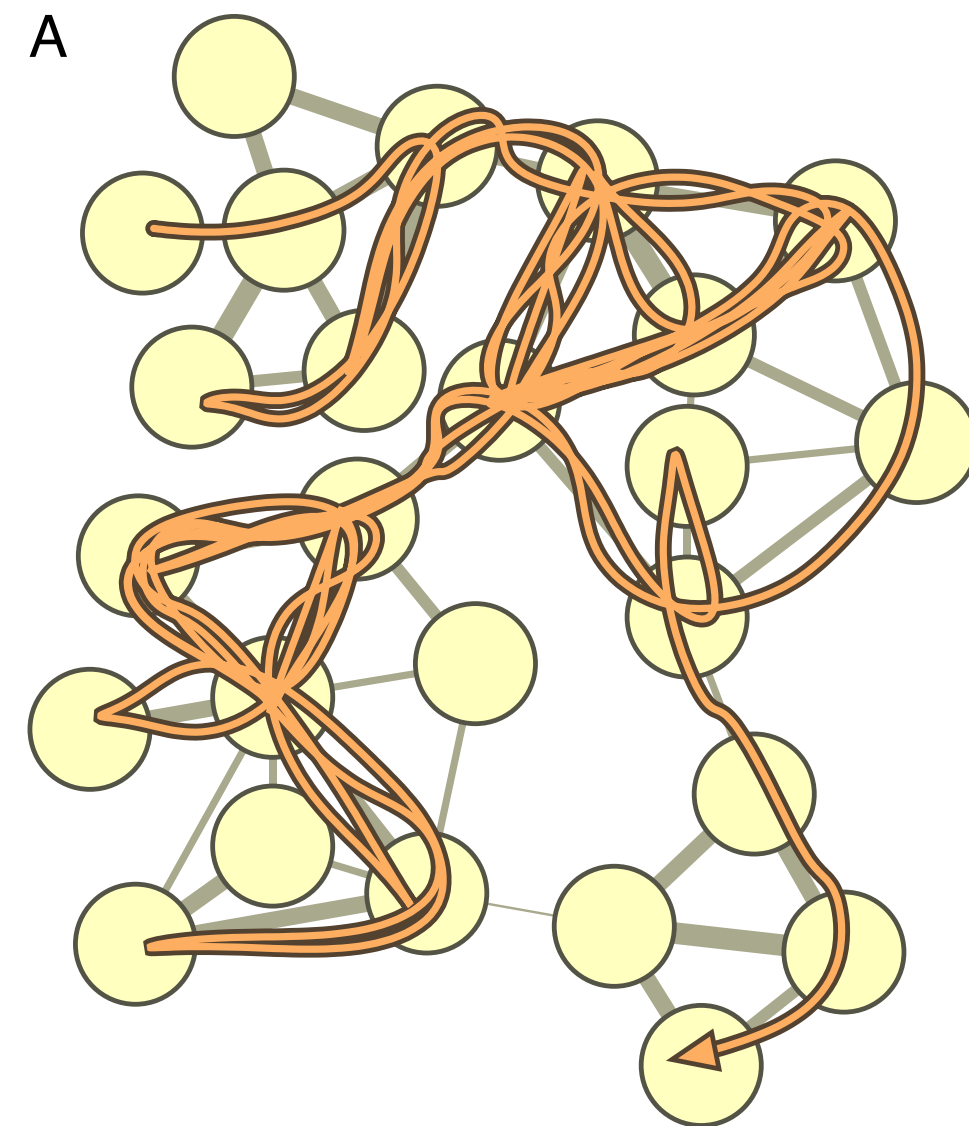
## Maps of random walks on complex networks reveal community structure

Martin Rosvall\*<sup>†</sup> and Carl T. Bergstrom\*<sup>‡</sup>

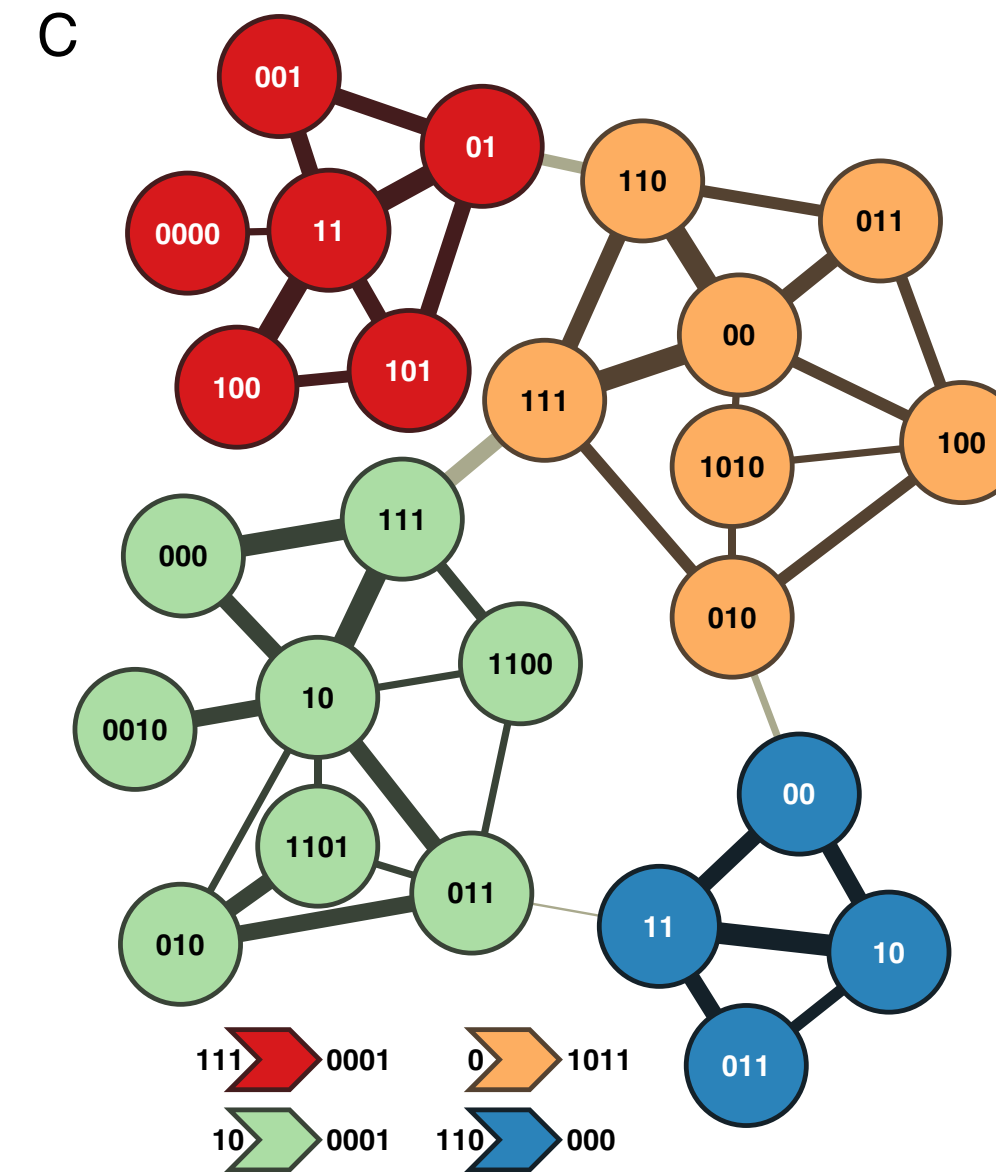
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# Maps of random walks on complex networks reveal community structure

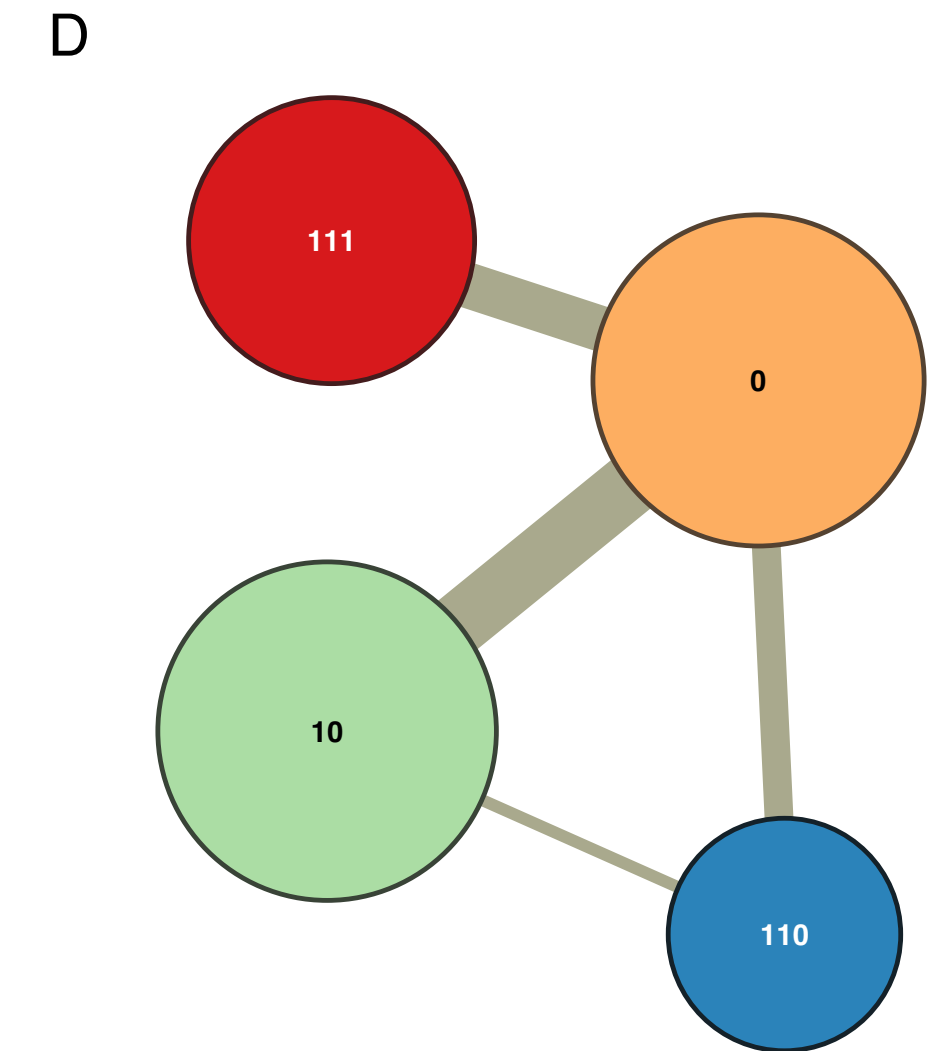
Martin Rosvall\*† and Carl T. Bergstrom\*\*‡



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111 0000 11 01 101 100 101 01 0001 0 110 011 00 110 00 111 1011 10  
 111 000 10 111 000 111 10 011 10 000 111 10 111 10 0010 10 011 010  
 011 10 000 111 0001 0 111 010 100 011 00 111 00 011 00 111 00 111  
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 10 111 000 10 000 111 0001 0 111 010 1010 010 1011 110 00 10 011



111 0000 11 01 101 100 101 01 0001 0 110 011 00 110 00 111 1011 10  
 111 000 10 111 000 111 10 011 10 000 111 10 111 10 0010 10 011 010  
 011 10 000 111 0001 0 111 010 100 011 00 111 00 011 00 111 00 111  
 110 111 110 1011 111 01 101 01 0001 0 110 111 00 011 110 111 1011  
 10 111 000 10 000 111 0001 0 111 010 1010 010 1011 110 00 10 011

# Graph neural networks

Recall:

Node attribute list

Alice	x11	x12
Bob	x21	x22
Carol	x31	x32
⋮	⋮	⋮

$p$  features  
(attributes)

Supervised learning

$$y = f(X)$$

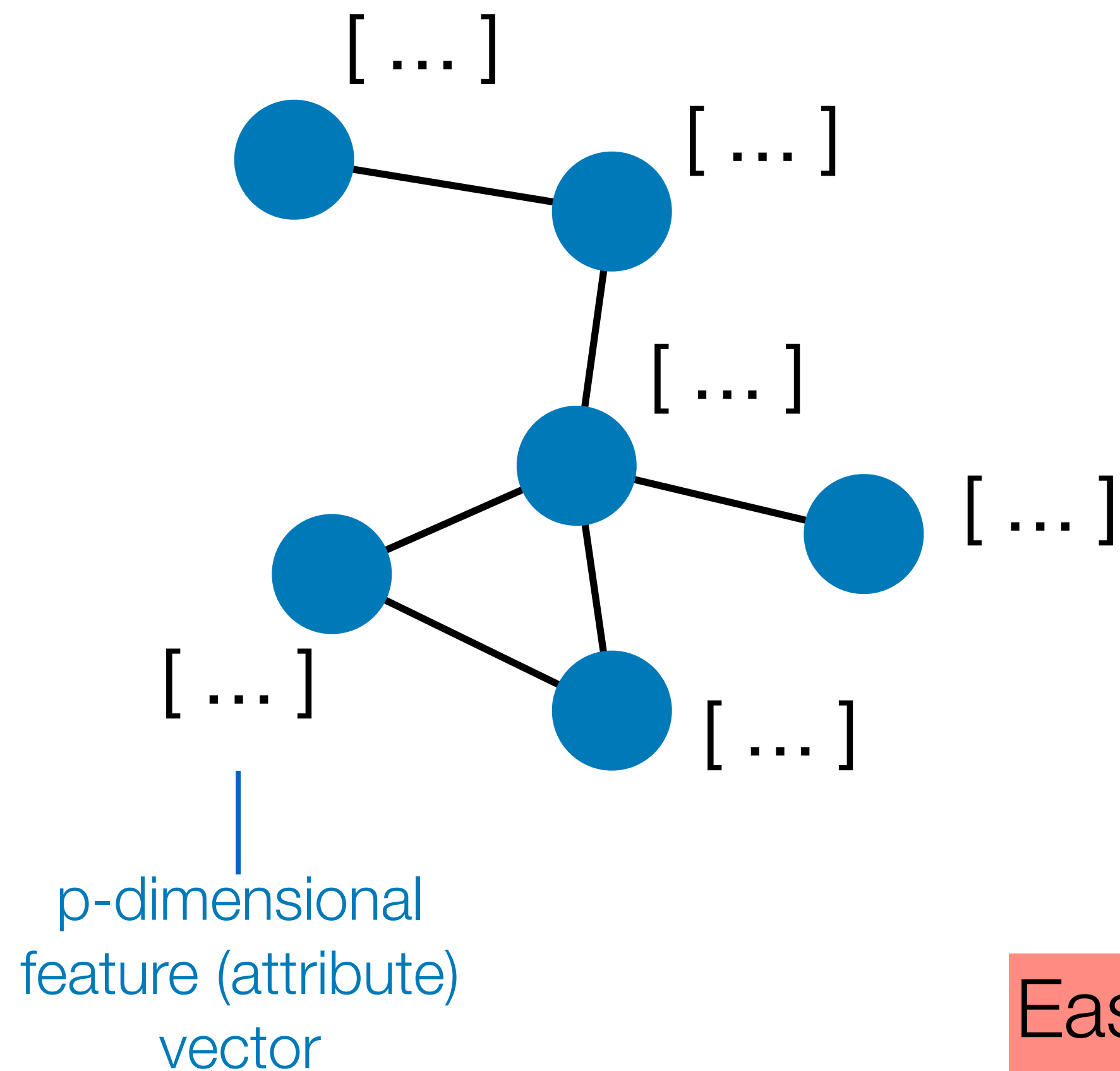
$N \times p$  matrix of features or predictors  
each row is an observation, each  
column is a feature

# Graph neural networks

Supervised learning

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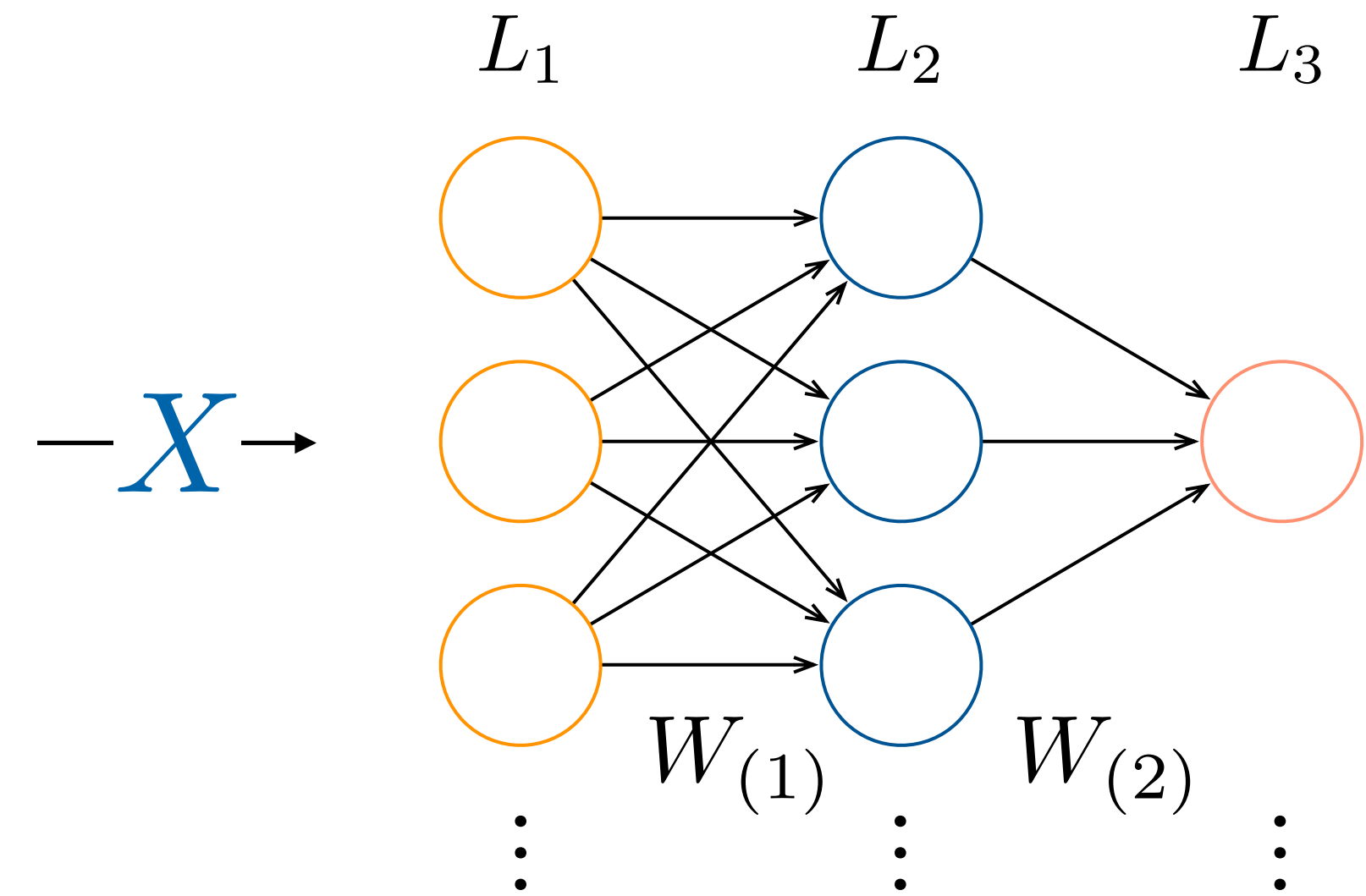


Easy enough when observations are **independent**  
How to incorporate the network?



# neural networks

Idea: propagate **your data** through the neural network

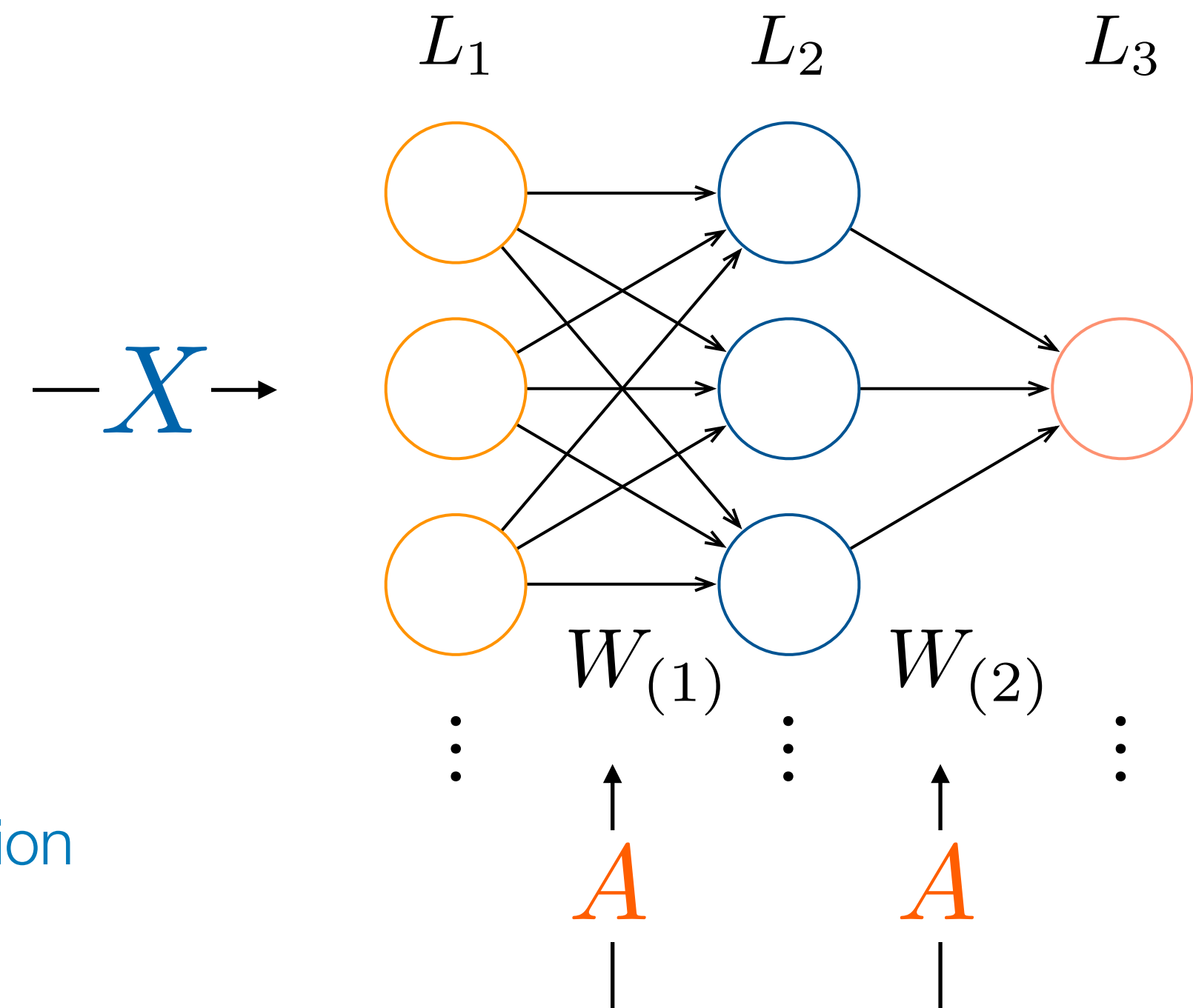


$$H_{(0)} = X$$

NN:  $H_{(\ell+1)} = \sigma (H_{(\ell)} W_{(\ell)})$        $\sigma$  — activation function

# Graph neural networks

Idea: propagate **your data** through the neural network, but **hit it with the graph** at each layer



$$H_{(0)} = X$$

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GNN:  $H_{(\ell+1)} = \sigma(\tilde{A}H_{(\ell)}W_{(\ell)})$       $\tilde{A}$  — preprocessed adjacency matrix

↑

# Graph neural networks

Idea: propagate *your data* through the neural network, but *hit it with the graph* at each layer


## Applications

- classifying nodes
- predicting links
- comparing networks

$$H_{(0)} = X$$

NN:  $H_{(\ell+1)} = \sigma \left( H_{(\ell)} W_{(\ell)} \right)$       $\sigma$  — activation function

GNN:  $H_{(\ell+1)} = \sigma \left( \tilde{A} H_{(\ell)} W_{(\ell)} \right)$       $\tilde{A}$  — *preprocessed adjacency matrix*



Designing visualizations

# Visualization $\subset$ Communication

Visualizations are one tool to tackle the larger problem of communicating your results

# Designing visualizations

Which kind of door handle is better?



# Designing visualizations

Which kind of door handle is better?



Better? Easier to open!

# Designing visualizations

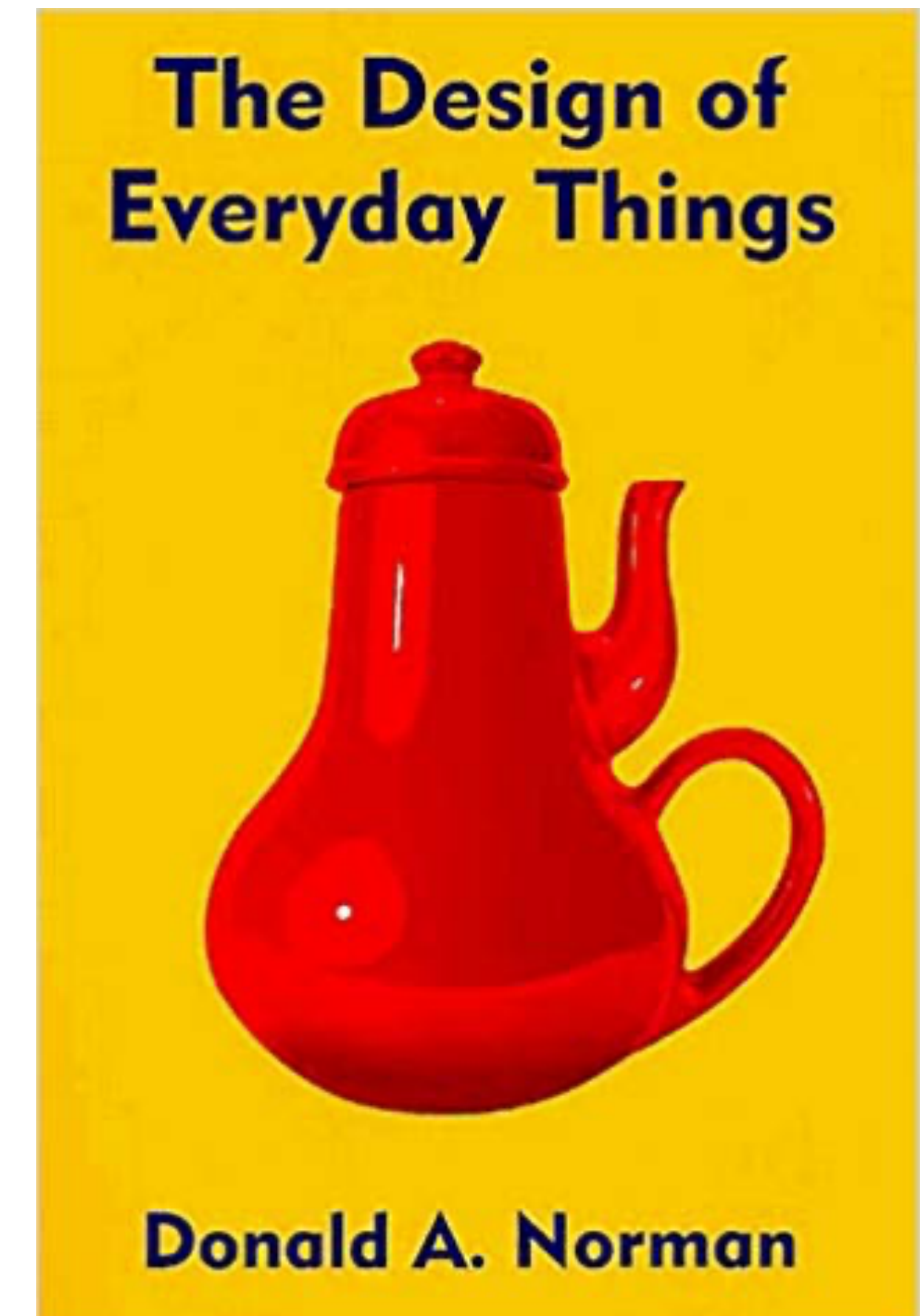
"Design is how it works"  
–Steve Jobs





# Designing visualizations

"Design is how it works"  
–Steve Jobs



# Designing visualizations

Which kind of door handle is better?



Better? Easier to open!

**Visualizations: better = easier to understand**

# Designing visualizations

- Know your message
- Know your medium
- Know your audience
- Account for strengths and weaknesses of human perception
- Keep it simple

# Great info: series of articles published in Nature Methods during 2010-2015 called "Points of View"

**POINTS OF VIEW**

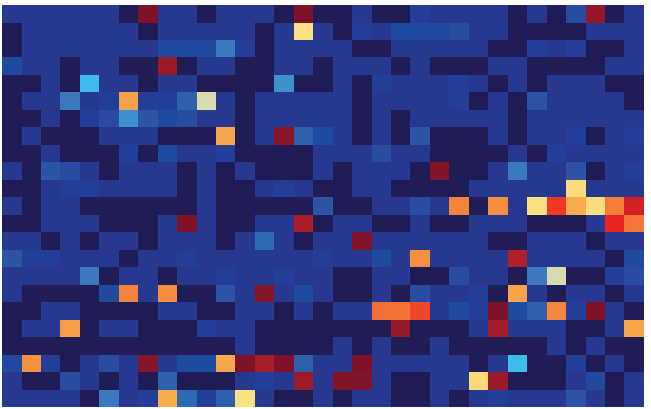
## Saliency to relevance

In science communication, it is critical that visual information be interpreted efficiently and correctly. The discordance between components of an image that are most noticeable and those that are most relevant or important can compromise the effectiveness of a presentation. This discrepancy can cause viewers to mistakenly pay attention to regions of the image that are not relevant. Ultimately, the misdirected attention can negatively impact comprehension.

Saliency is the physical property that sets an object apart from its surroundings. It is particularly important to ensure that saliency aligns with relevance in visuals used for slide presentations. In these situations, information transmission needs to be efficient because the audience member is expected to simultaneously listen and read.

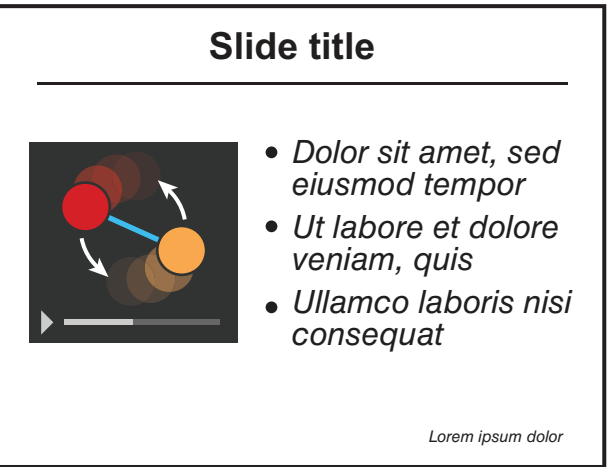
**THIS MONTH**

**a**



Low High

**b**



- *Dolor sit amet, sed eiusmod tempor*
- *Ut labore et dolore veniam, quis*
- *Ullamco laboris nisi consequat*

Lorem ipsum dolor

**Figure 2** | Discordances between saliency and relevance can be harmful. (a) The relative visibility of hues in the color scale is asymmetric, making higher values (represented by deep red) less apparent. (b) Continuously moving images can be distracting and can compromise the viewer's ability to concentrate on other content.

In contrast, unintentional and inadvertent assignment of saliency can be harmful to the communicative potential of images. In the same

# The challenge

Six months of work

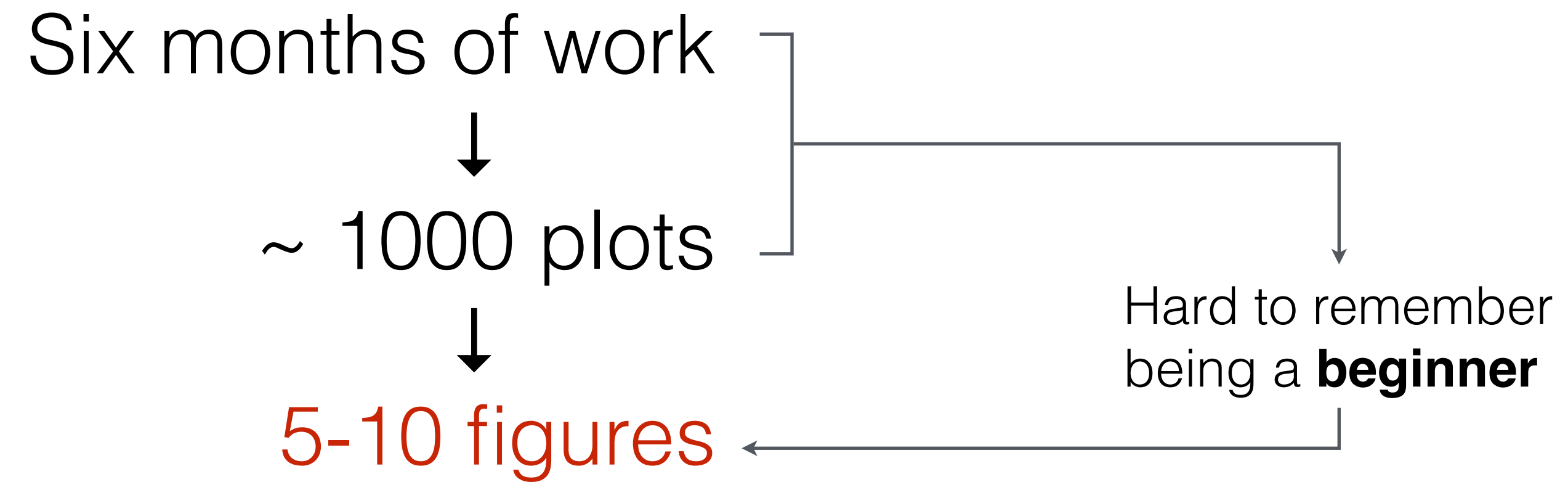


~ 1000 plots



5-10 figures

# The challenge



# Know your message

A figure/visualization has a **goal**: what do you want the reader to learn?

# Know your message

A figure/visualization has a **goal**: what do you want the reader to learn?

Summary sentence:

“Cancer deaths are down, but mostly due to decreased smoking rates.”

“Algorithm B converges faster than A.”

“Bats spread Ebola, not rodents.”

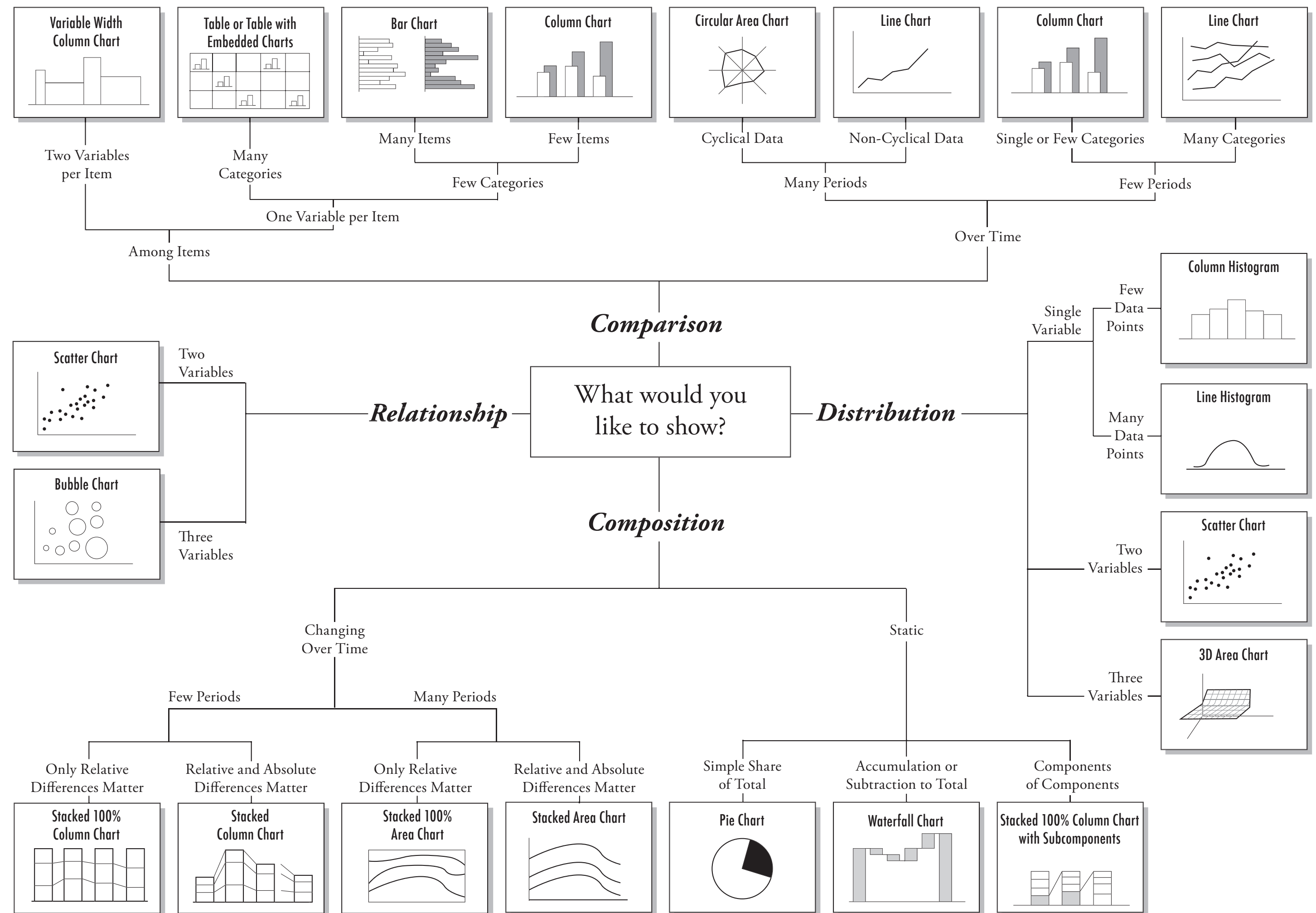
“The rate of text messages increased after approximately day 45.”

Build your figure(s) with this goal in mind.



Use your **summary sentence** to **guide** the kind of visualization(s) you use

## Chart Suggestions—A Thought-Starter

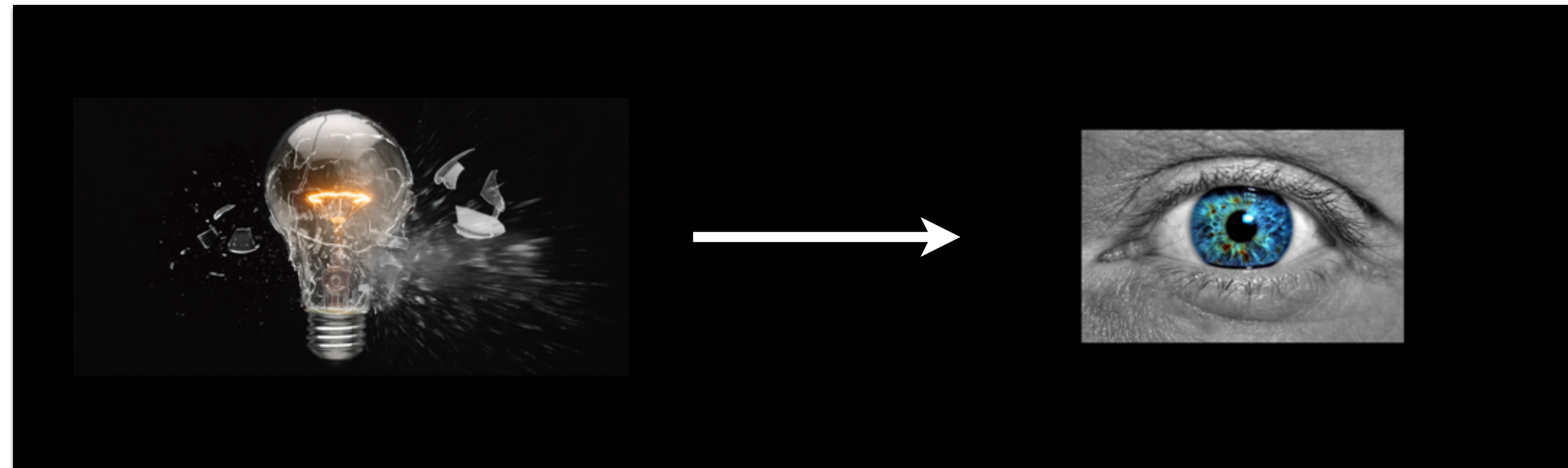


<http://extremepresentation.com>

Zelazny, Say it with Charts, 2001

# Know your medium

Print? Web? Slides?



# Know your audience



# Human perception

Parsing a figure or visualization requires performing **visual tasks**

Humans are **better at some tasks** and **worse at others**

## Aspect to compare

**easiest**

Positions on a common scale

Positions on the same but nonaligned scales

Lengths

Angles, slopes

Area

Volume, color saturation

**hardest**

Color hue

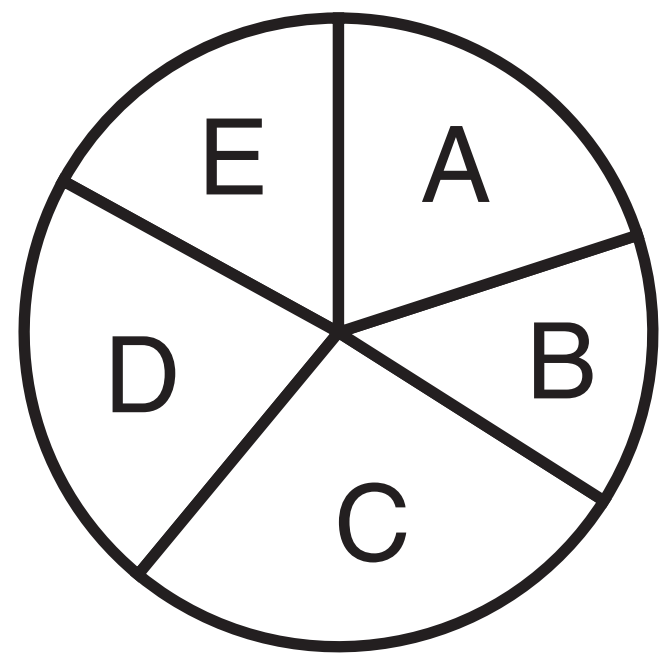
## Graphical Perception and Graphical Methods for Analyzing Scientific Data

William S. Cleveland and Robert McGill

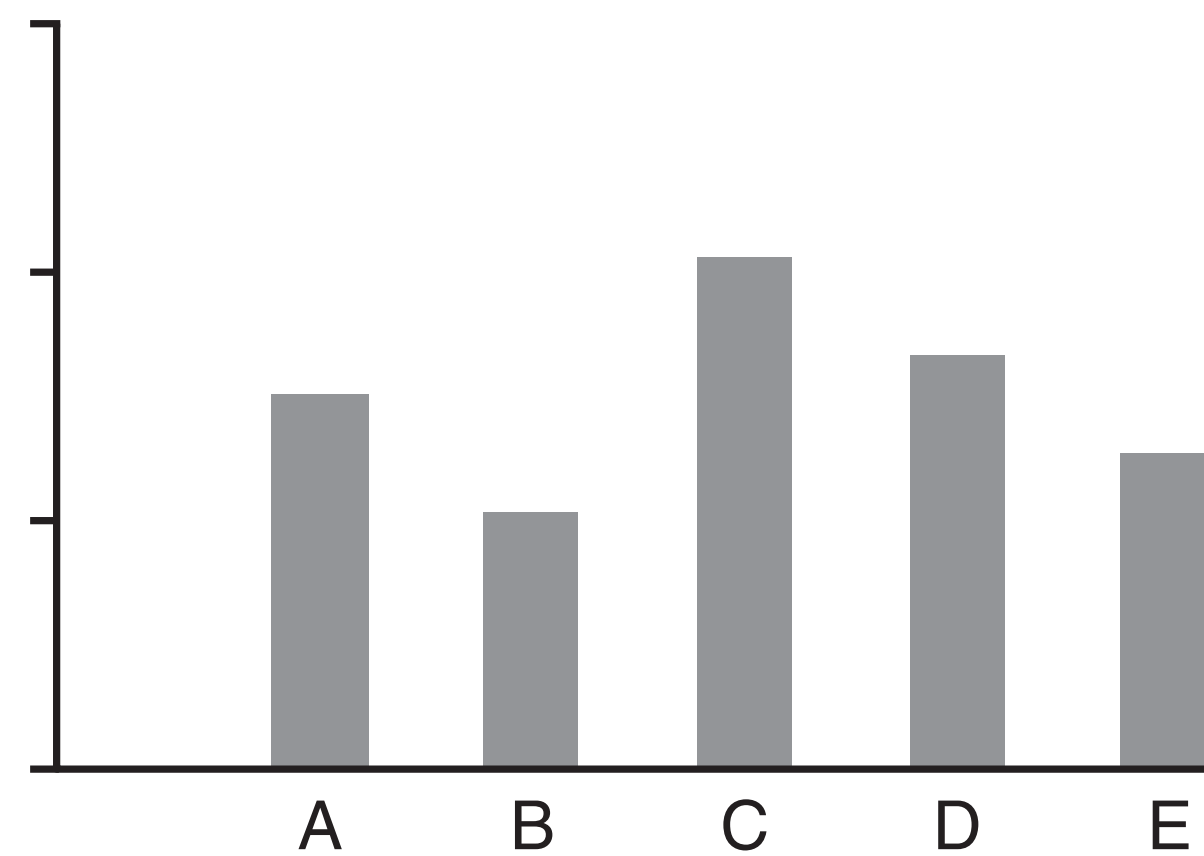
Science (1985)

# Human perception

Example: Comparing areas vs. lengths

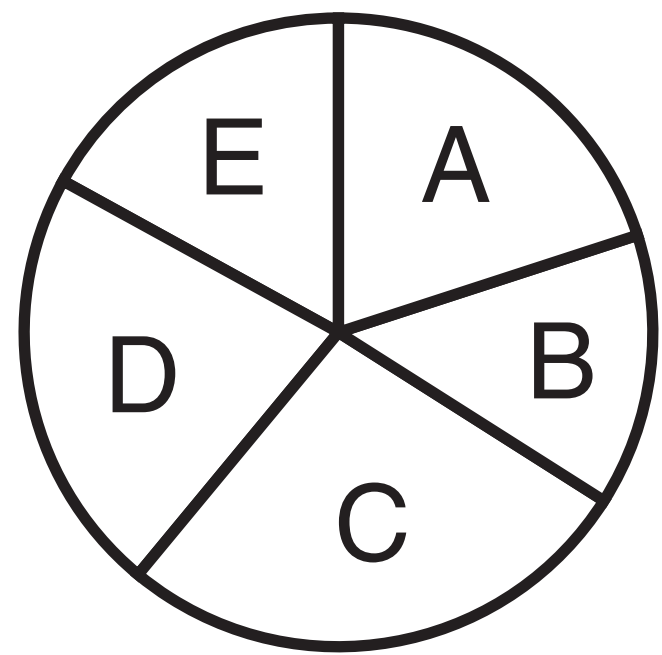


vs.

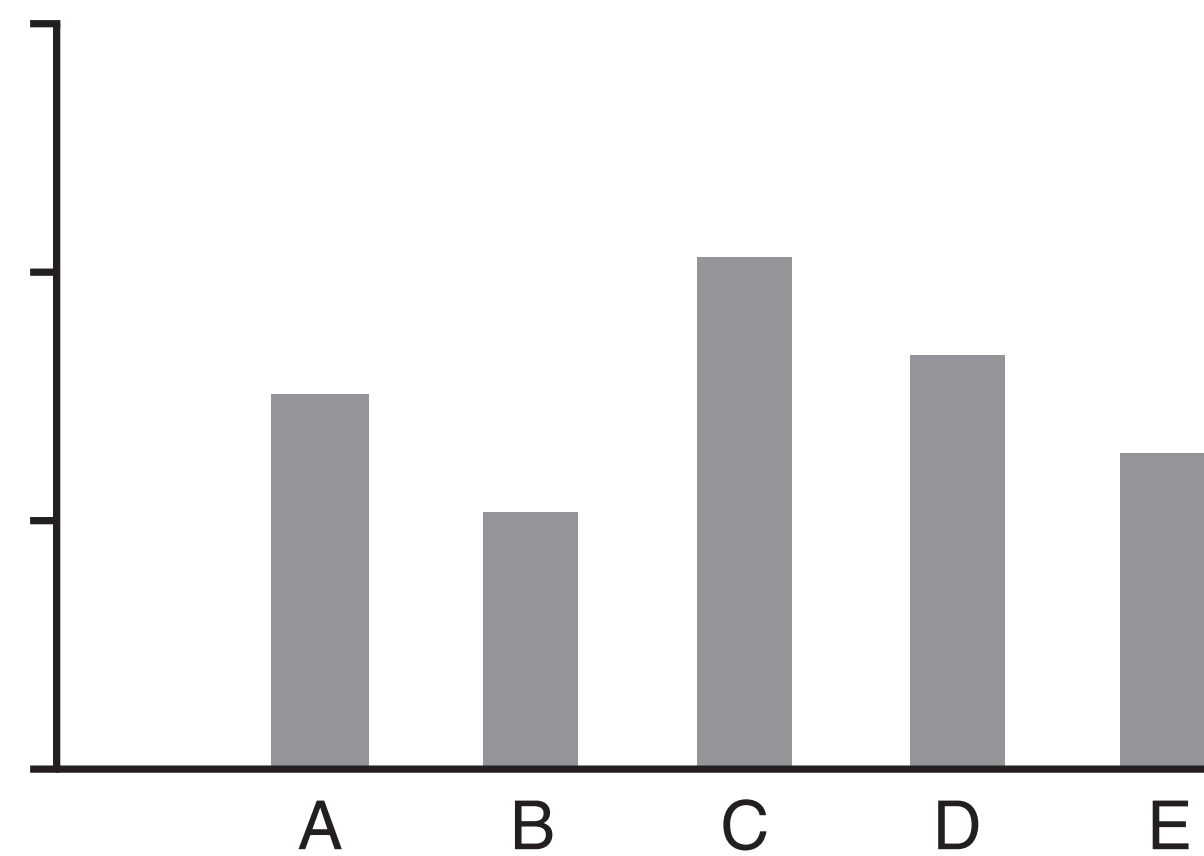


# Human perception

Example: Comparing areas vs. lengths



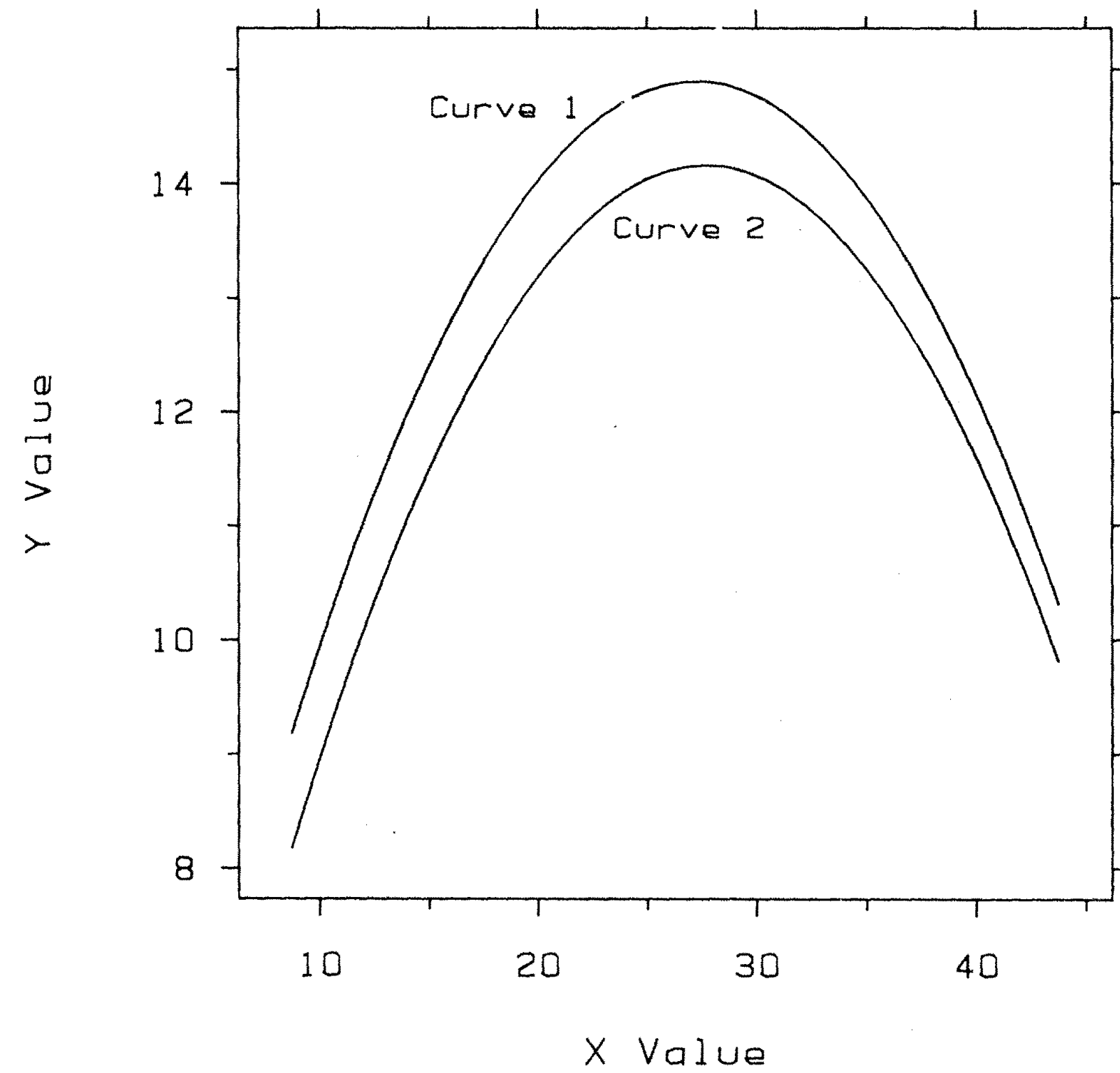
vs.



*Avoid Pie Charts!*

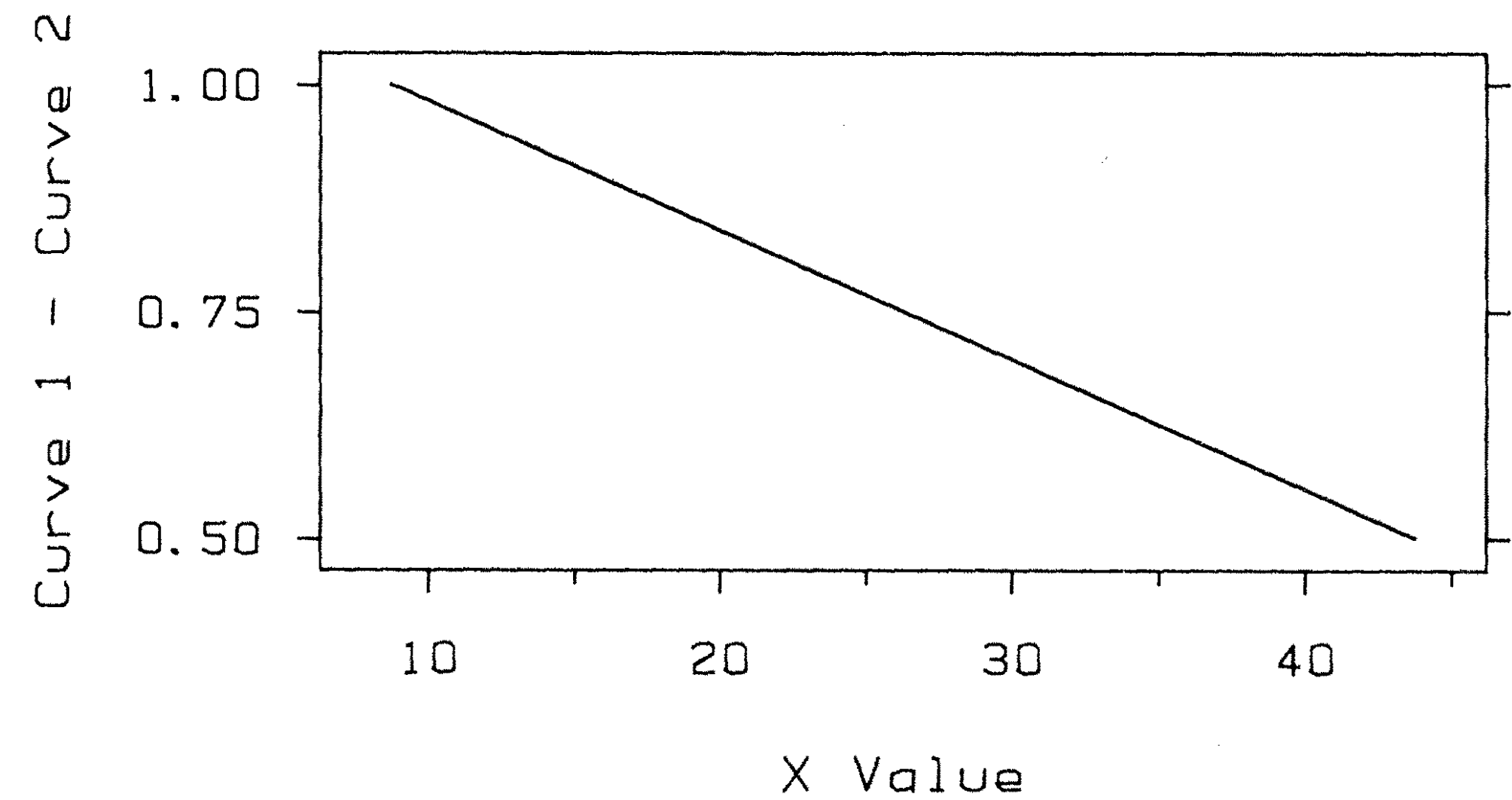
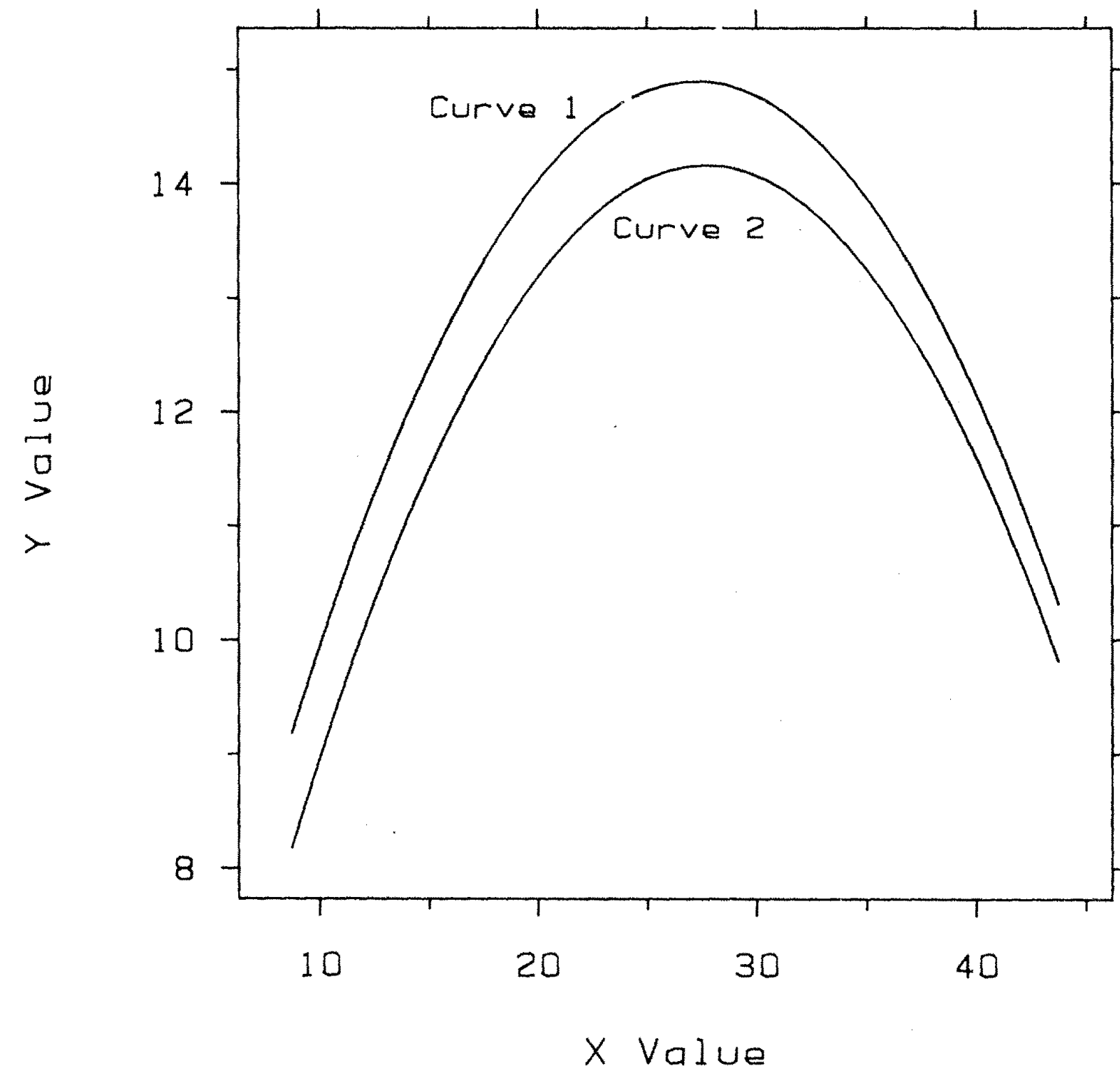
# Human perception

Perceptual biases plague even basic graphics



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Perceptual biases plague even basic graphics



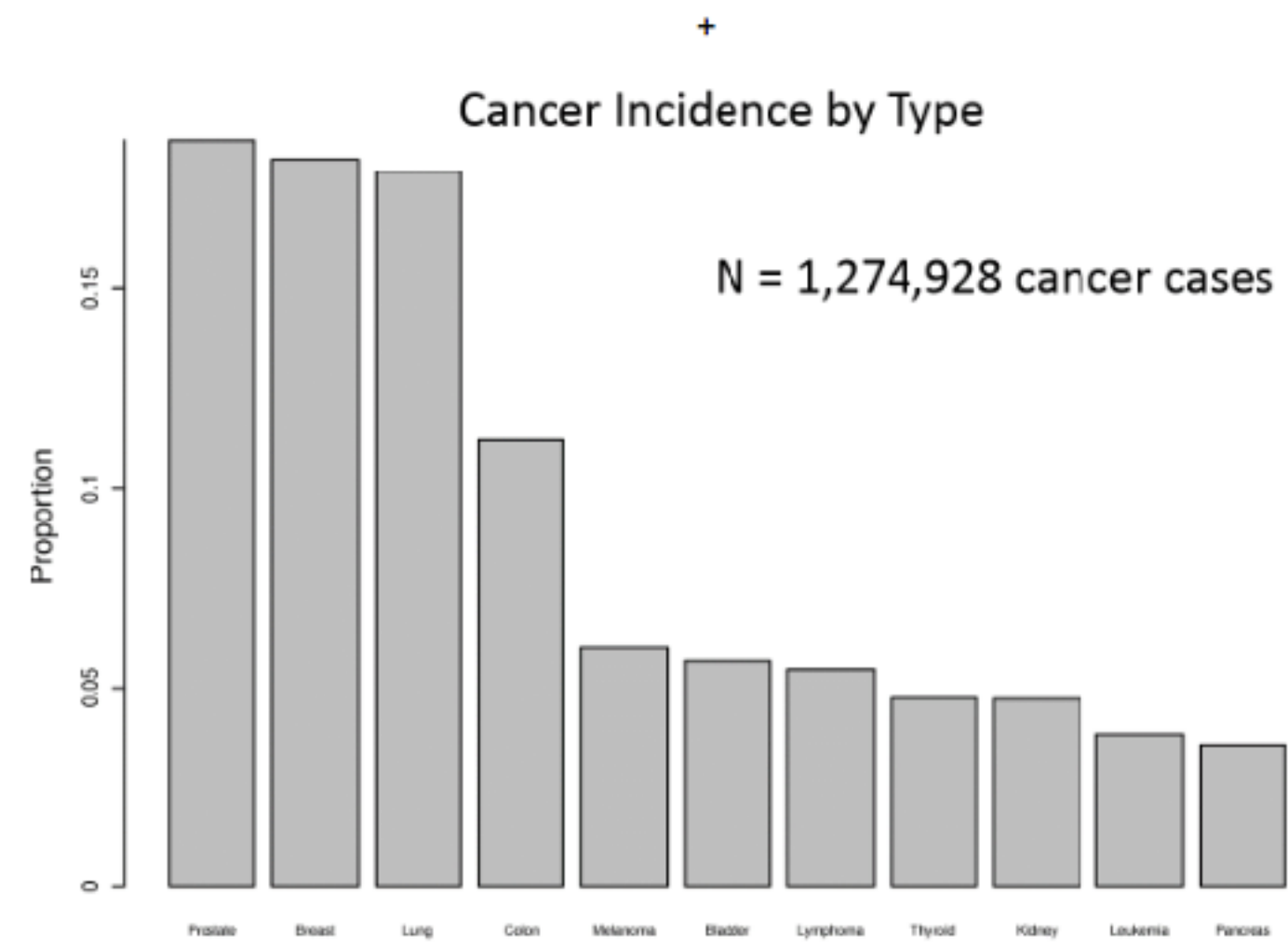


# Getting it right takes time

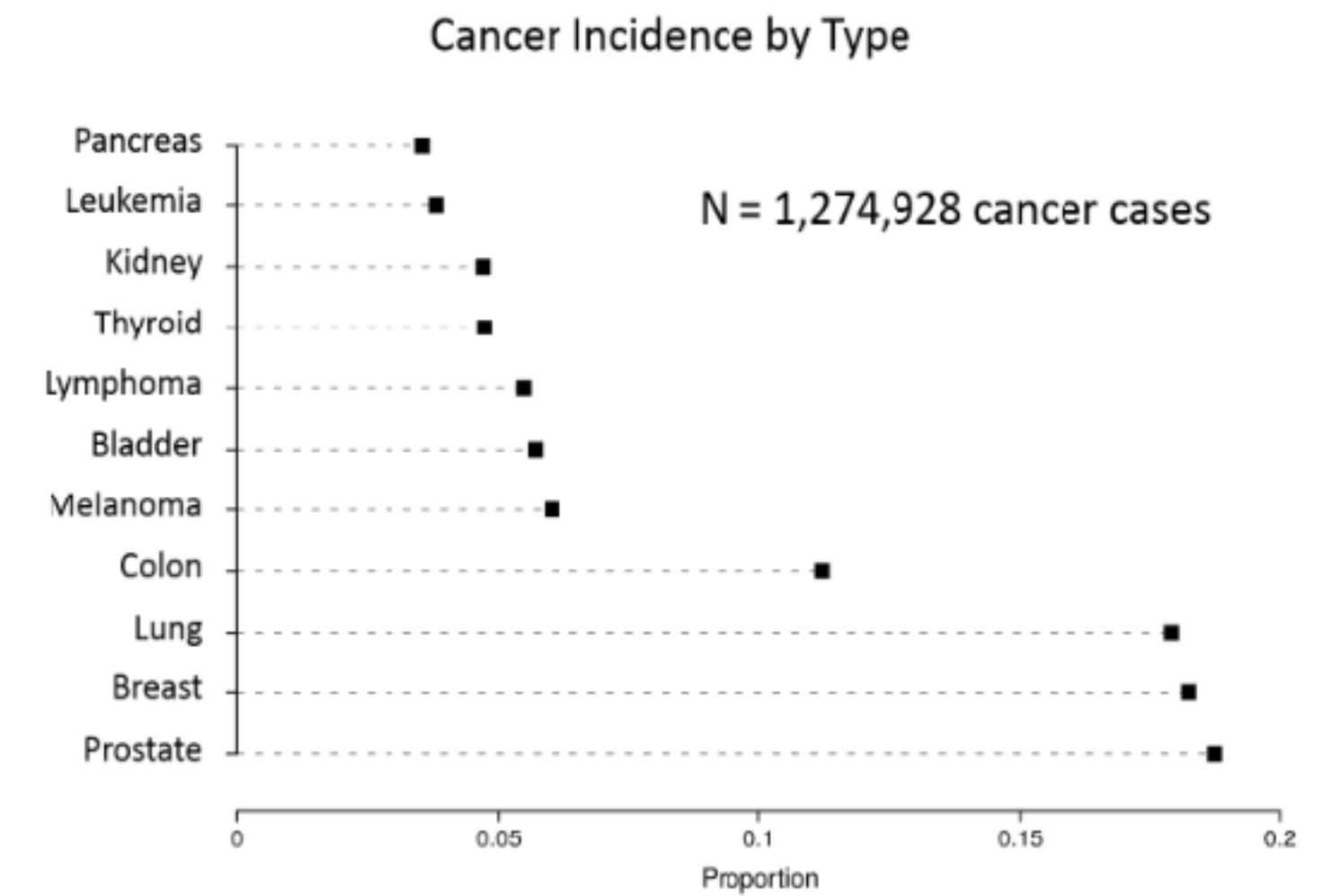
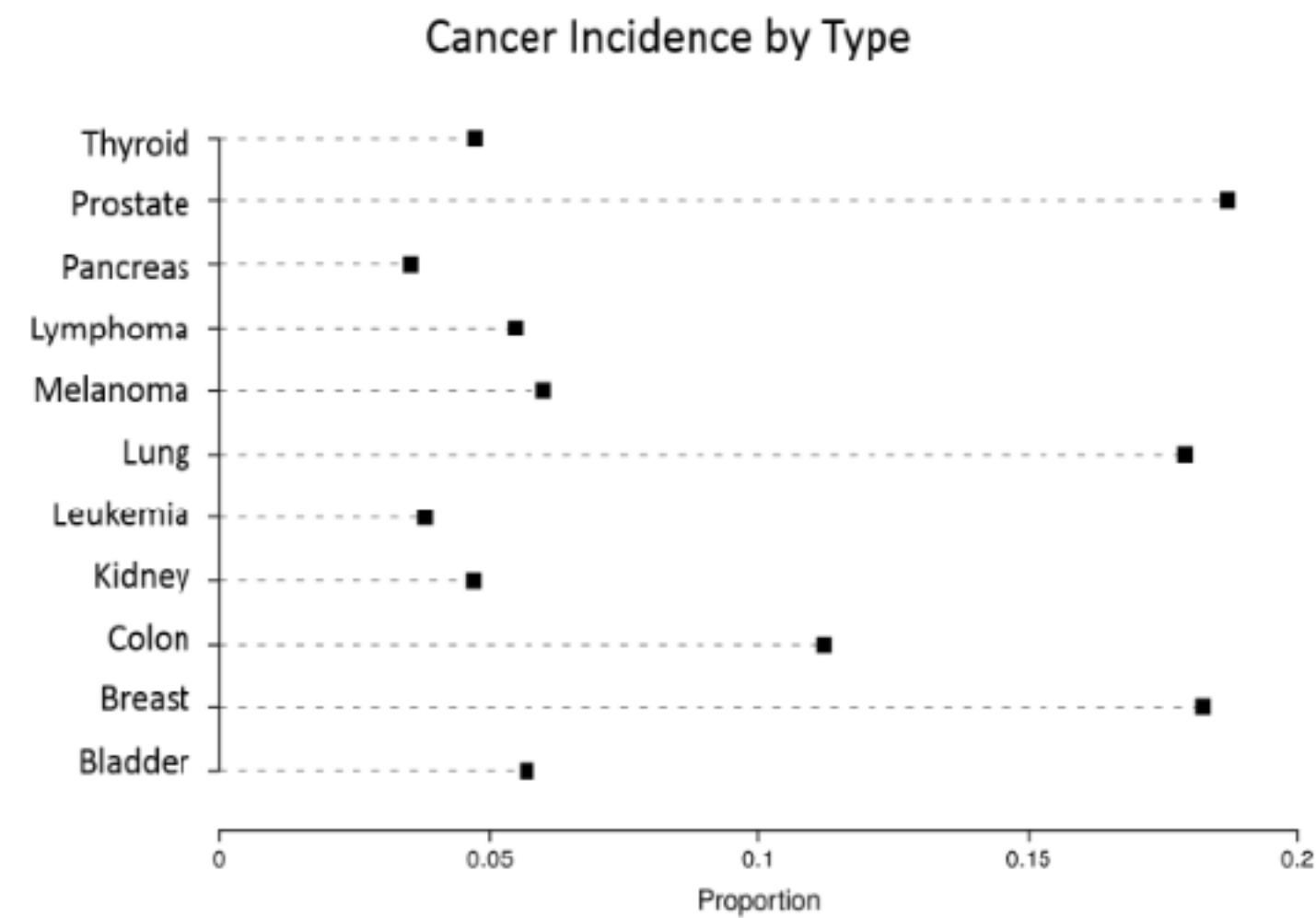
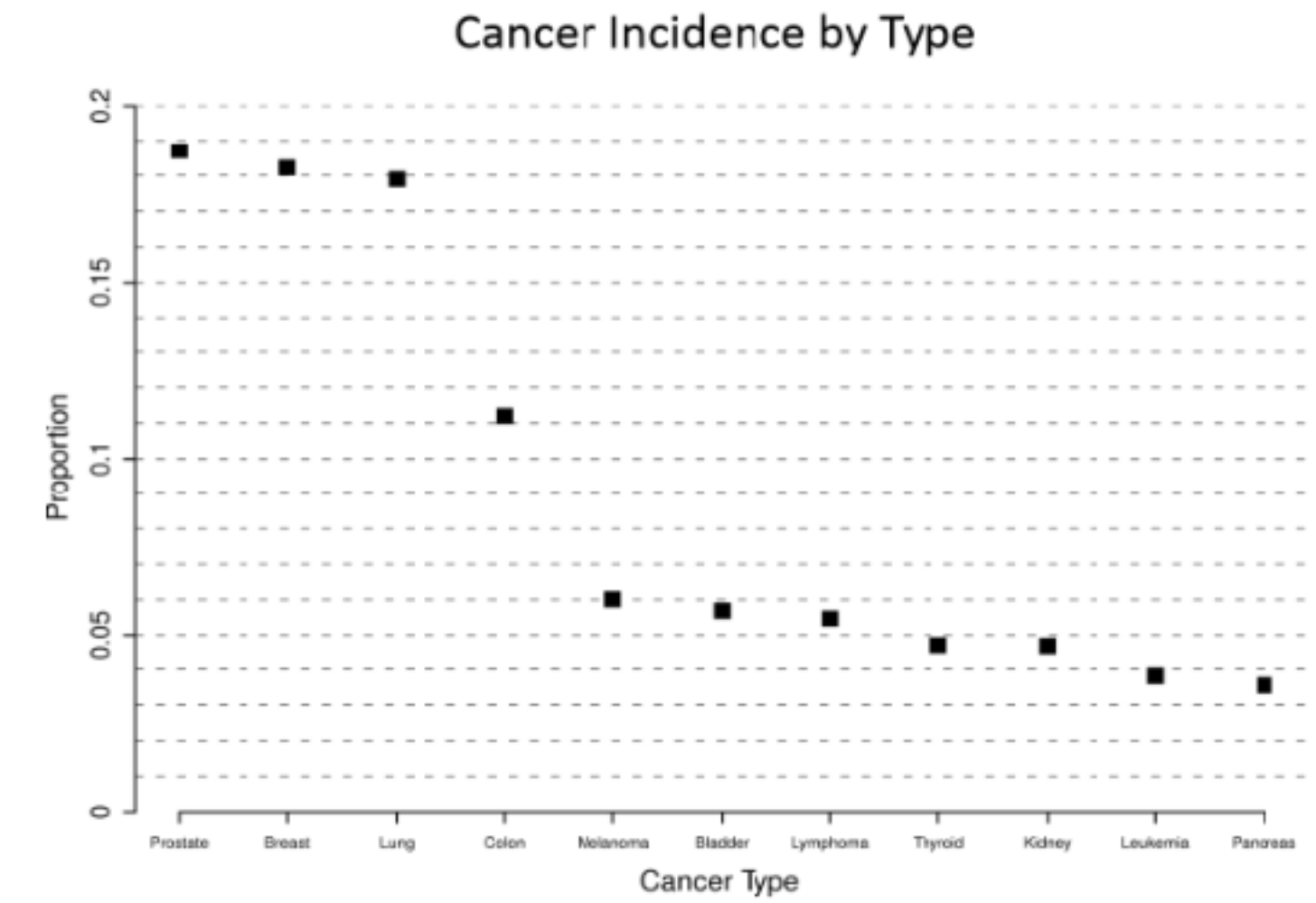
**Iterate!**

Readability is the most important goal!

Ver. 1



Ver. 2



Ver. 3

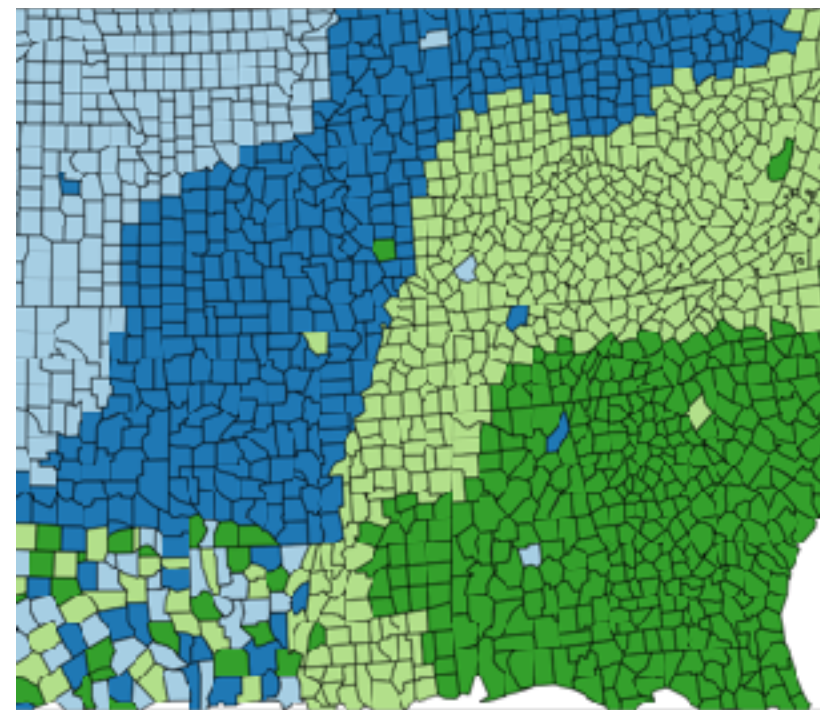
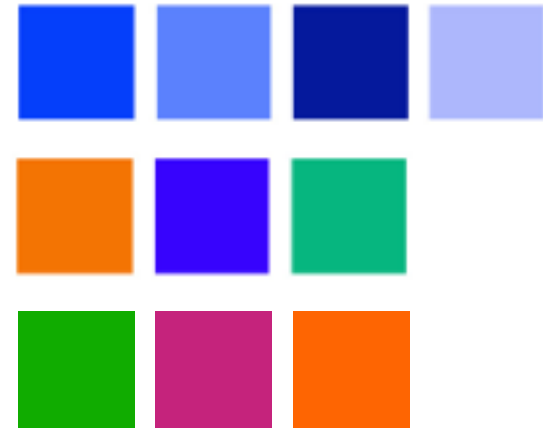
Ver. 4



color

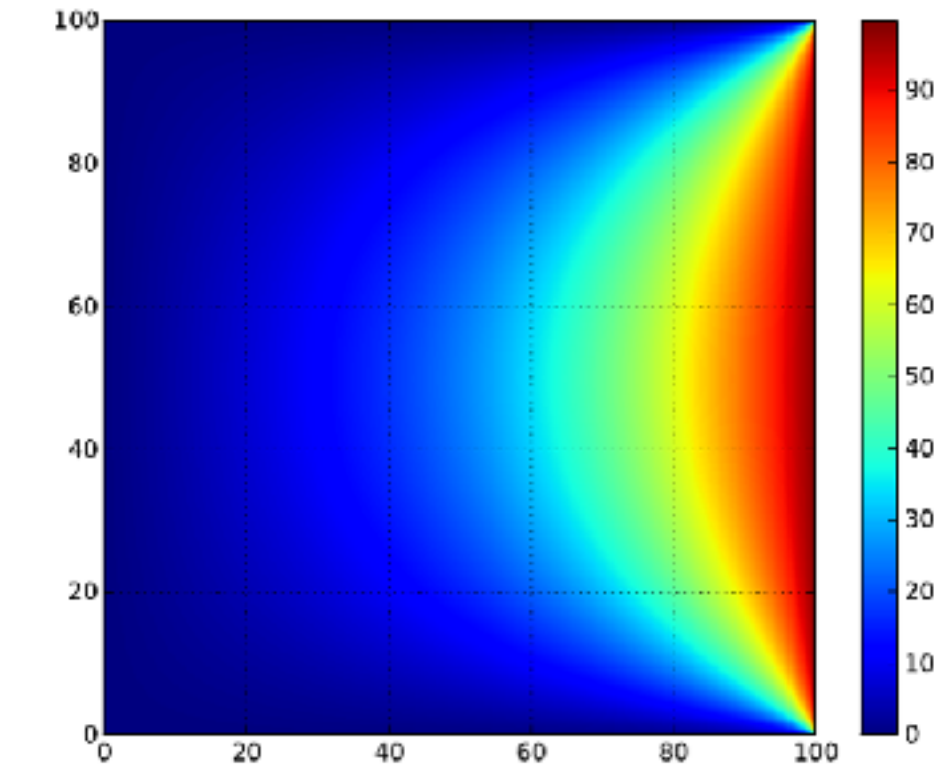
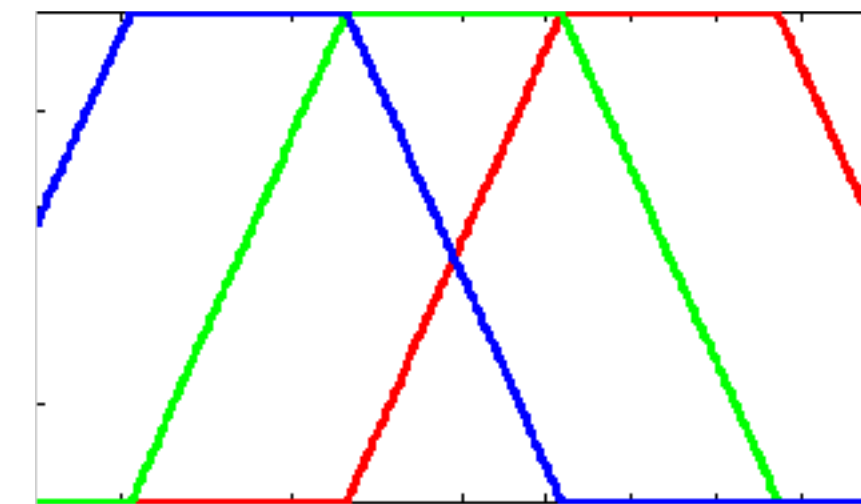
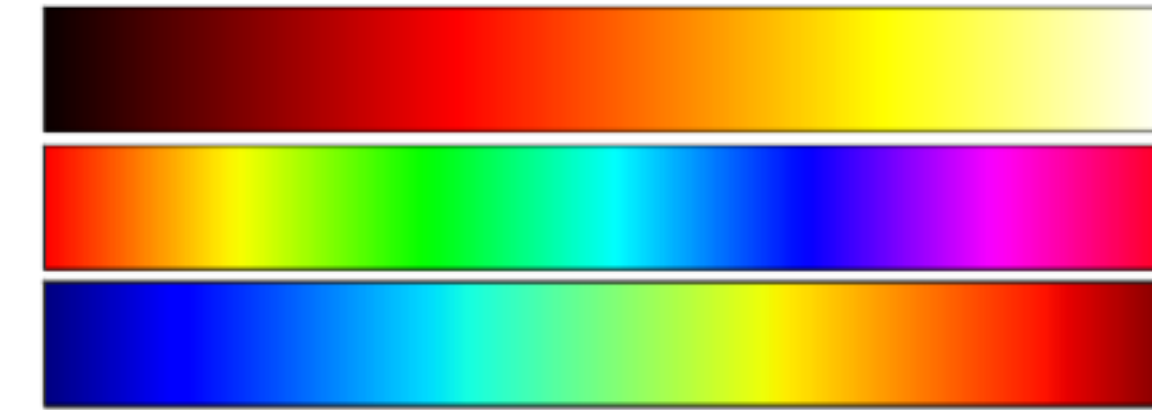
# Color schemes

discrete palette



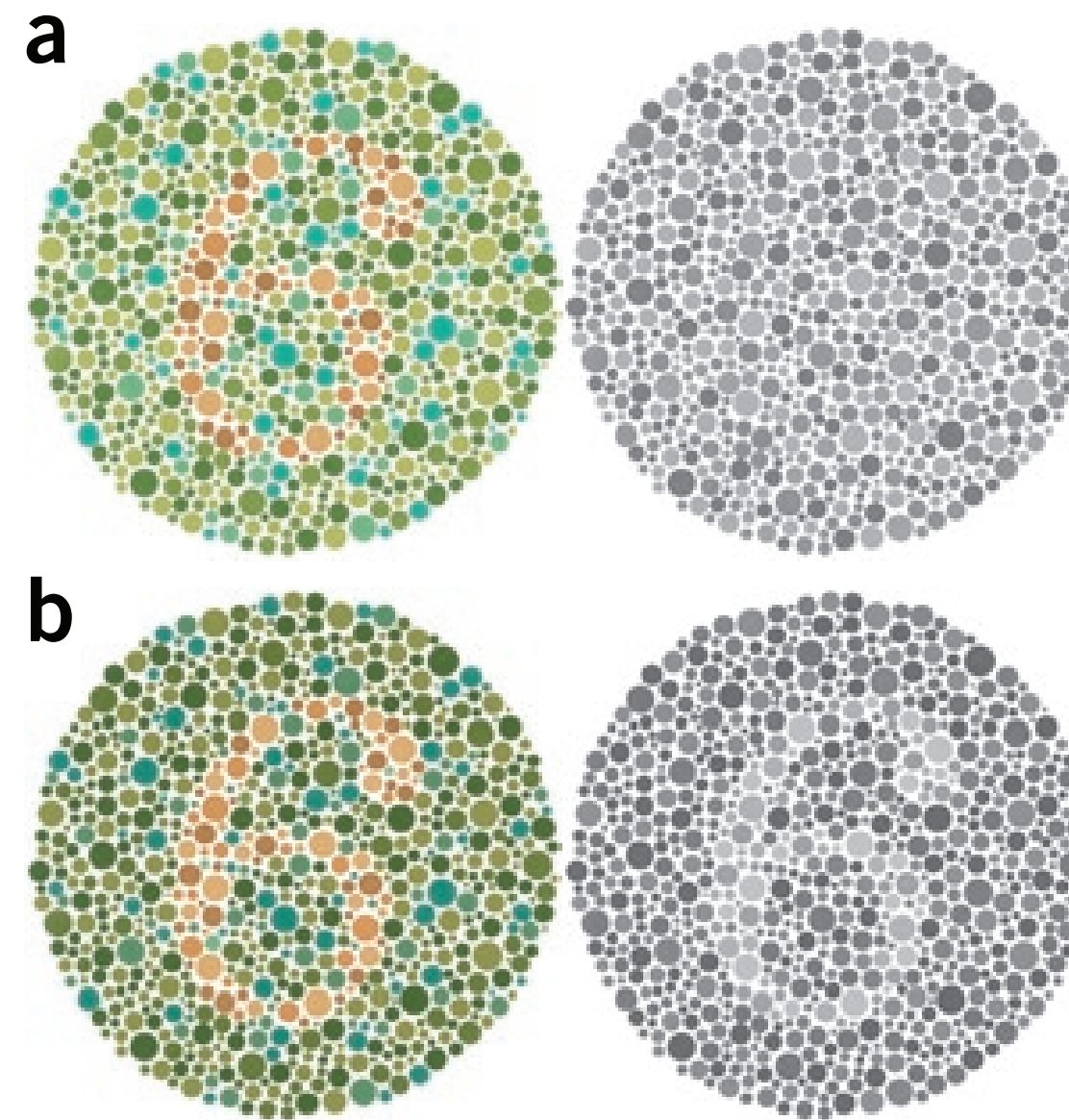
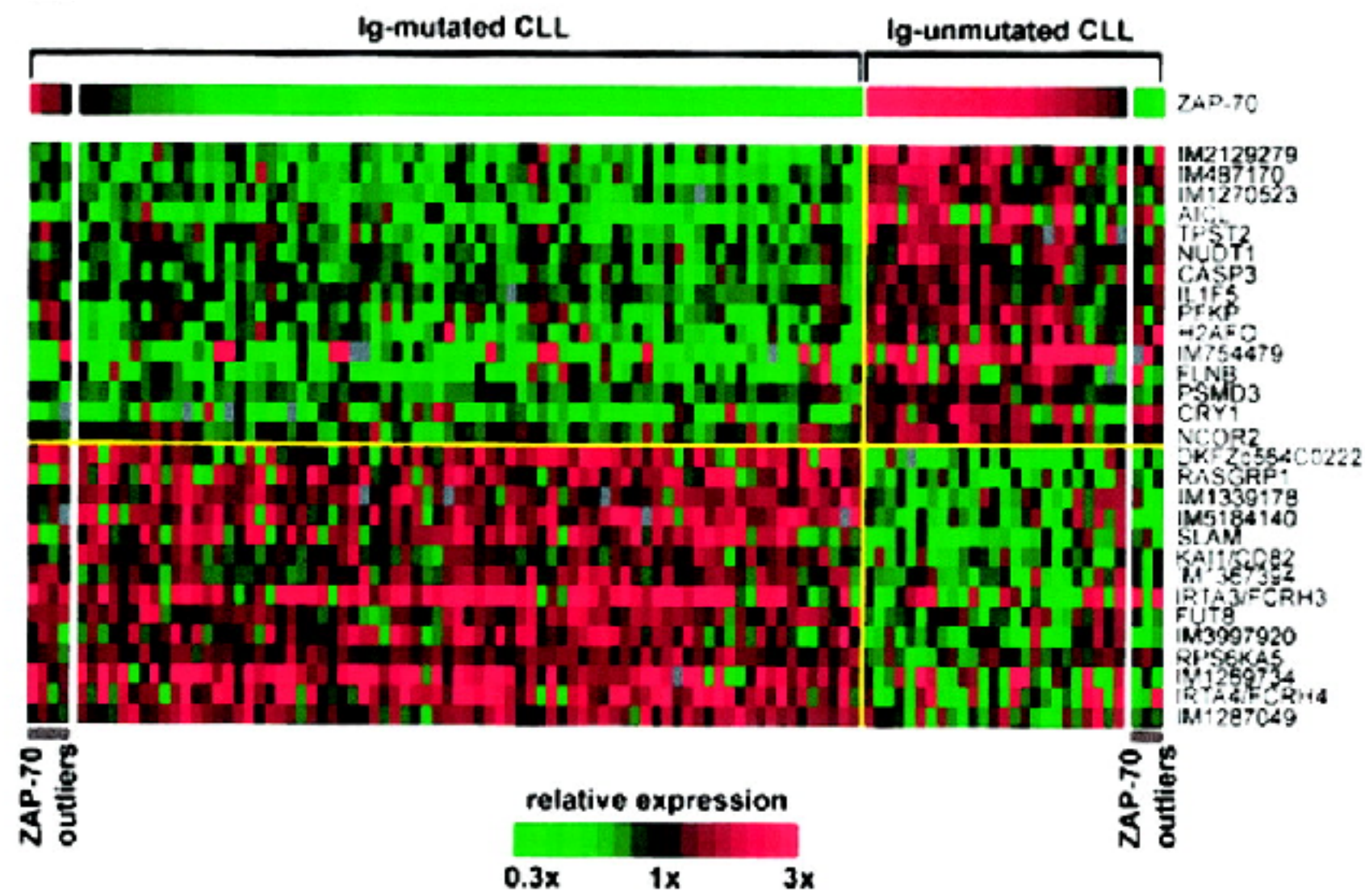
# Colormaps

continuous (function)



Good idea to lean on existing, **evidence-based** palettes (*Tableau 10*) and maps (*Viridis*)

# Color blindness: the **eye** is a noisy channel



**Figure 1** | Ishihara color-vision test plate. (a) Viewers with normal color vision should see the numeral '6'. (b) Changing lightness of background improves contrast.



Don't rely completely on color— tweak hue/saturation to improve contrast

Red/Green blindness is most common → avoid it

Put it all together:

Keep it simple?

# VINYL

Comparing Music Artists through Visualization

Search for an artist...

Radiohead X

Muse X

Up to 4 artists can be added to the comparison.

## More Options

Find a song on this chart

Just cluster similar songs

Split View

Show Album Cover

Avoid Overlapping

How to read this vis?

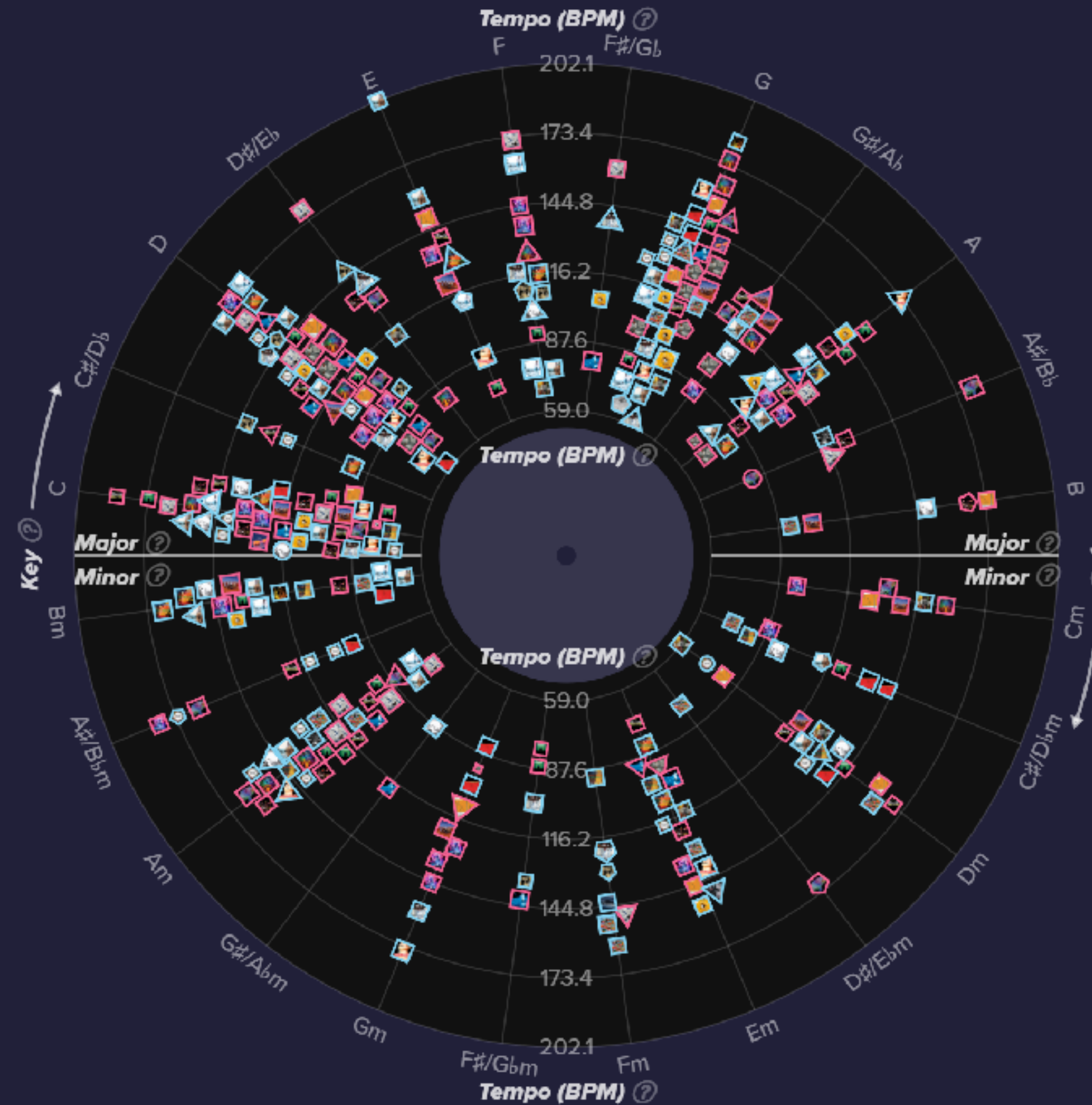
**About the Data** The data visualized here were pulled from [Spotify API](#). Most data attributes are computed by Spotify's audio analysis algorithms.

X / Angular Axis

KEY

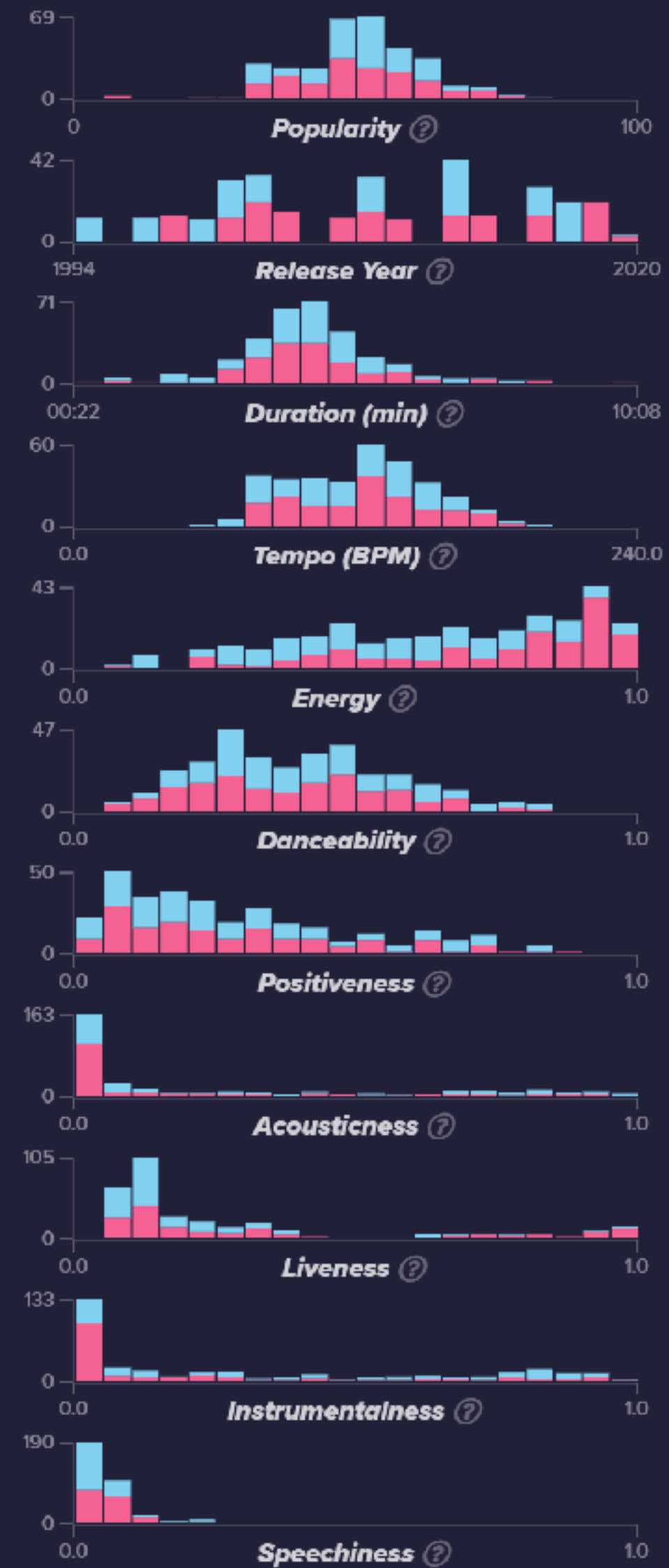
Y / Radial Axis

TEMPO



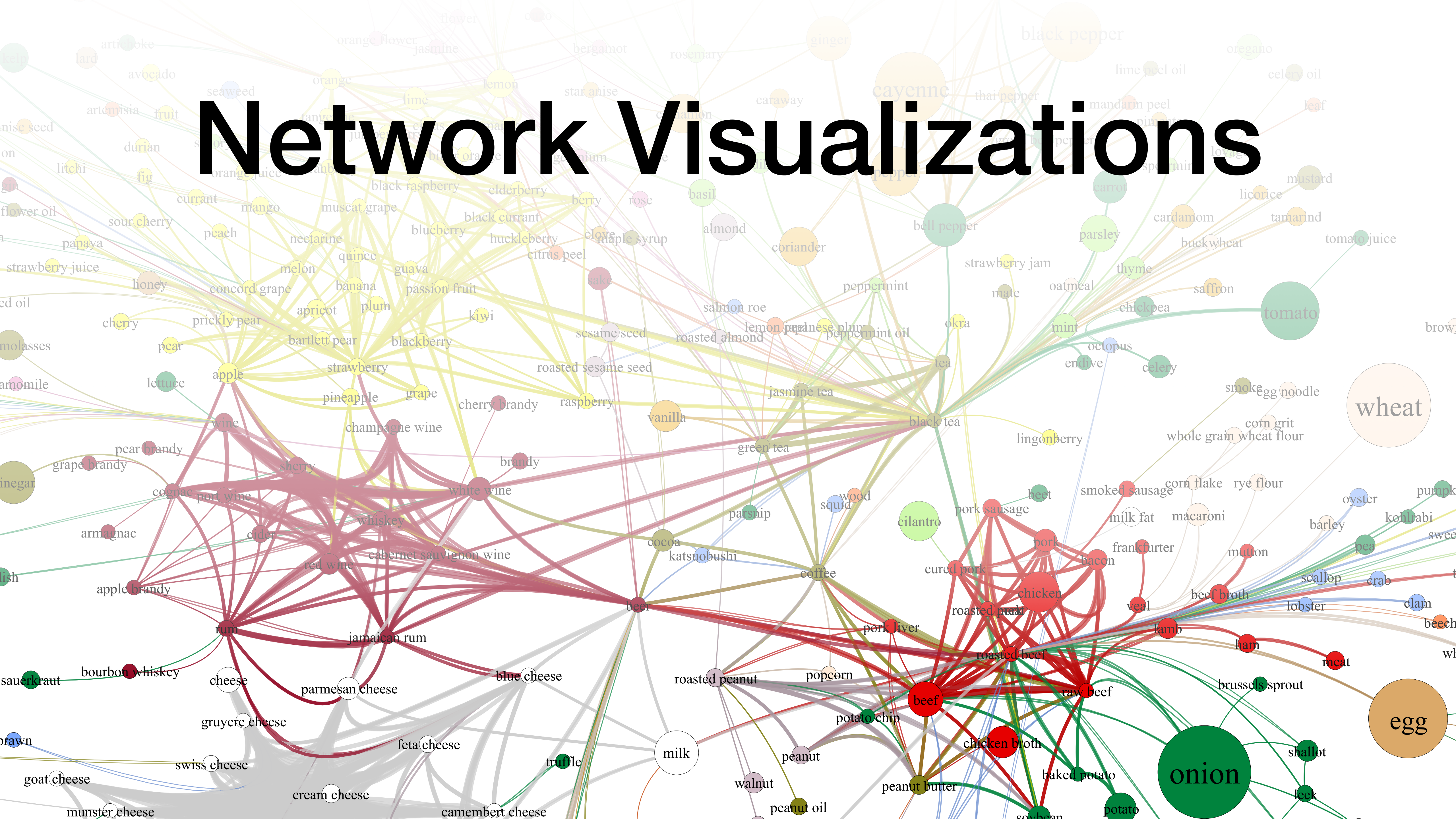
Drag a song here for more details

## Song Feature Distributions



Made by [Tae Prasongpongchai](#), [Xi Chen](#), [Benjamin Du Preez](#), [McKenzie Murphy](#).

# Network Visualizations



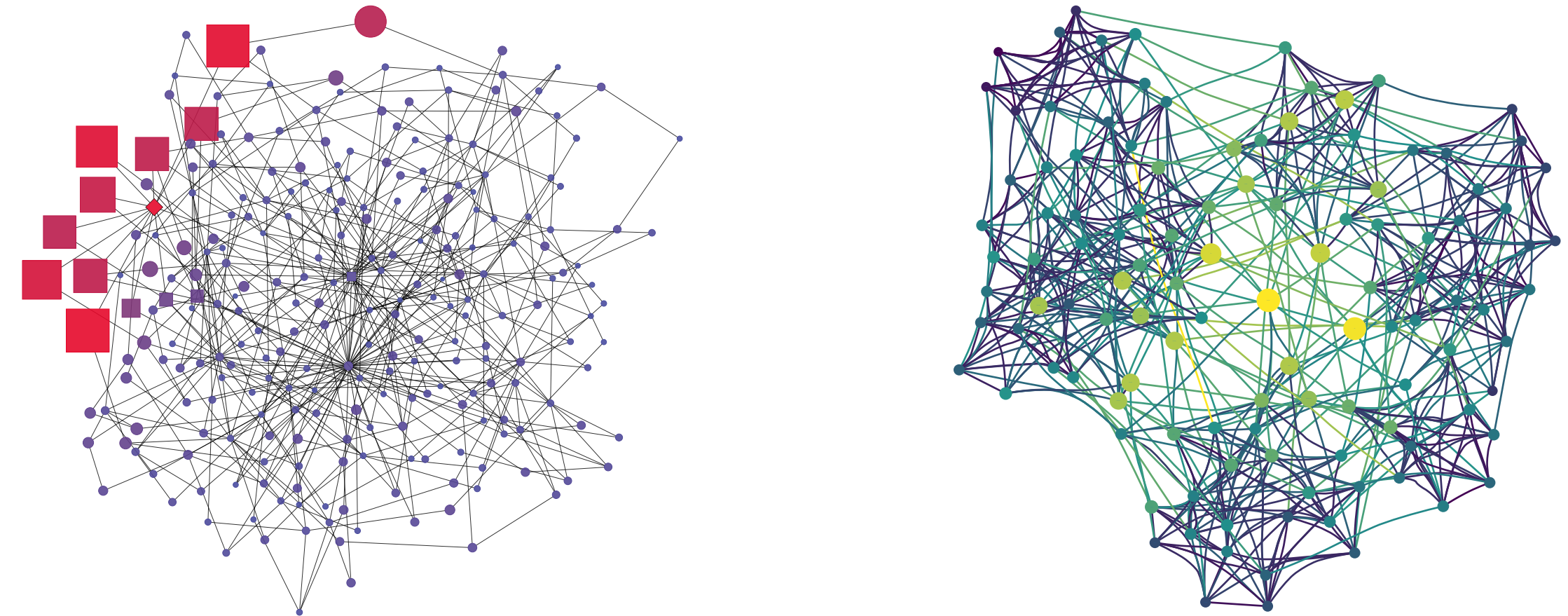
# Network visualizations

Before we begin, a **tough question**: is a network visualization **appropriate**?

Ghoniem *et al.* InfoVis'04 (2004)

Foucault Welles & Meirelles (2015)

Foucault Welles & Xu (2018)

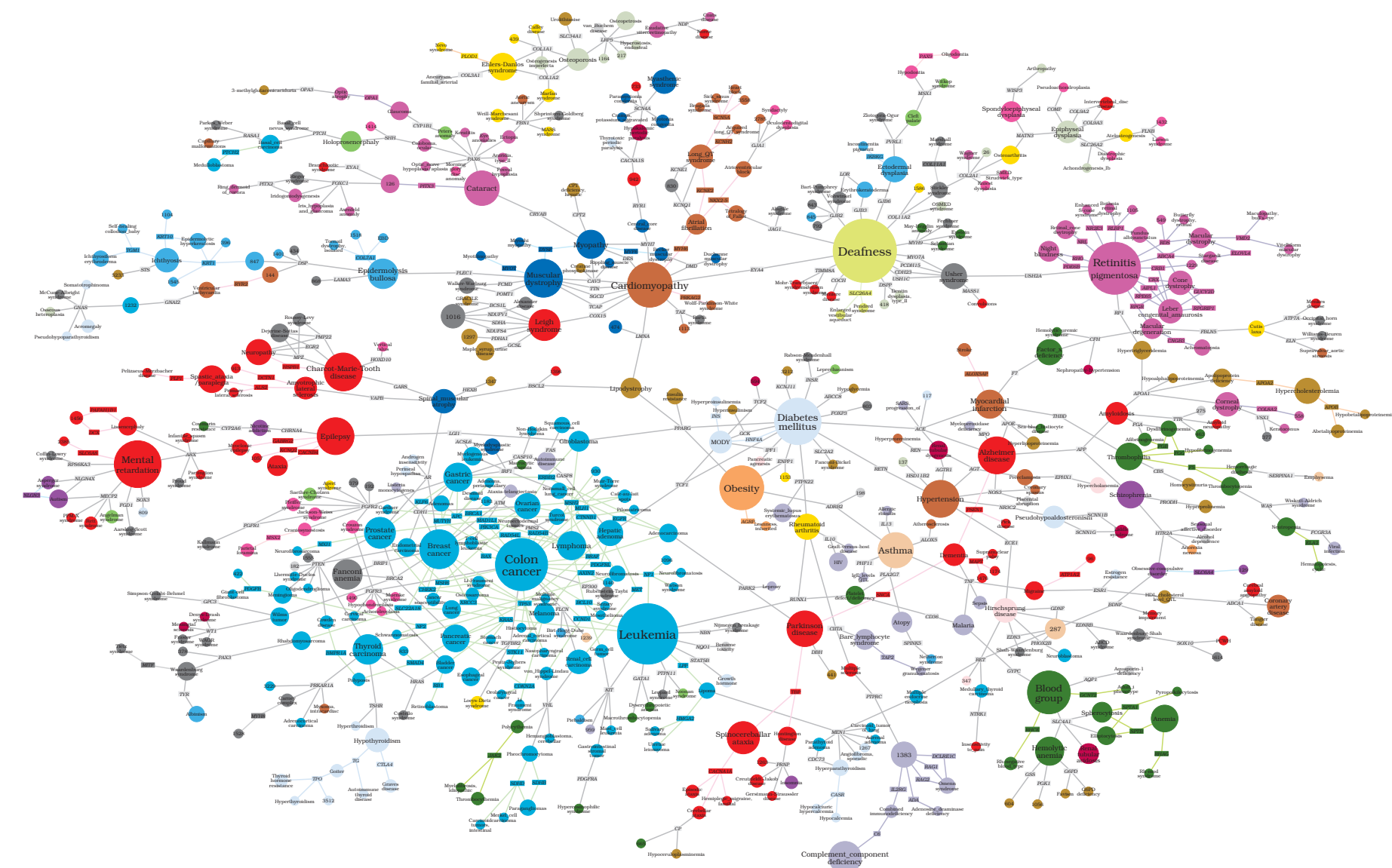


Alternative approaches

Bagrow *et al.* EPL (2008)

Bagrow & Bollt (2019)

Schulman *et al.* (2011)



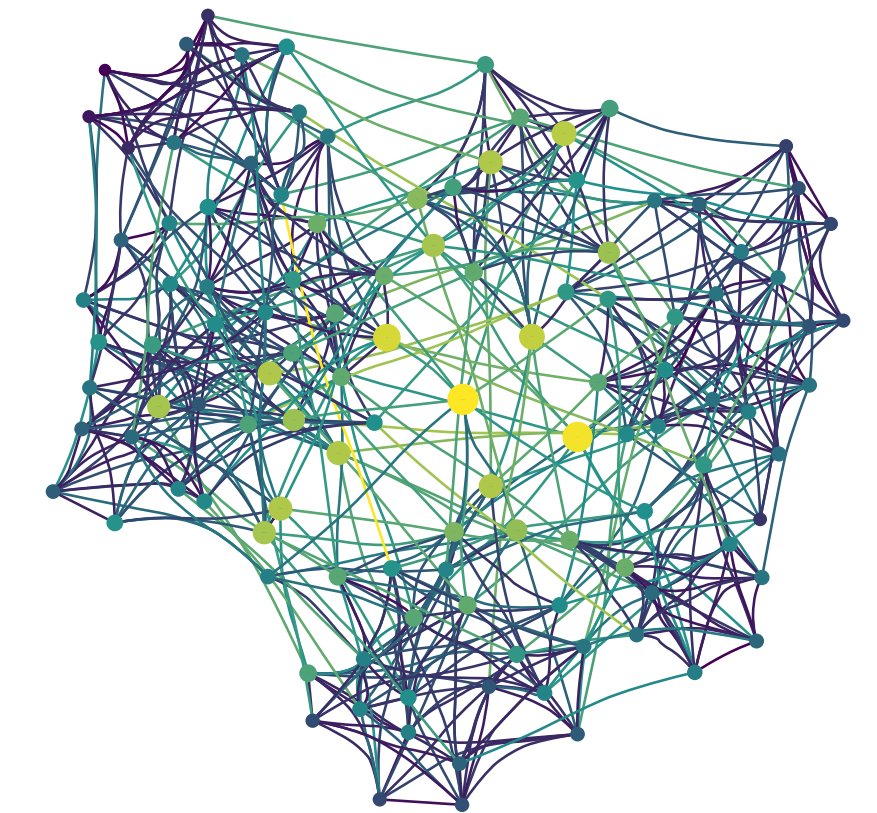
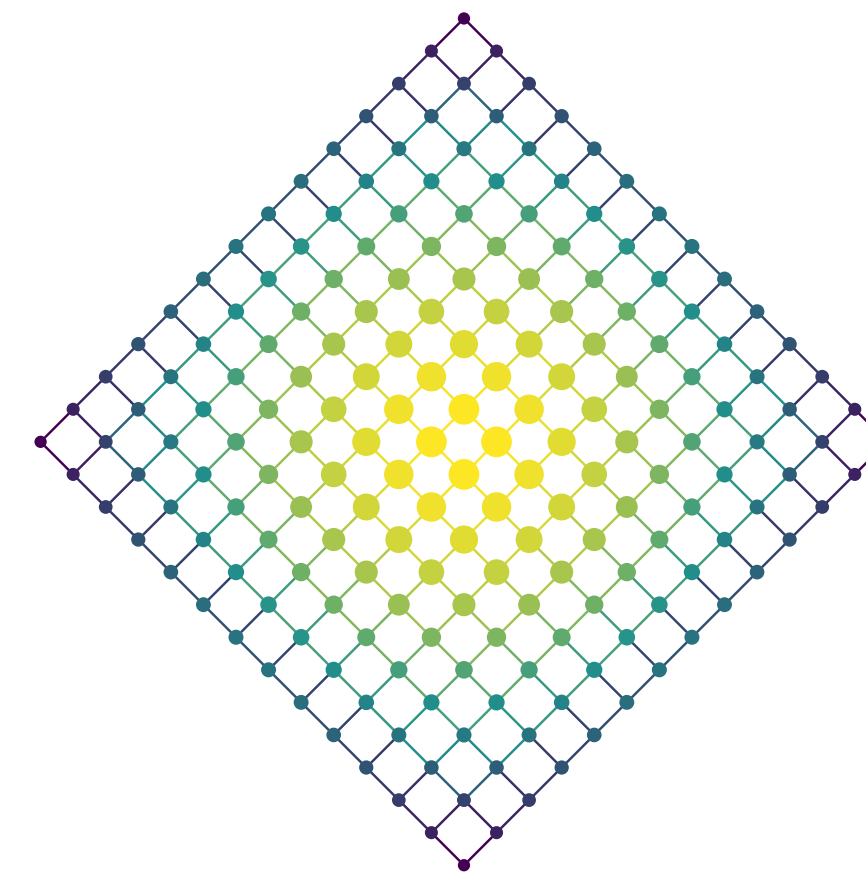
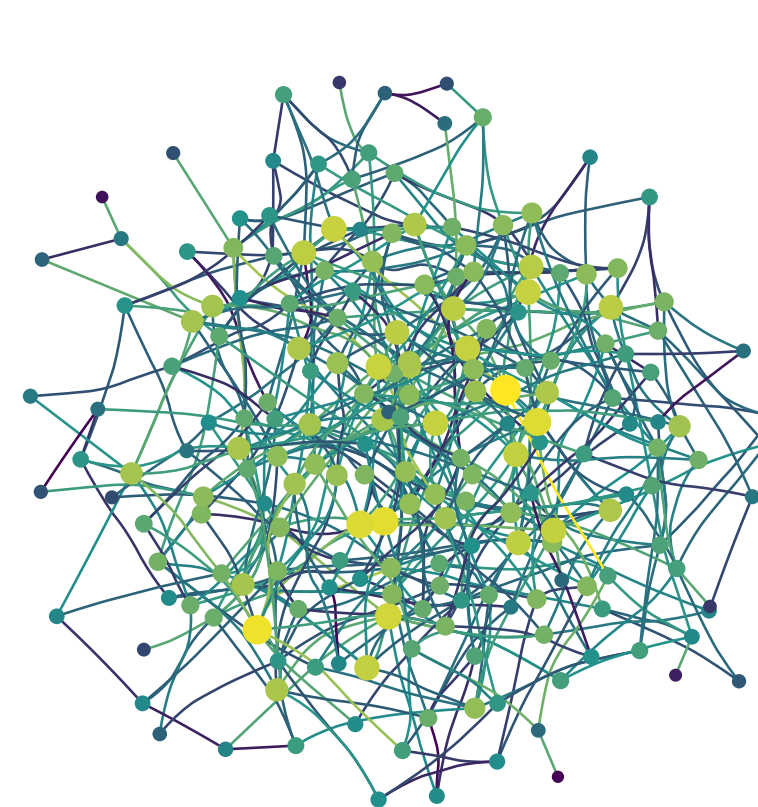
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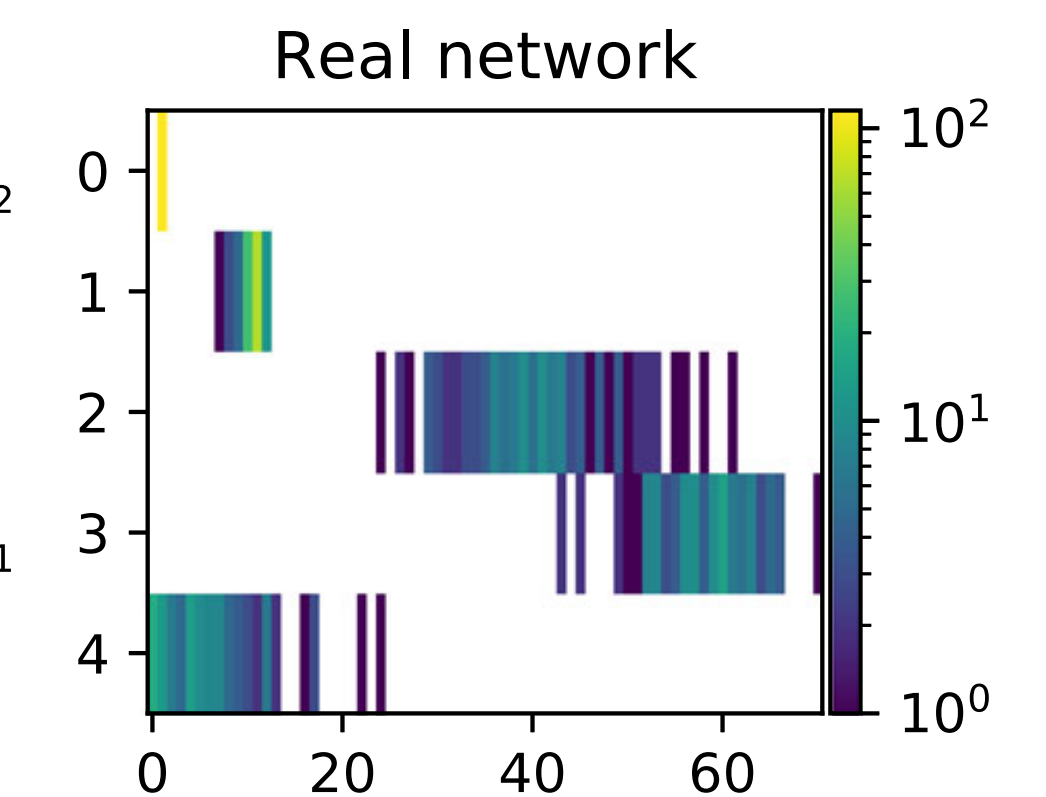
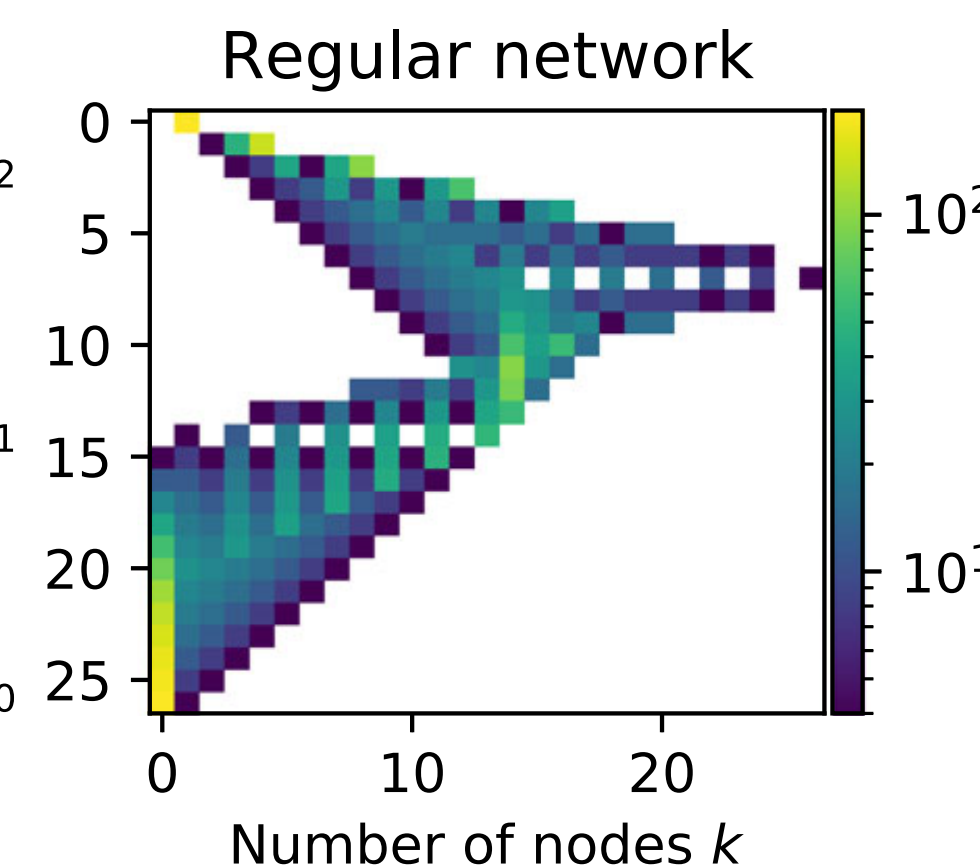
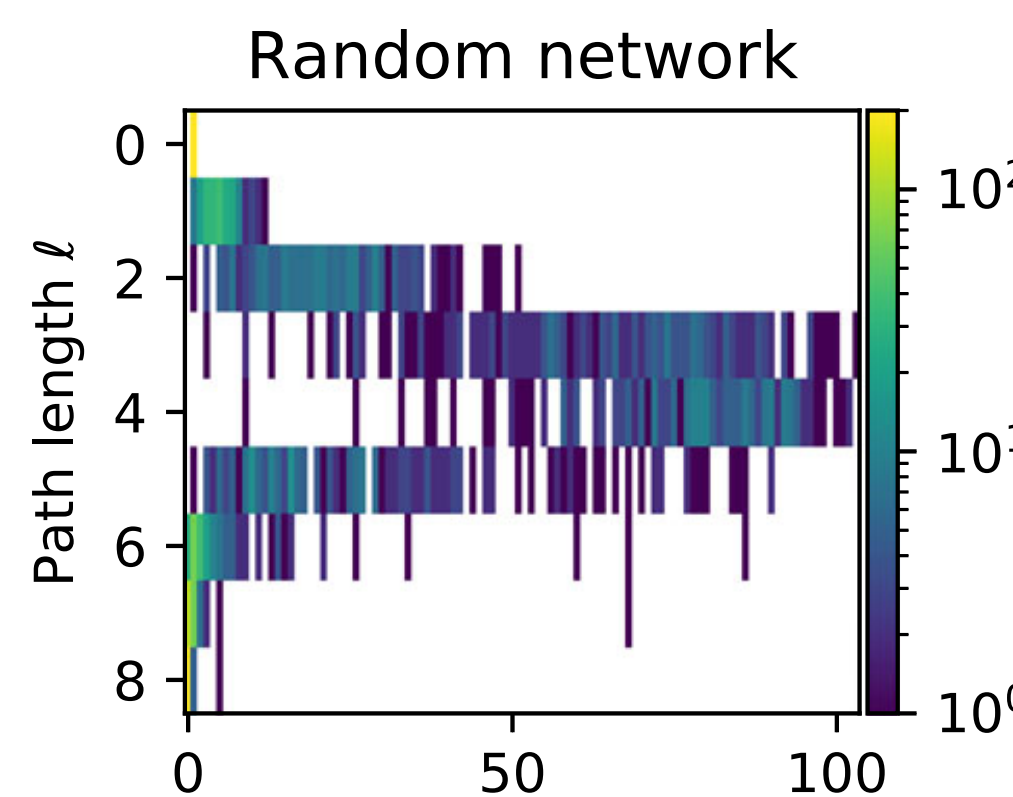


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Schulman *et al.* (2011)





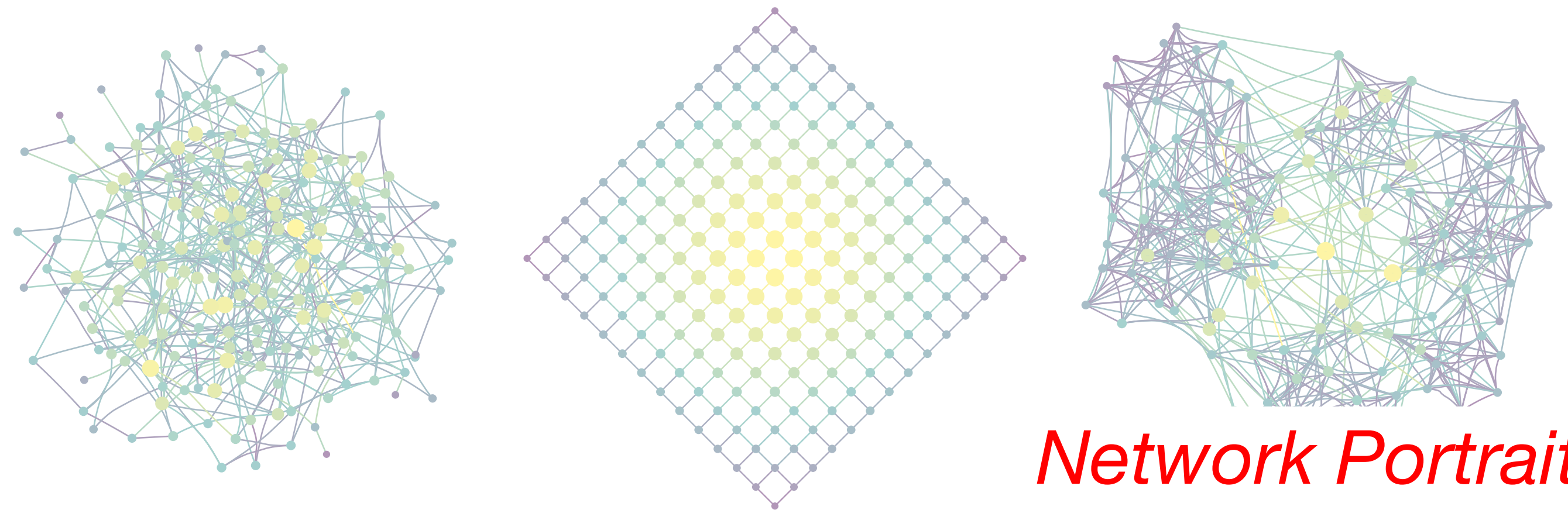
# Network visualizations

Before we begin, a **tough question**: is a network visualization **appropriate**?

Ghoniem *et al.* InfoVis'04 (2004)

Foucault Welles & Meirelles (2015)

Foucault Welles & Xu (2018)



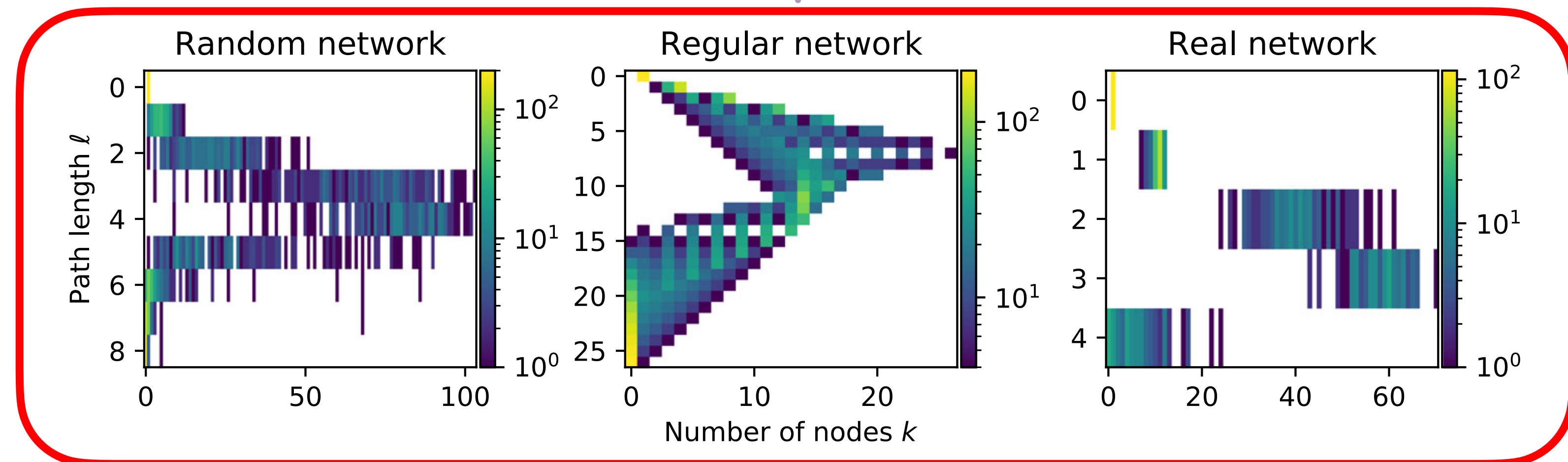
*Network Portraits*

Alternative approaches

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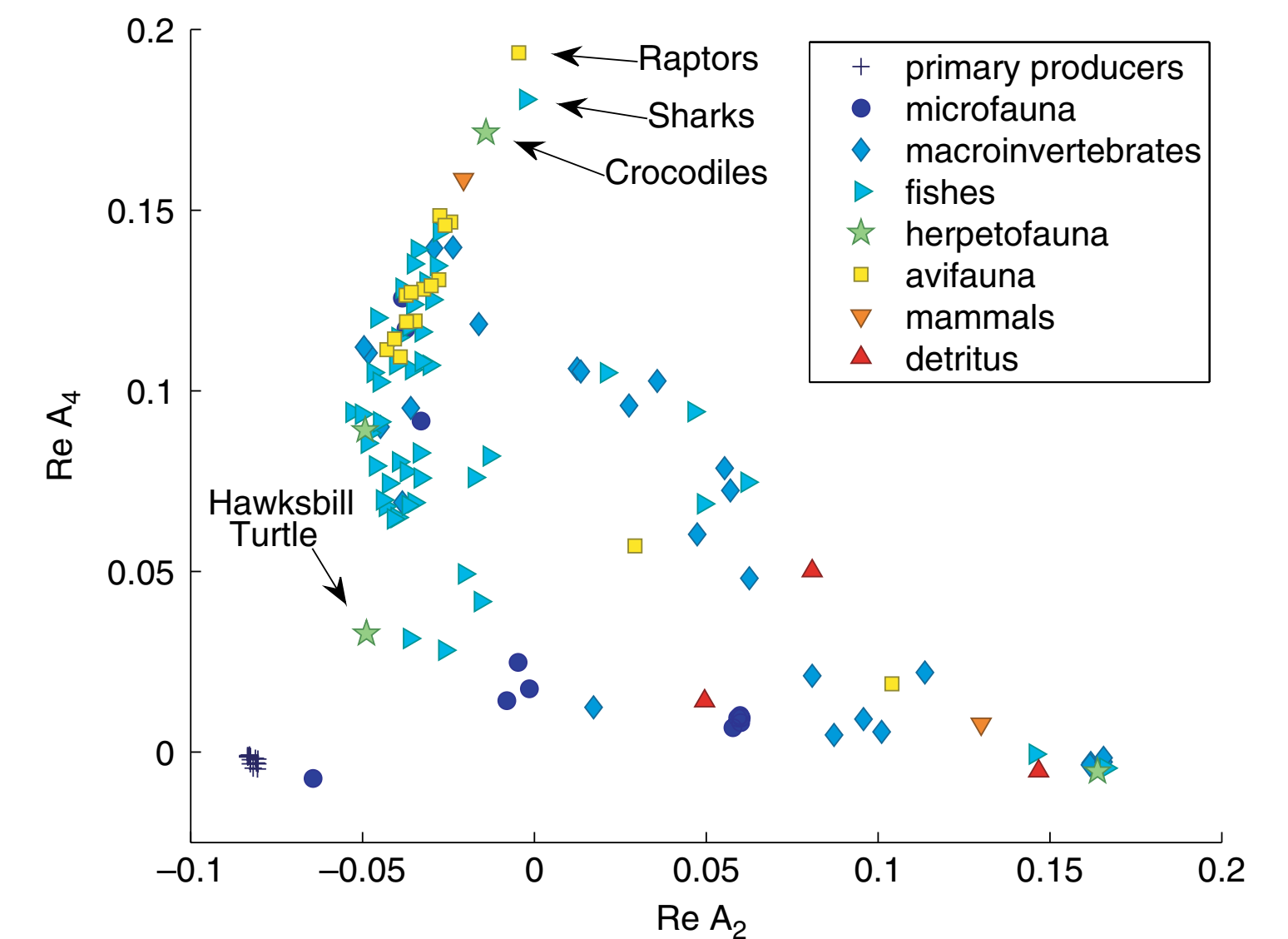
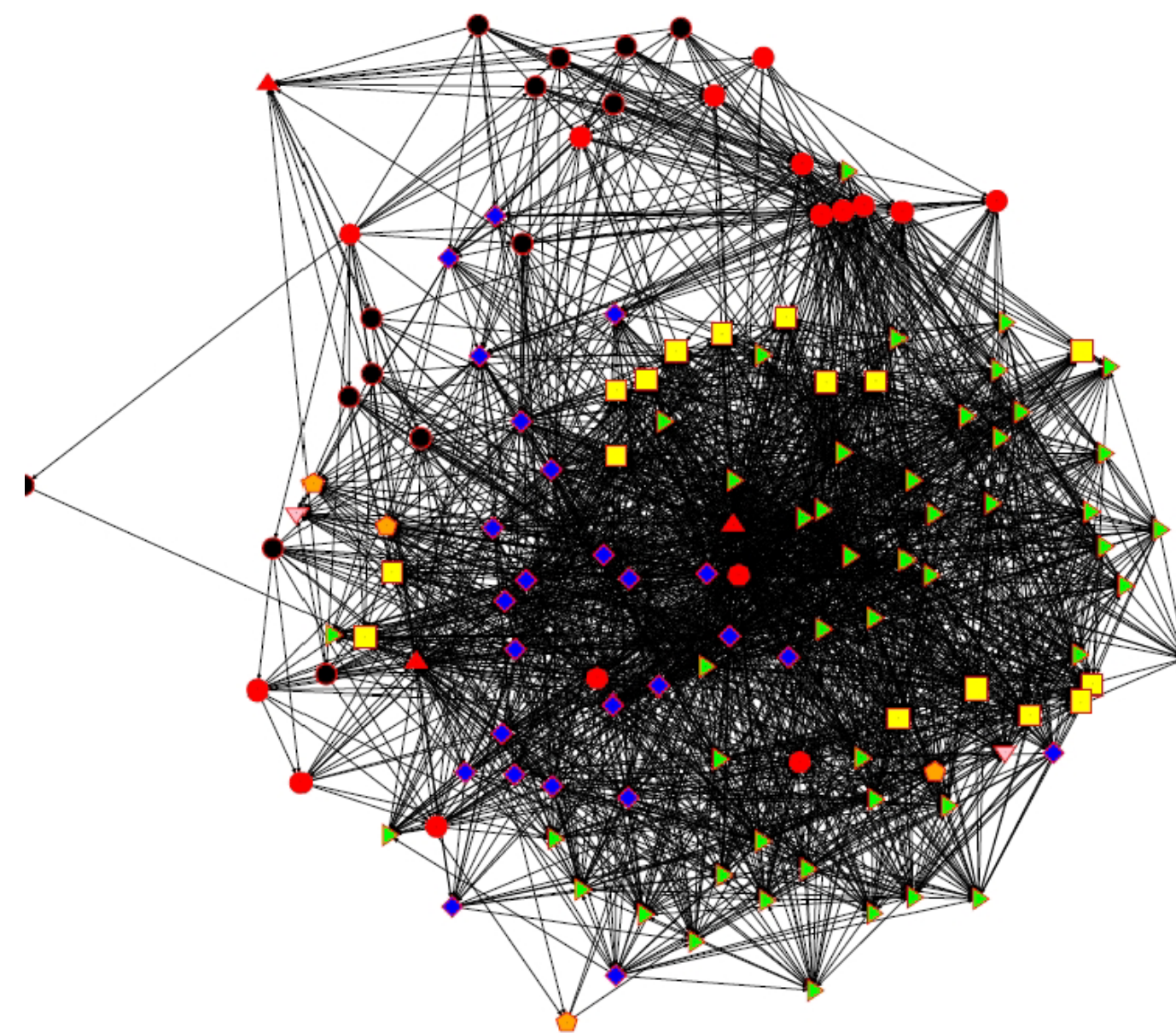
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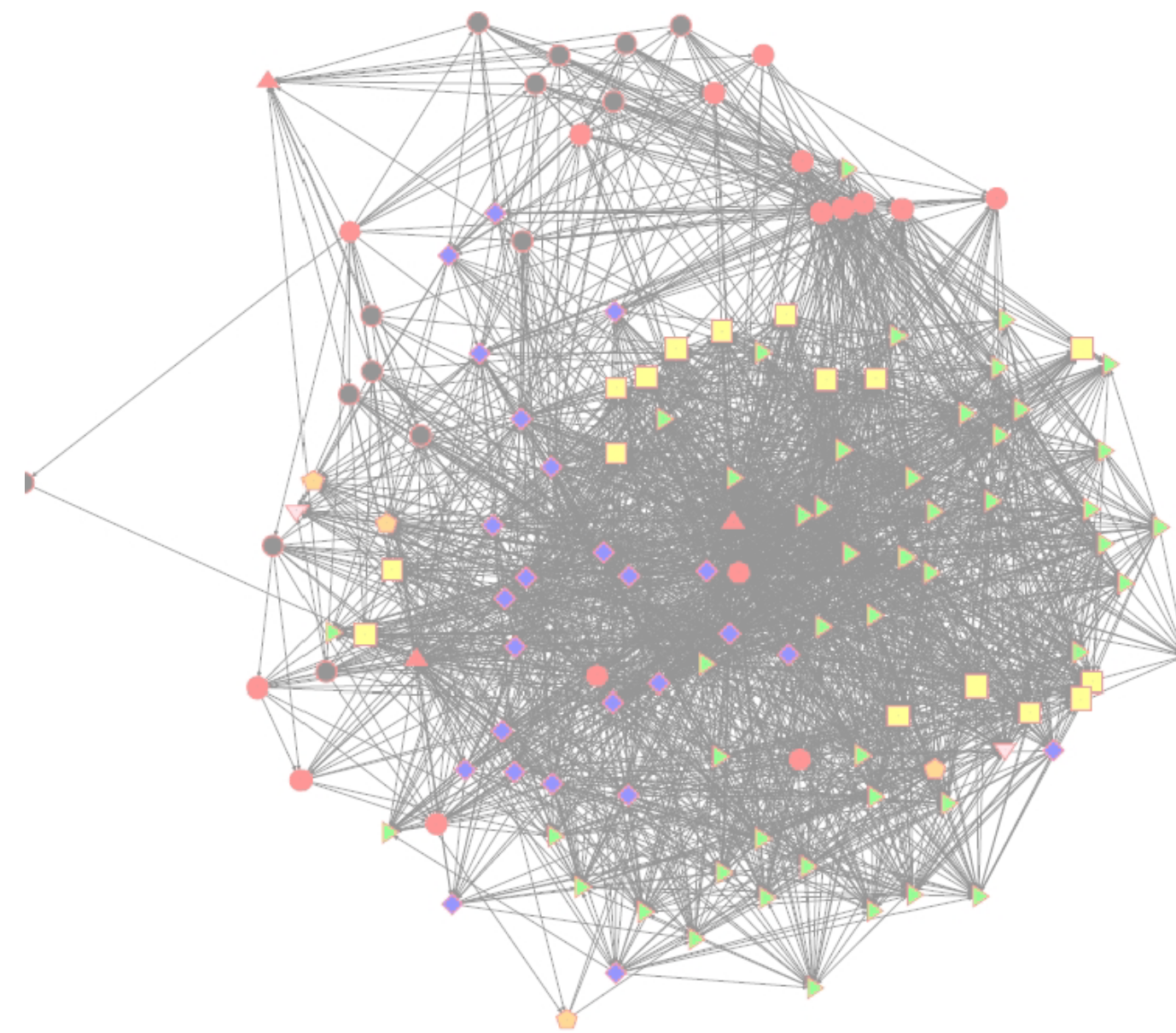
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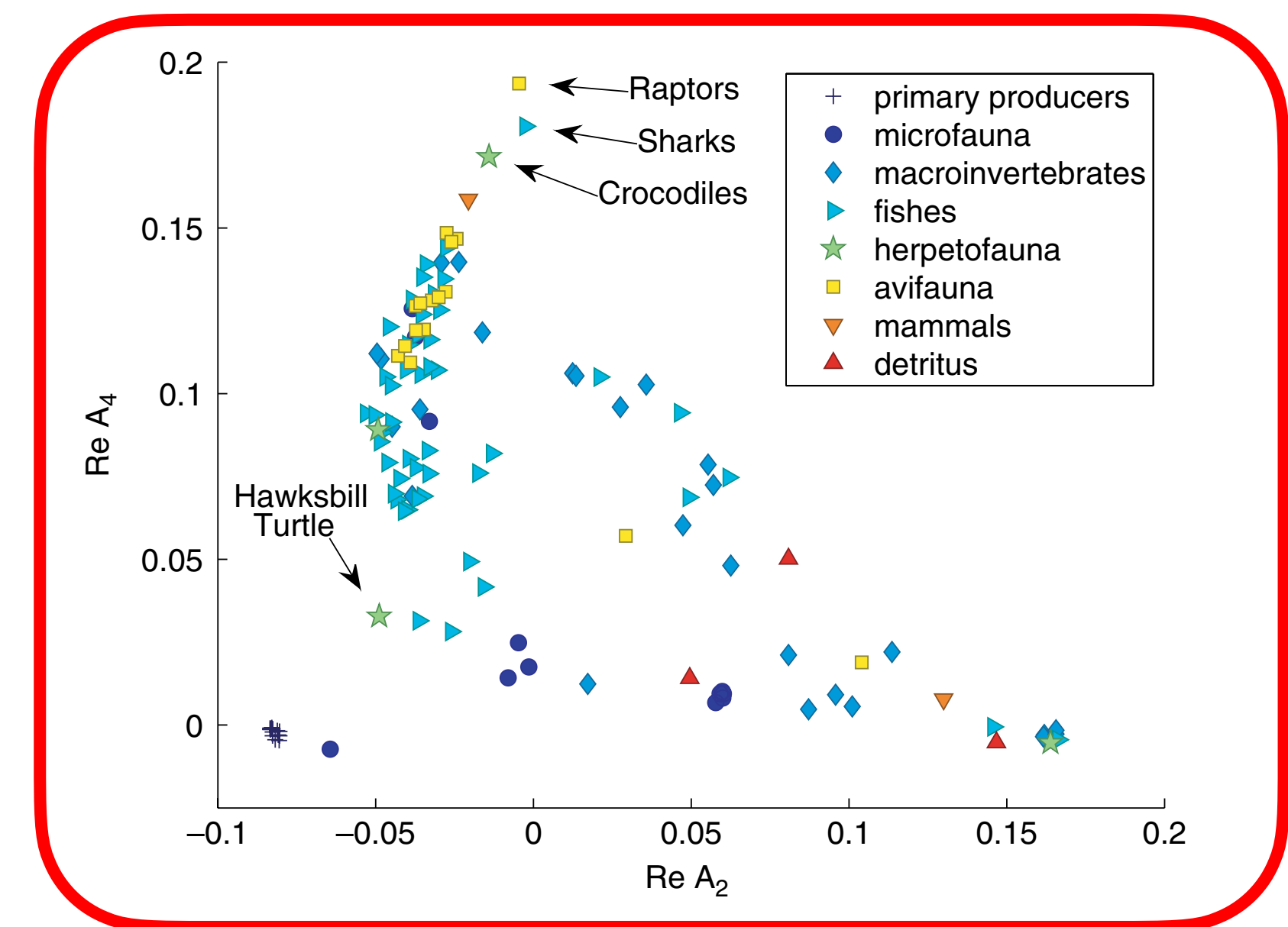
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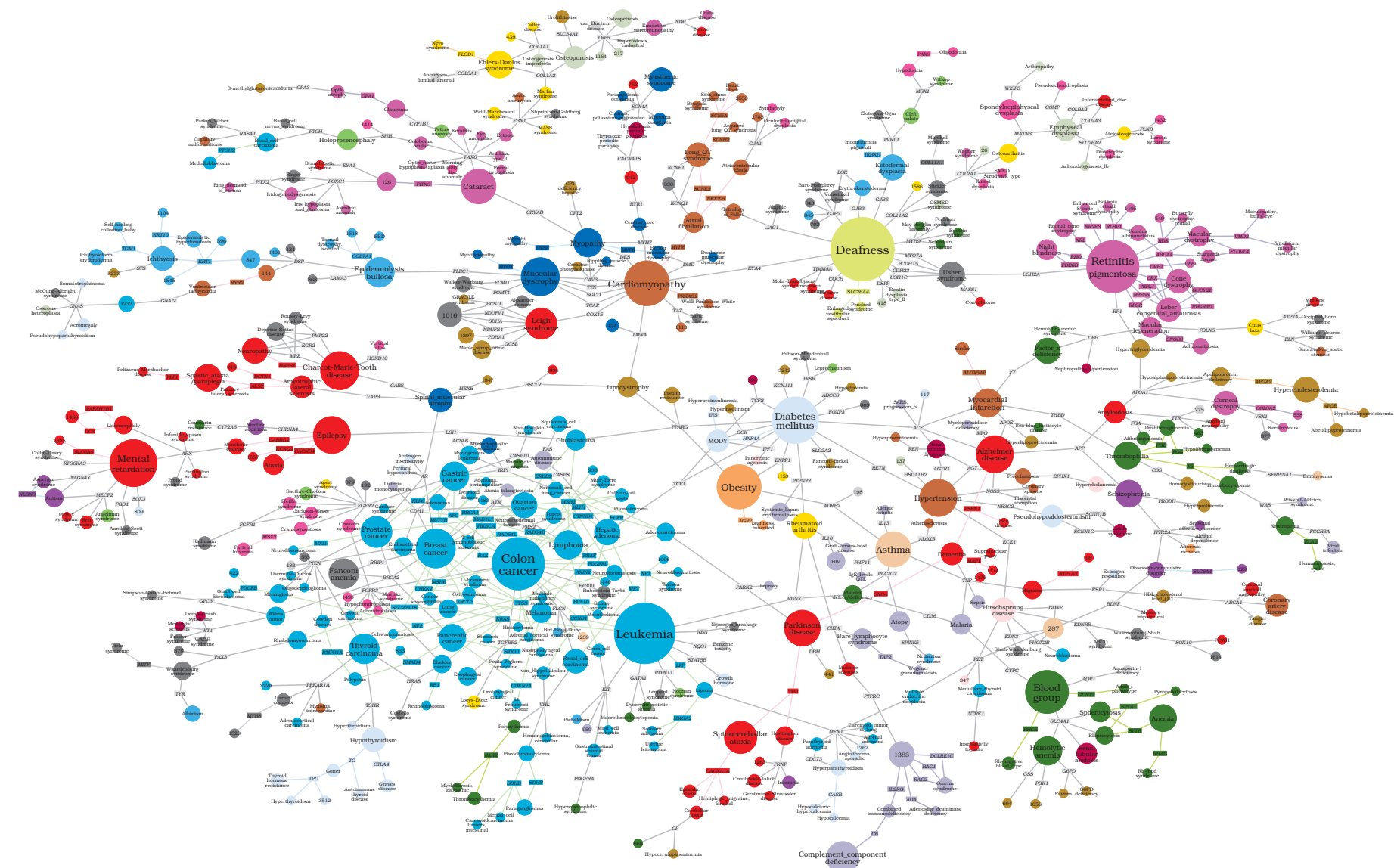
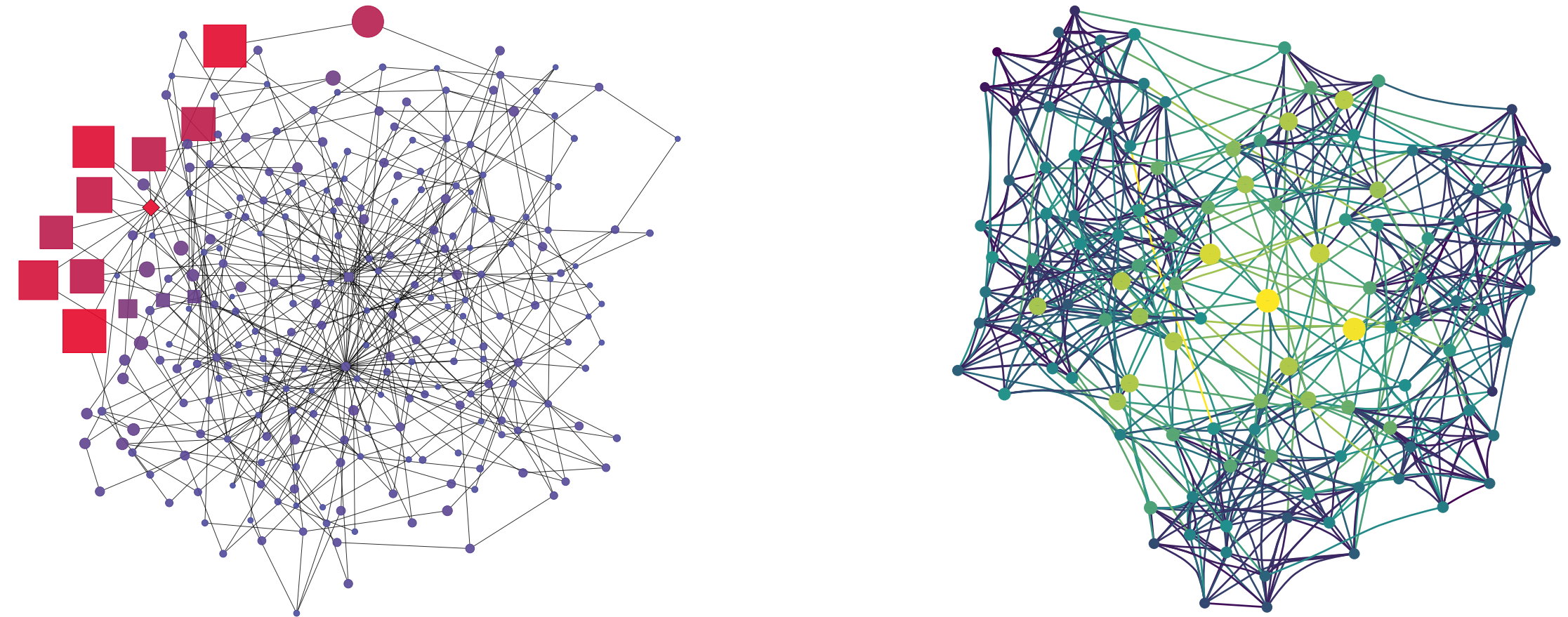
**Observable Representation**



# Network visualizations

- Know your message
- Know your medium
- Know your audience
- Account for strengths and weaknesses of human perception
- Keep it simple

All these points still hold for *visualizing networks*



# Aspects of a network visualization

1. Layout (node coordinates)
2. Node "mapper"
3. Link "mapper"

# Aspects of a network visualization

## 0. Preprocessing

- Project if bipartite?
- **Thin** the network
- Retain only subgraph(s)
- Group nodes, network of **communities**?
- ...

## 1. Layout (node coordinates)

## 2. Node "mapper"

## 3. Link "mapper"

# Aspects of a network visualization

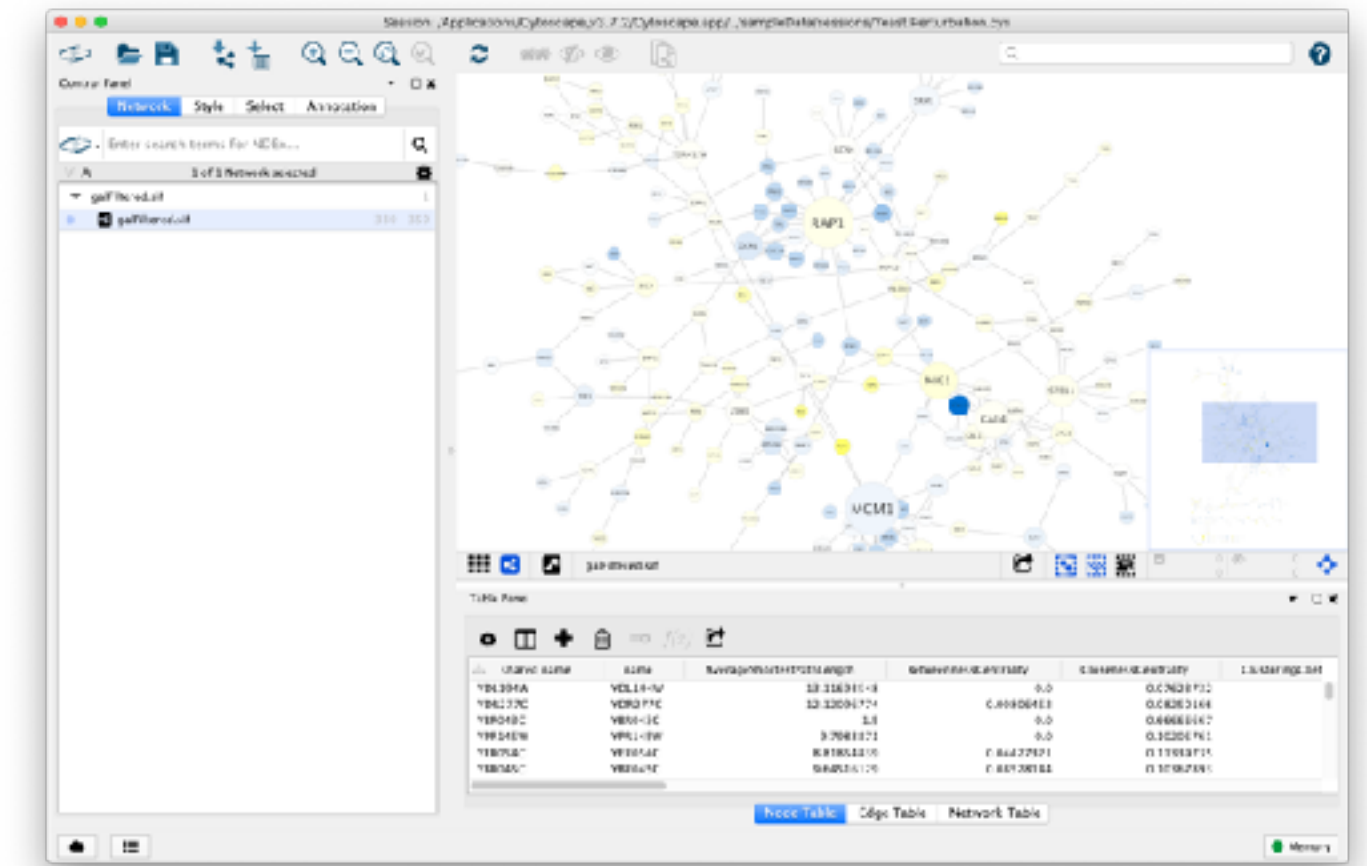
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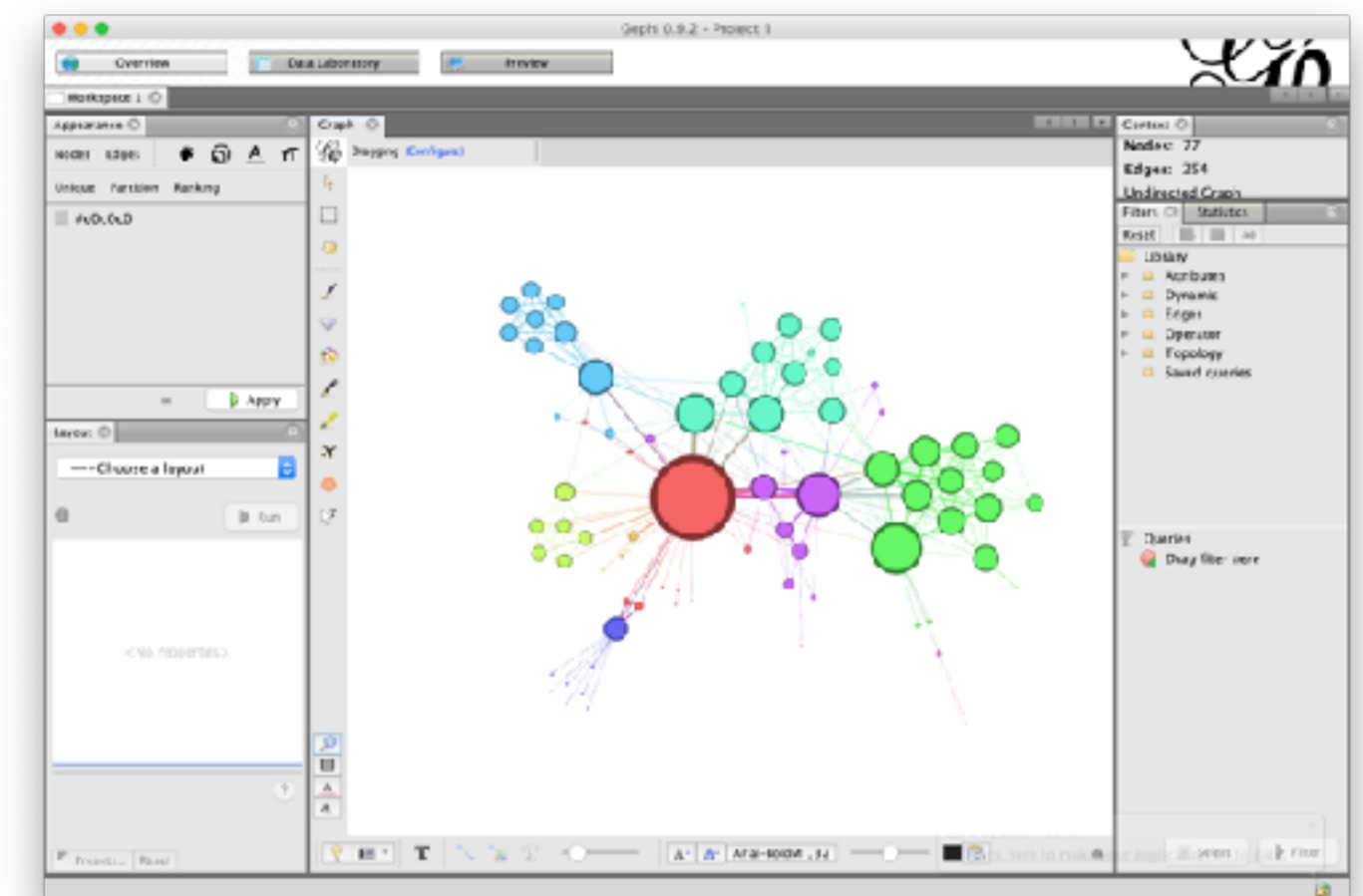
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Apps

Cytoscape



Gephi



# 1. Layout (node2xy)

Place nodes in a **visually meaningful way**  
Minimize link length and crossing...

*Graph drawing* — many algorithms

Can be slow for dense/large  
networks... should large networks  
even be visualized?



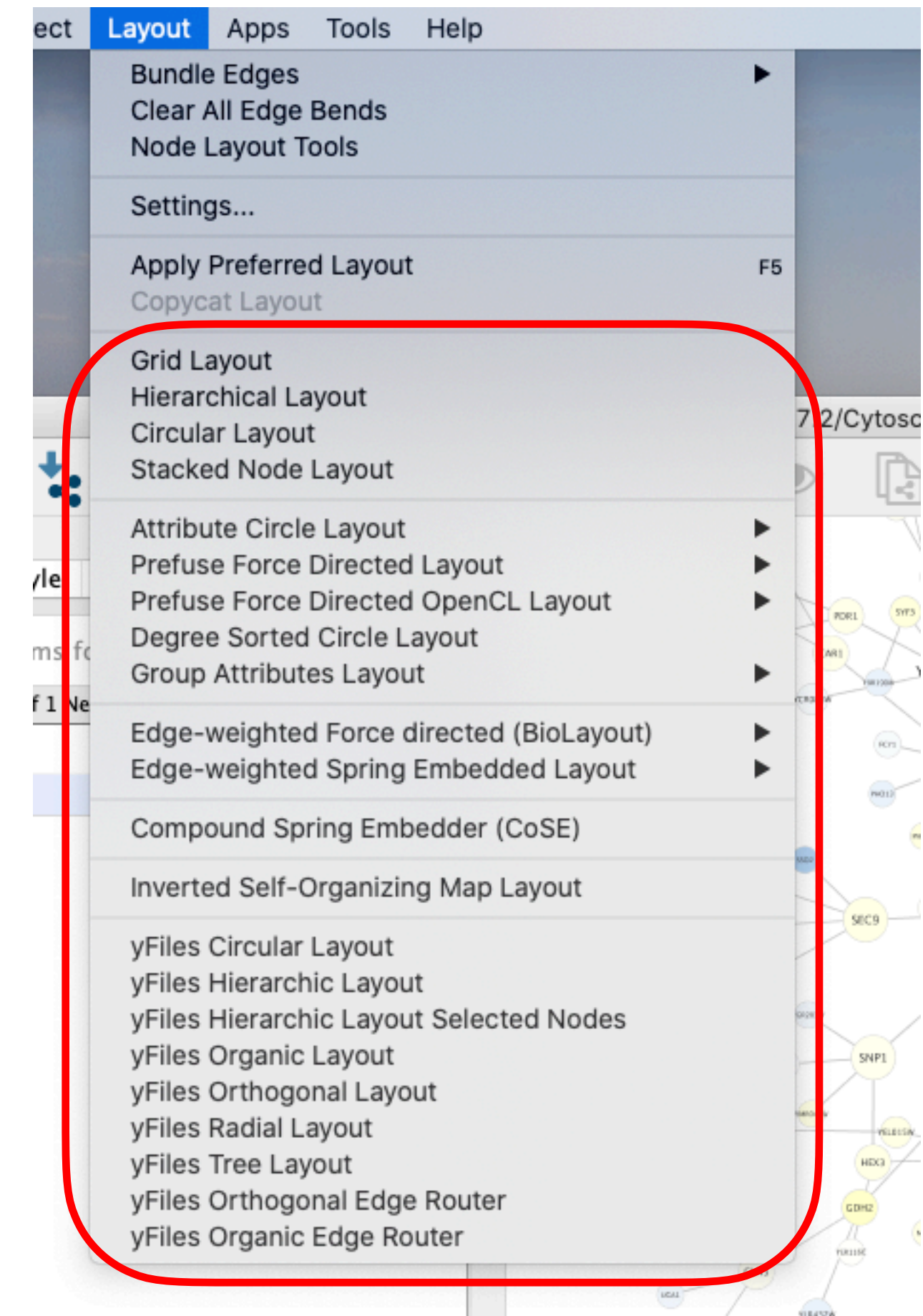
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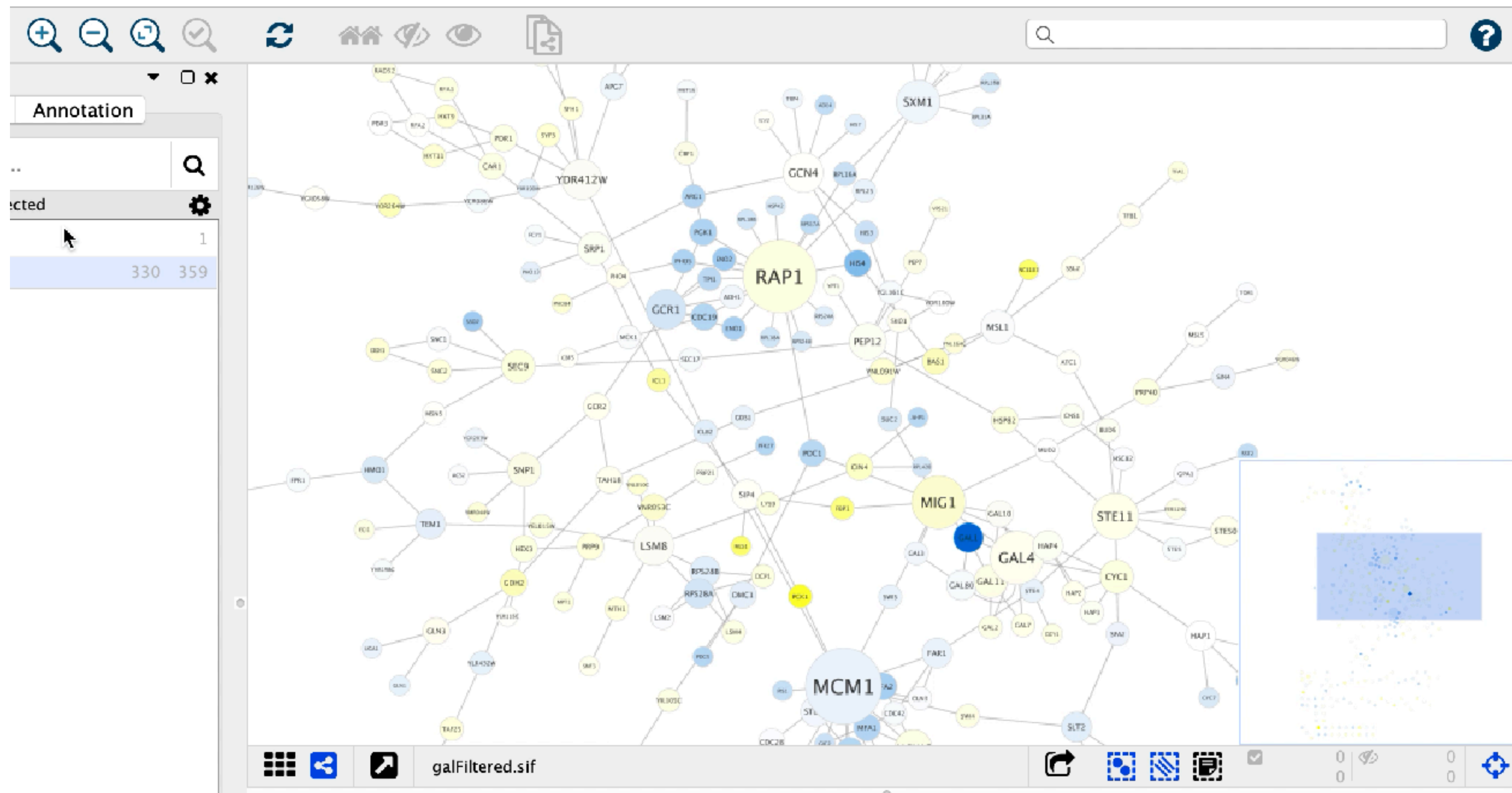
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Cytoscape →



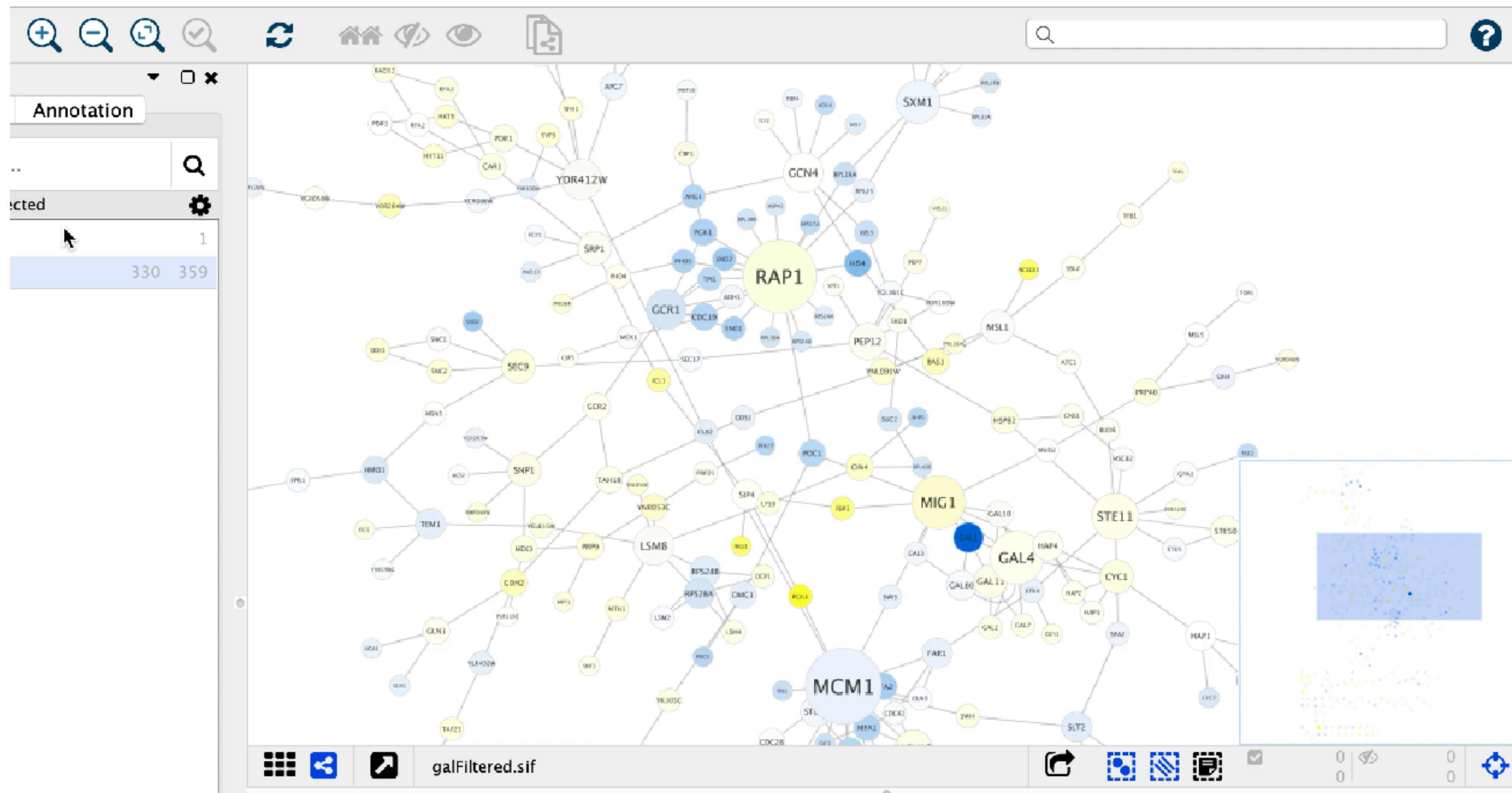
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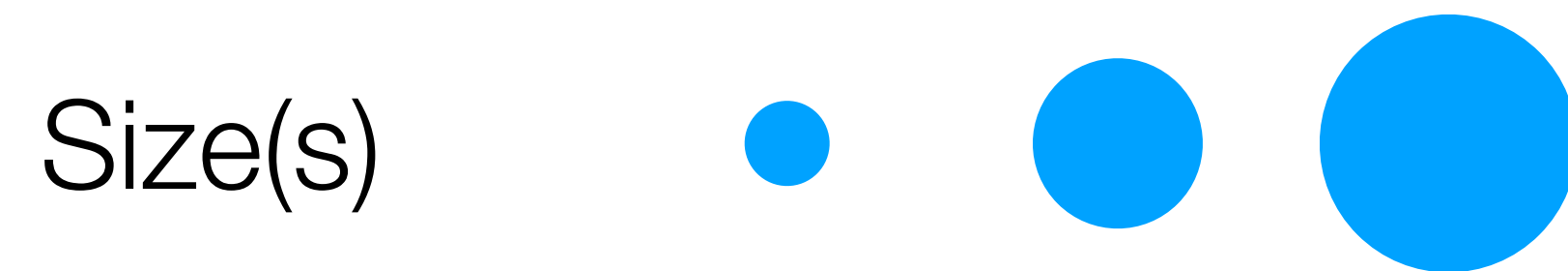
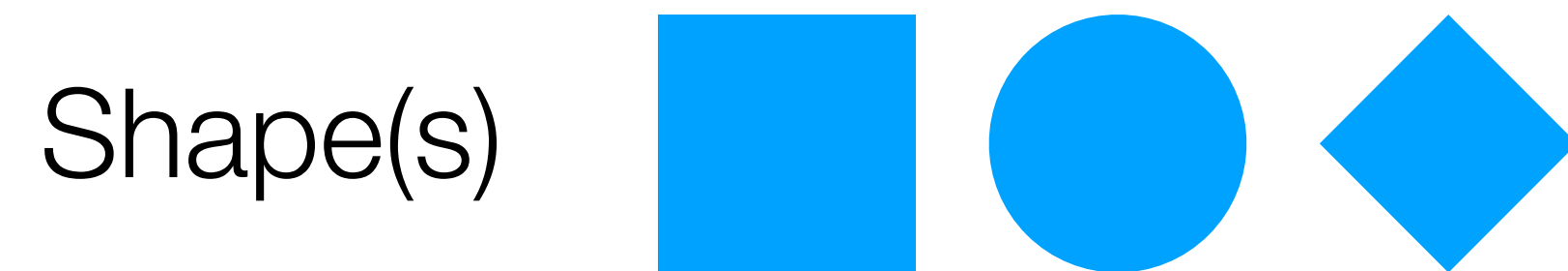
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# 2. Node mapper (node2viz)

How to draw nodes?

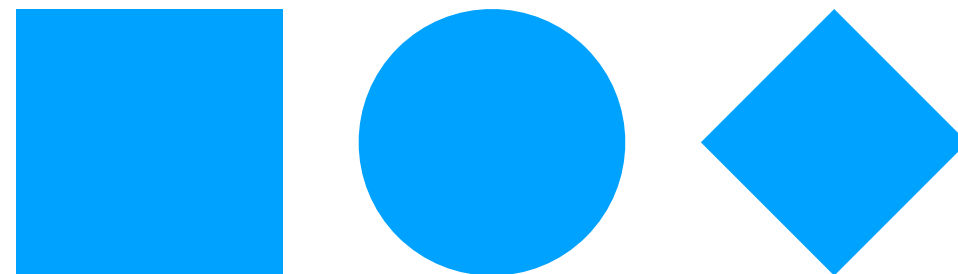


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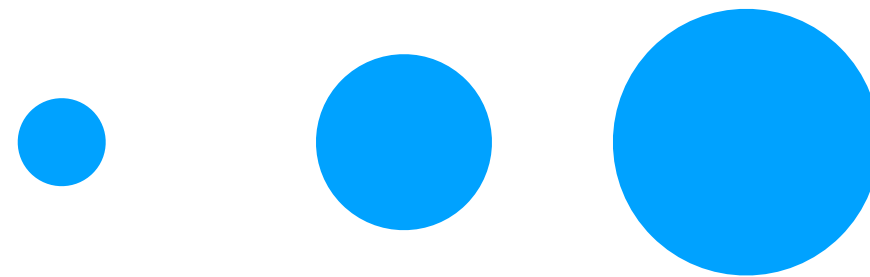
How to draw nodes?

Tip: represent attributes by varying graphics

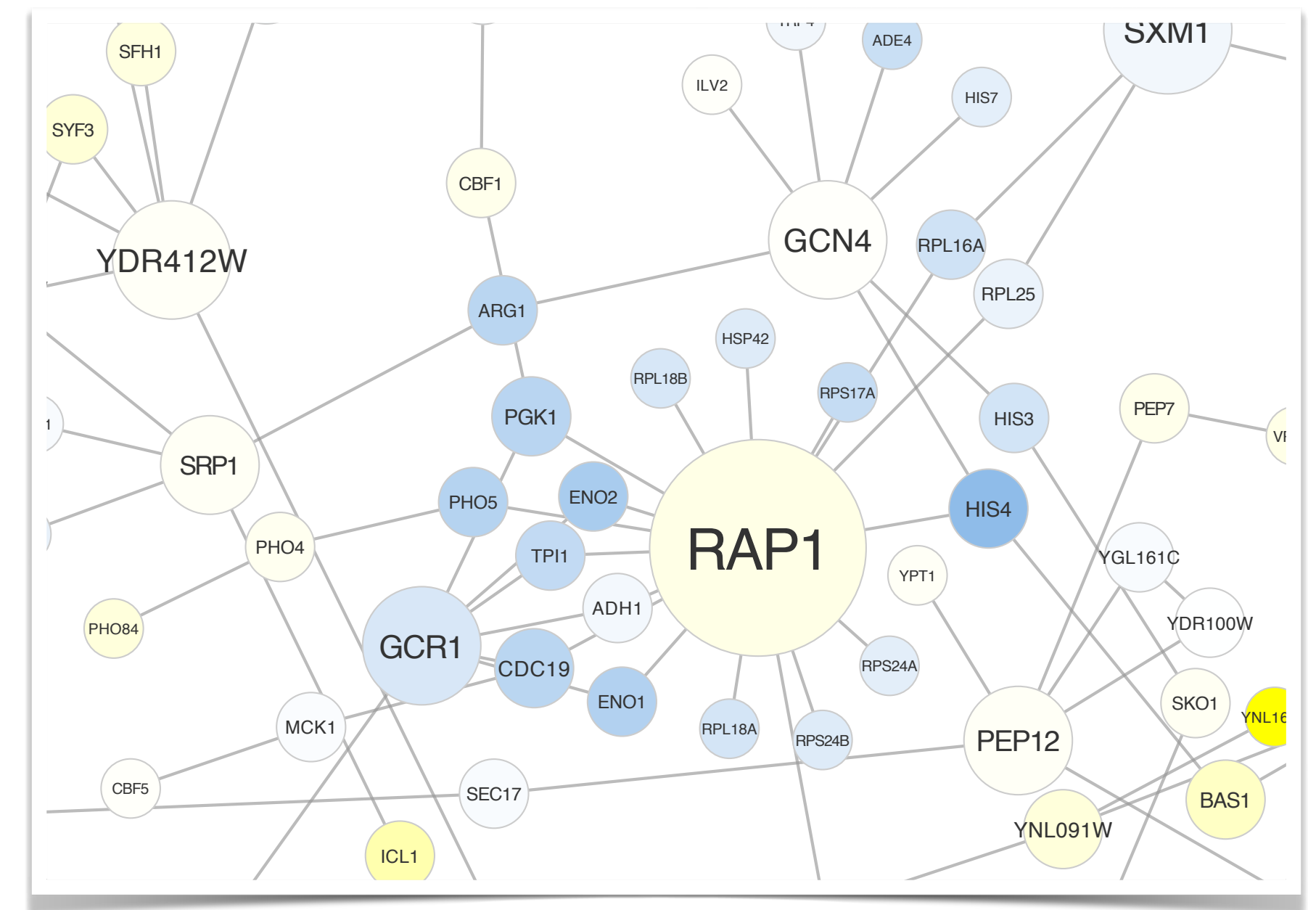
Shape(s)



Size(s)



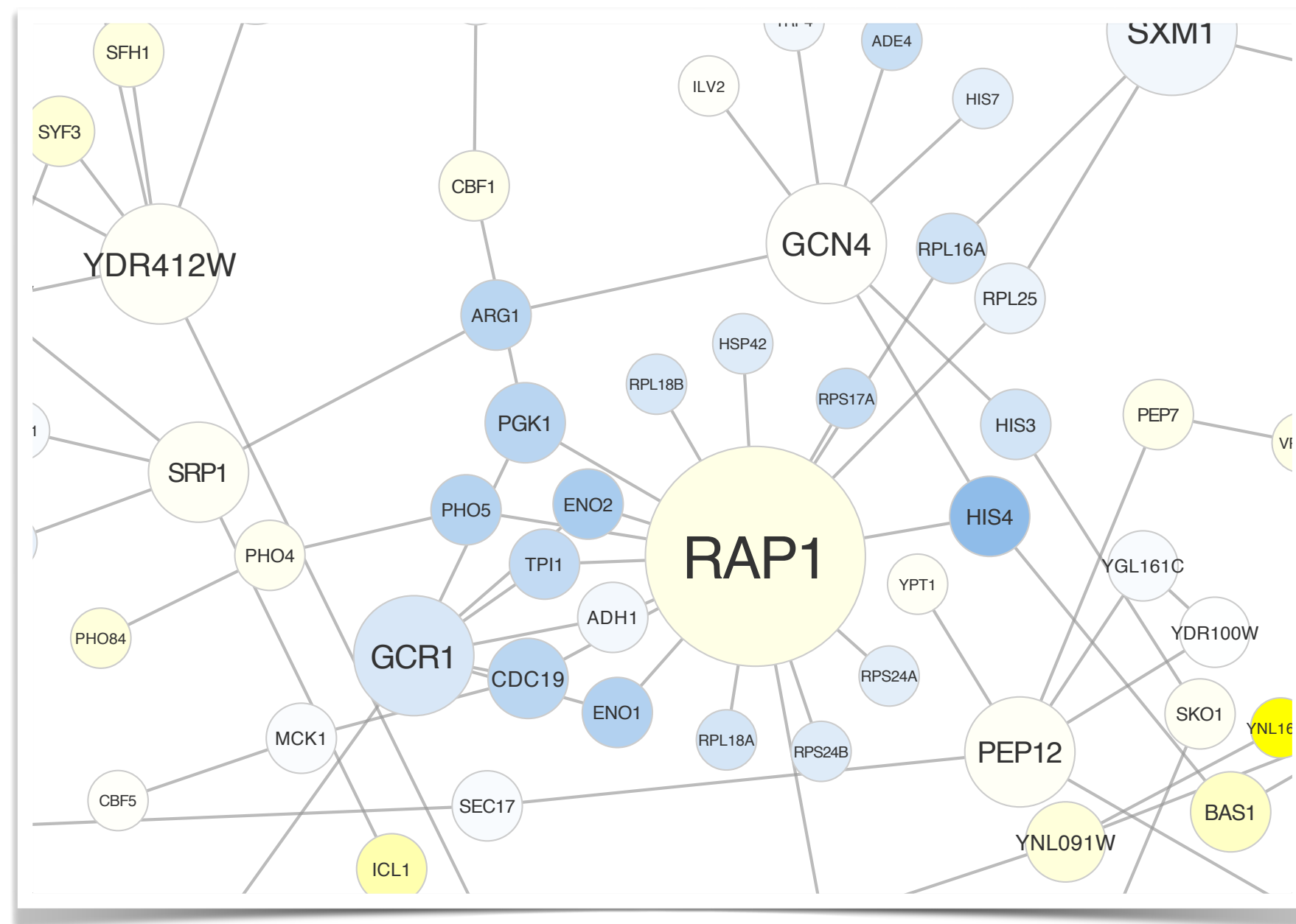
Color(s)



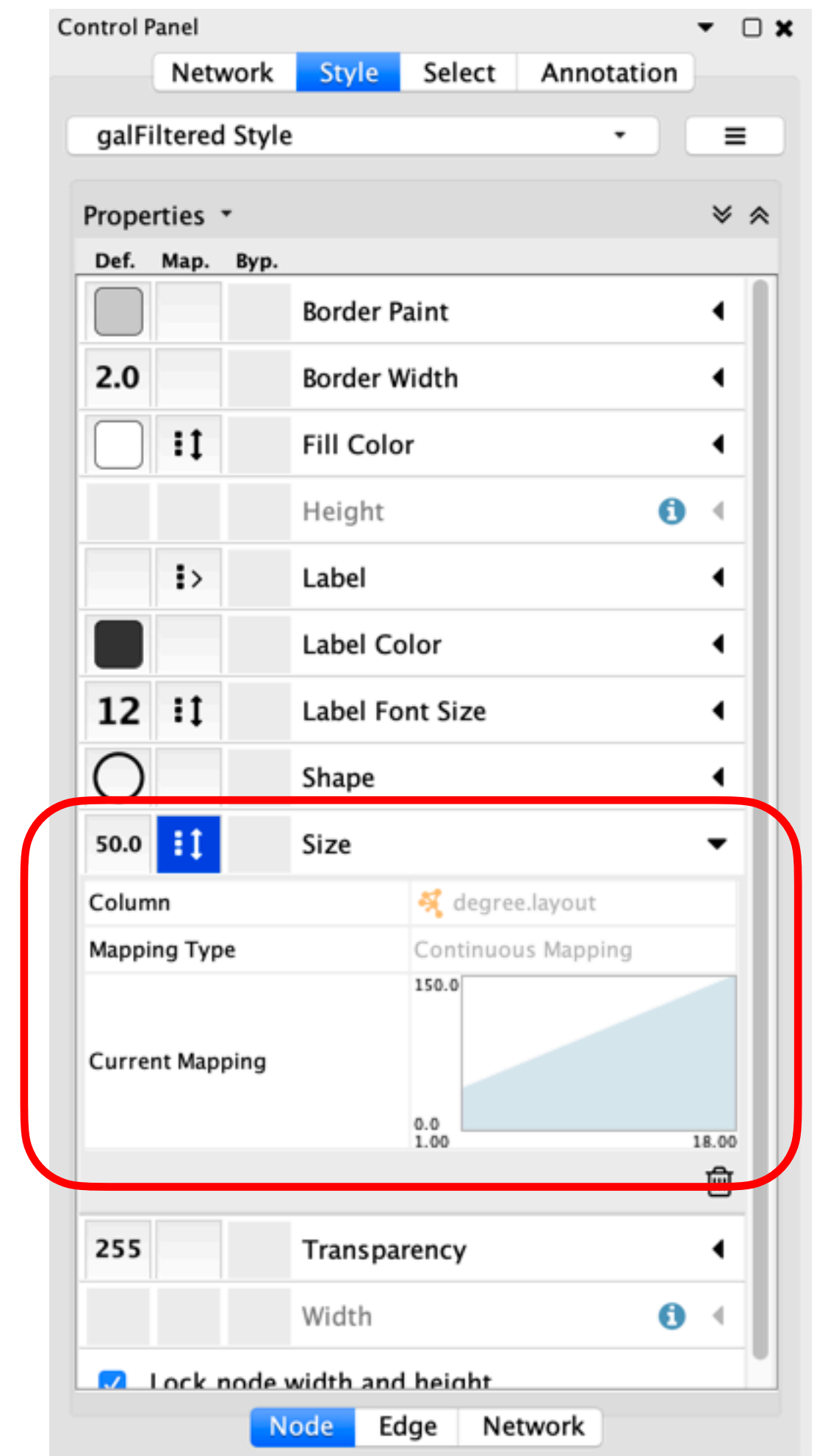
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Cytoscape

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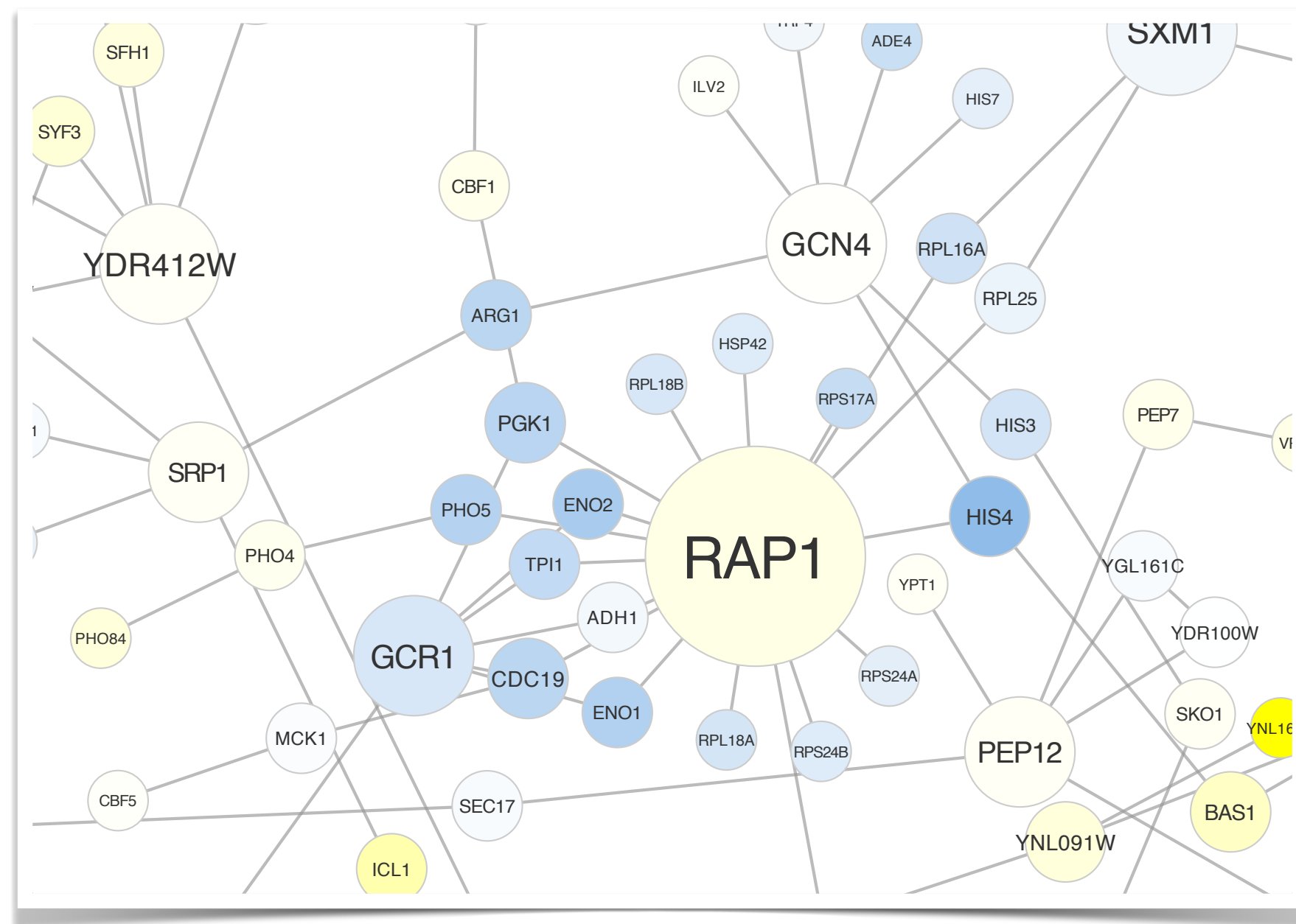
Node size ~ degree



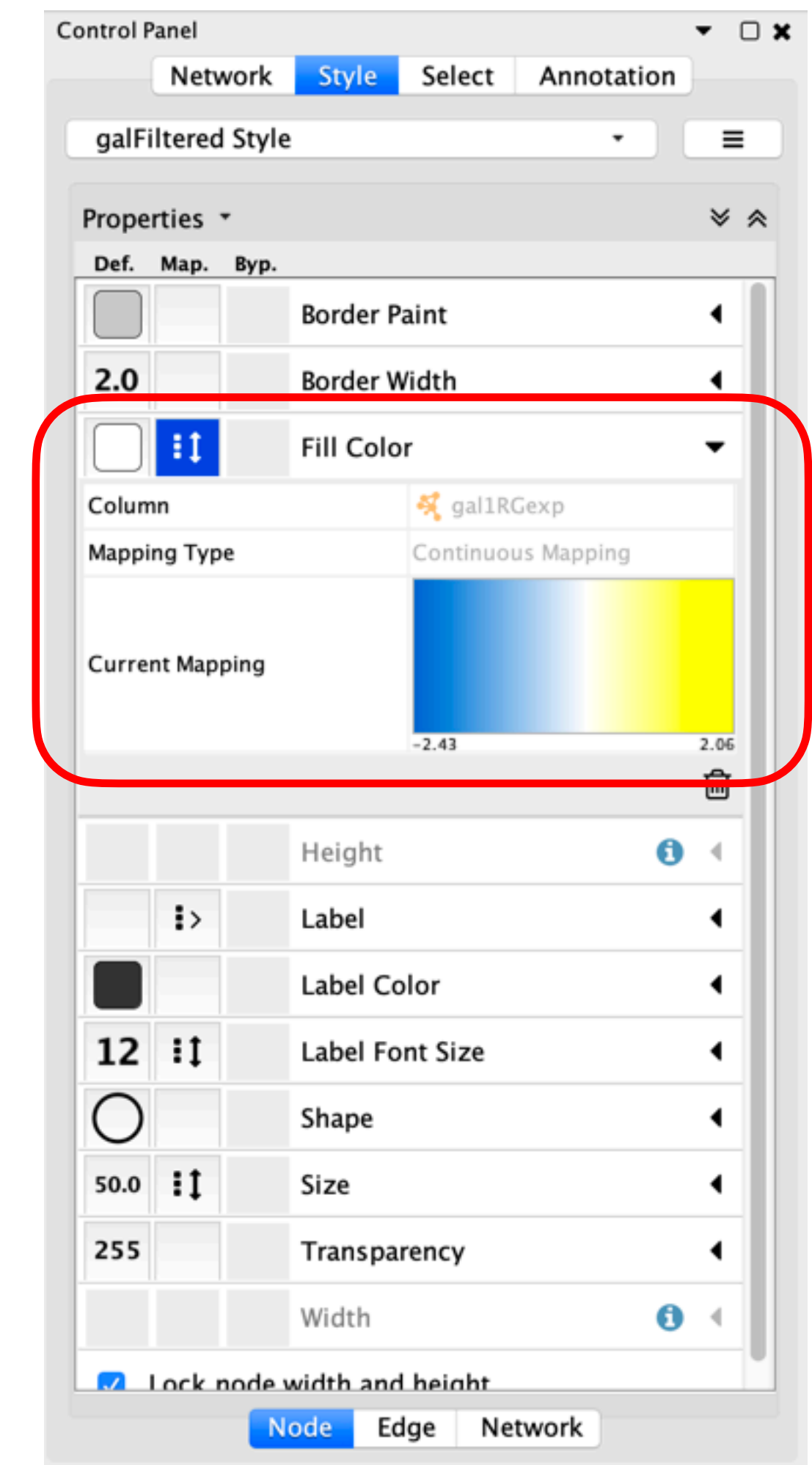
# 2. Node mapper (node2viz)

Cytoscape

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Node color ~ gene expression level



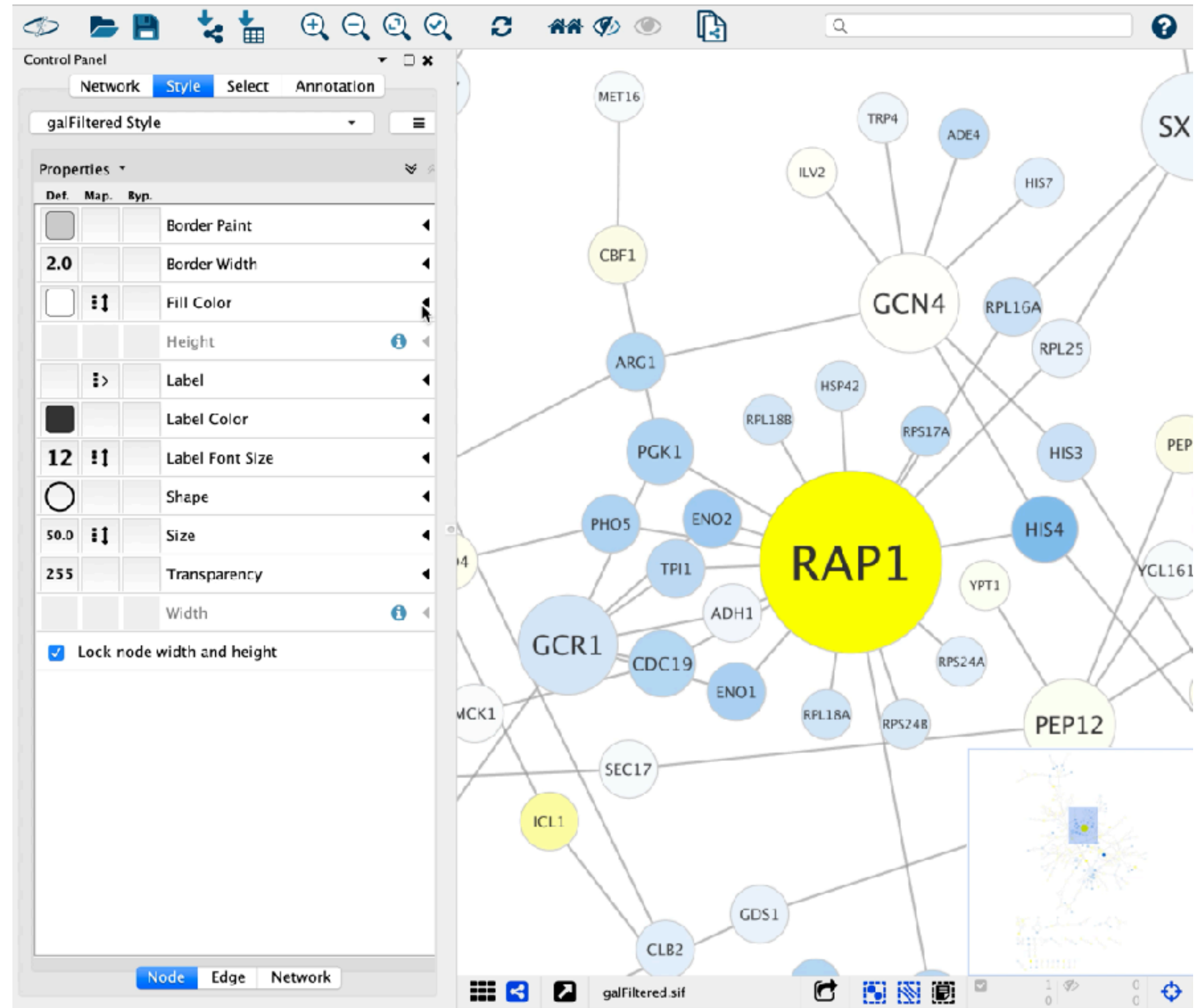
# 3. Link mapper (link2viz)

How to draw links?

Shape(s) | ↓ ↔

Thickness(s) | | |

Color(s) | 





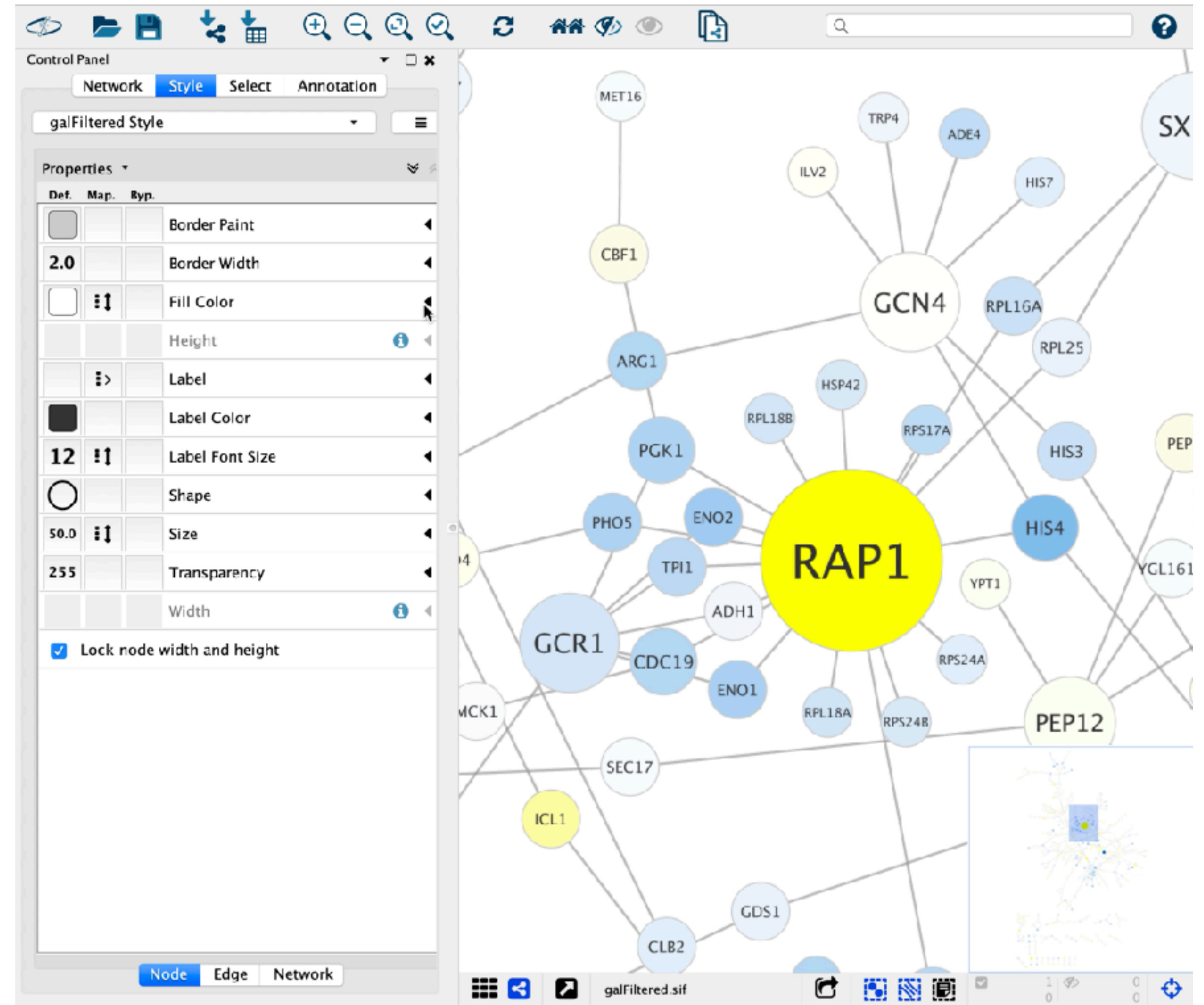
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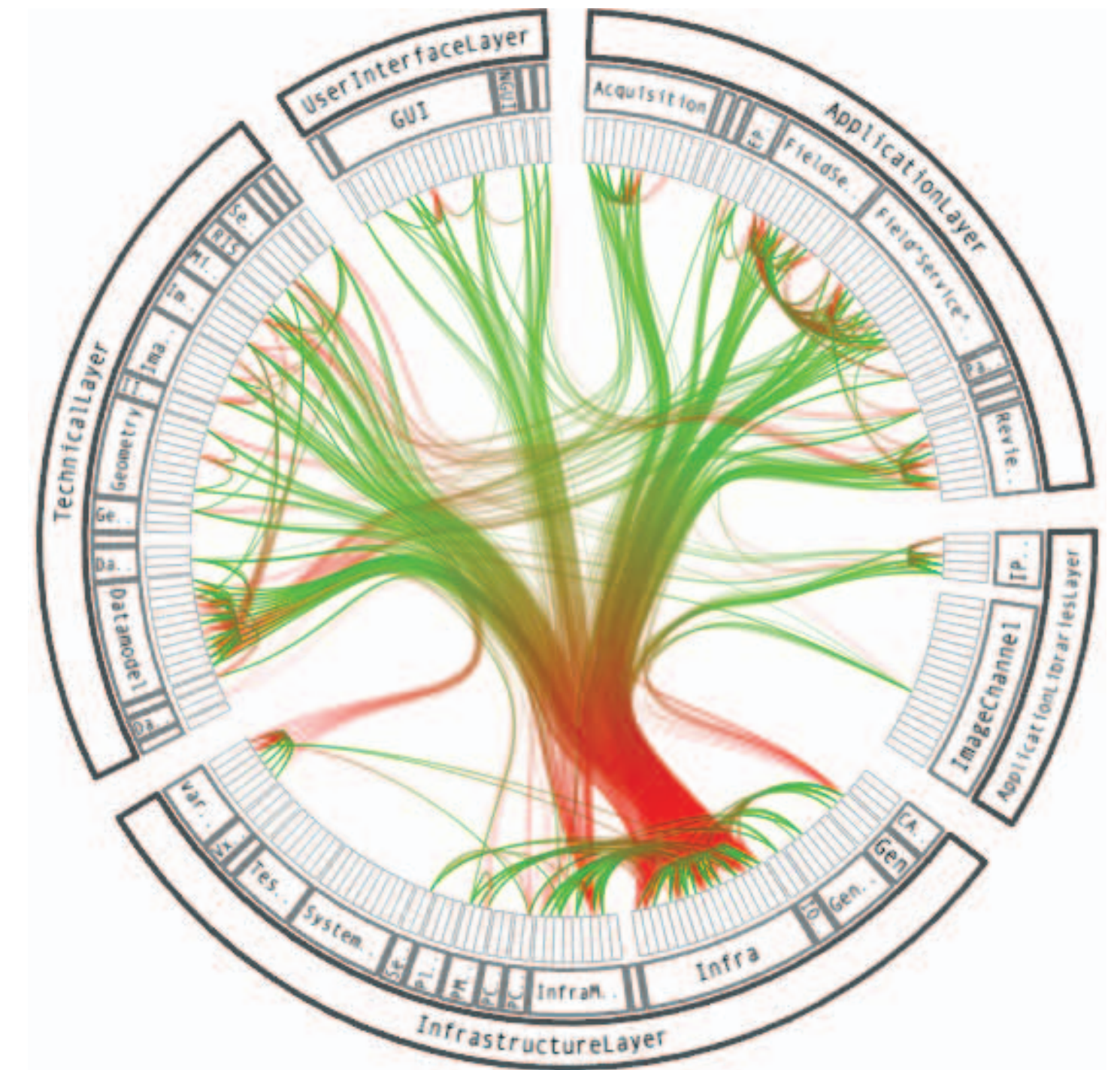
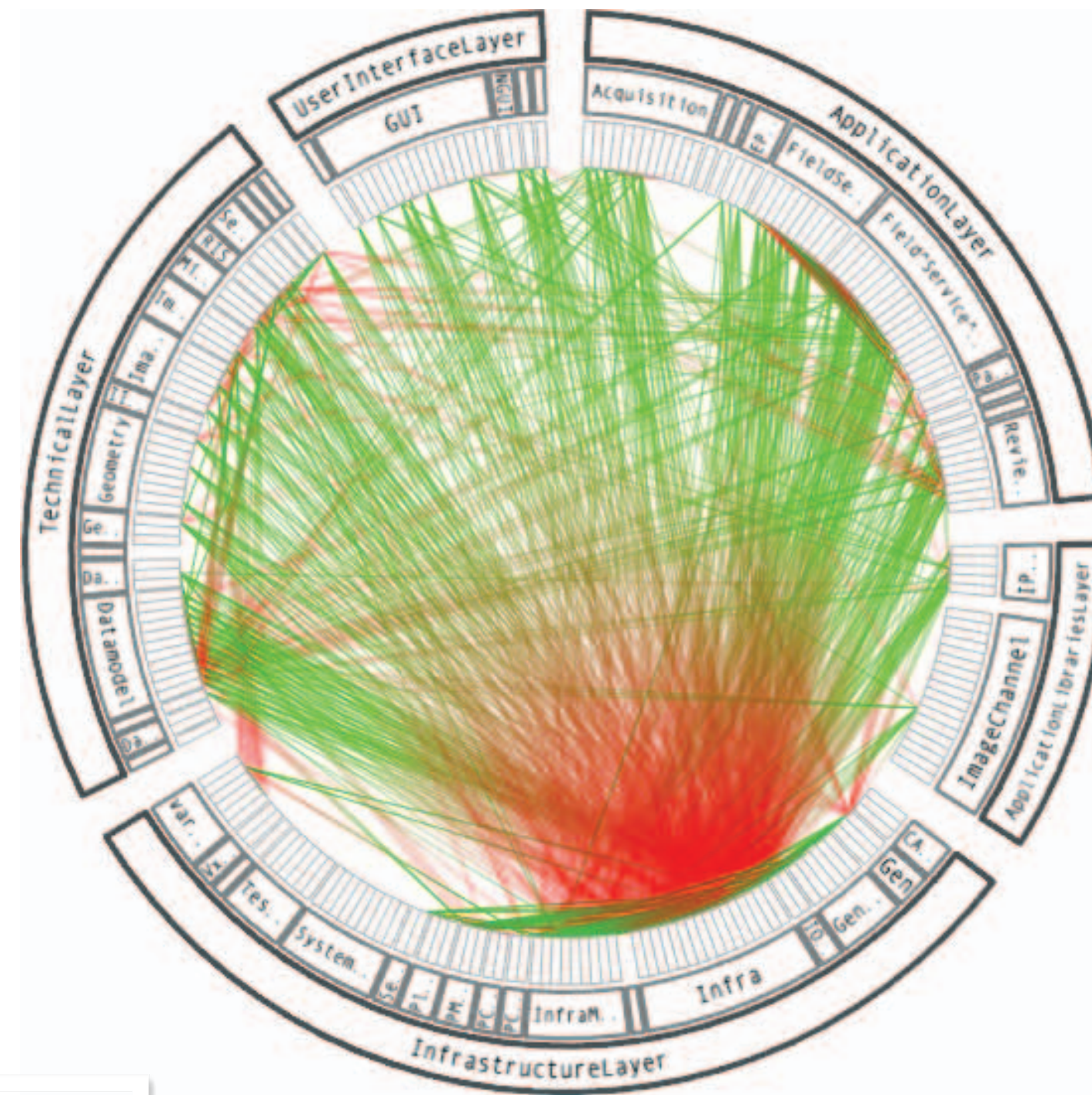
Thickness(s) | |

Color(s) | 



Tip: edges don't need to be straight lines

## Edge bundling



Hierarchical Edge Bundles:  
Visualization of Adjacency Relations in Hierarchical Data

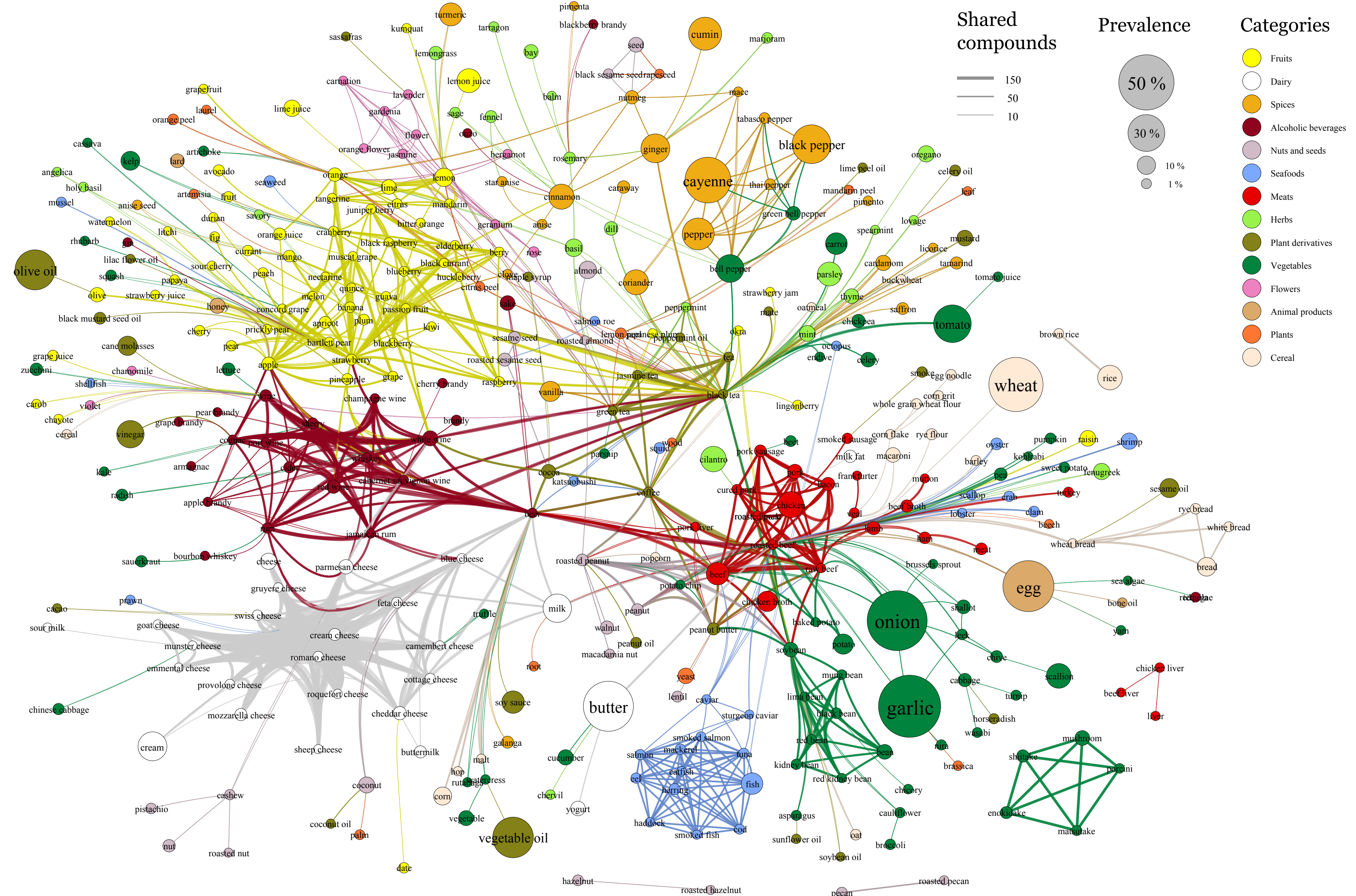
Danny Holten

Holton (2006)

# Flavor Network

Yong-Yeol Ahn, Sebastian Ahnert, James P. Bagrow, and A.-L. Barabási

“Flavor network and the principles of food pairing”, *Scientific Reports* **1**, 196 (2011)



Tip: edges don't need to be straight lines

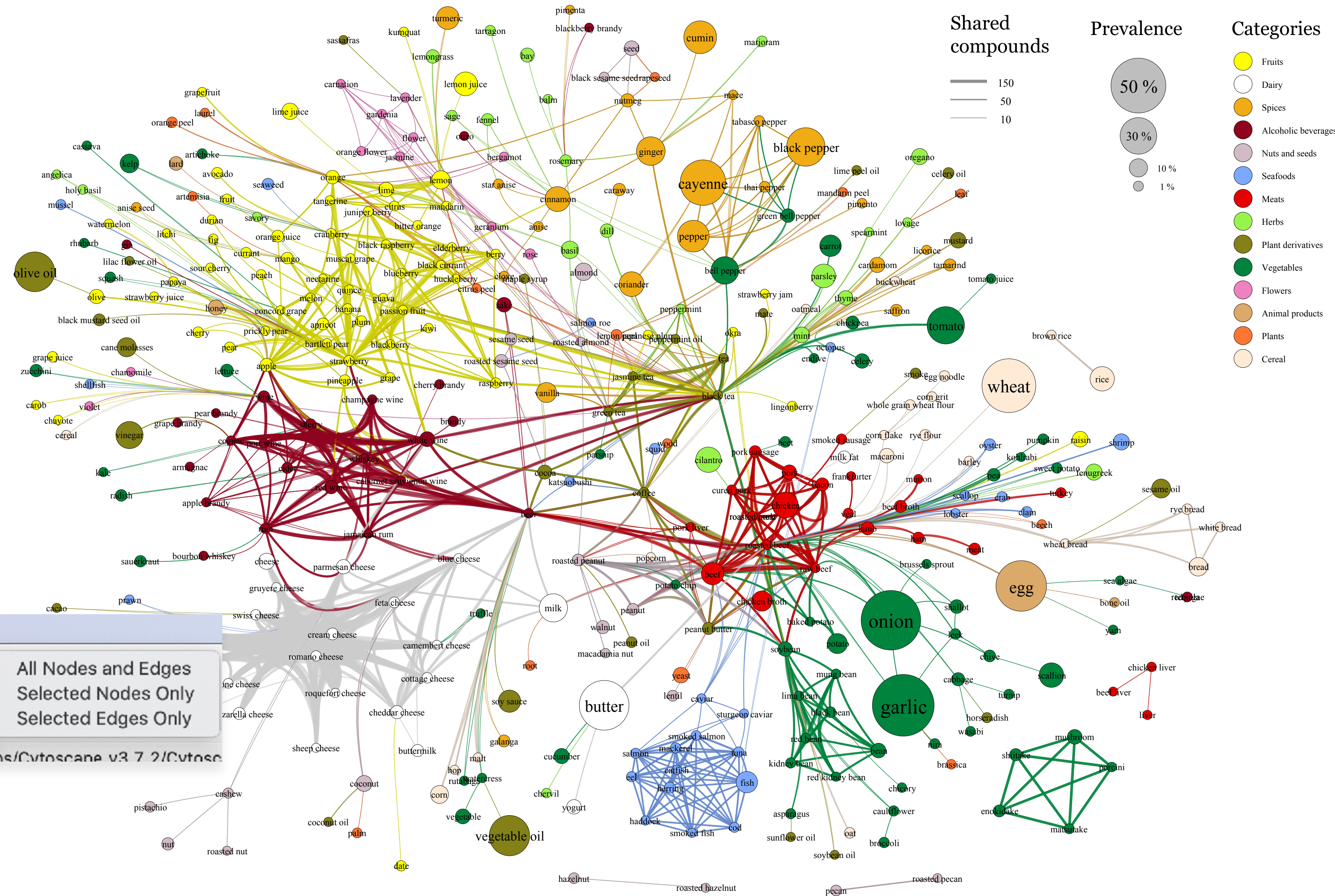
Edge bundling

Flavor network. Culinary ingredients (circles) and their chemical relationship are illustrated. The color of each ingredient represents the food category that the ingredient belongs to, and the size of an ingredient is proportional to the usage frequency (collected from online recipe databases: epicurious.com, allrecipes.com, menupan.com). Two culinary ingredients are connected if they share many flavor compounds. We extracted the list of flavor compounds in each ingredient from the book “Fenaroli’s handbook of flavor ingredients (5th ed.)” and then applied a backbone extraction method by Serrano et al. (*PNAS* **106**, 6483) to pick statistically significant links between ingredients. The thickness of an edge represents the number of shared flavor compounds. To reduce clutter, edges are bundled based on the algorithm by Danny Holten (<http://www.win.tue.nl/~dholten/>).

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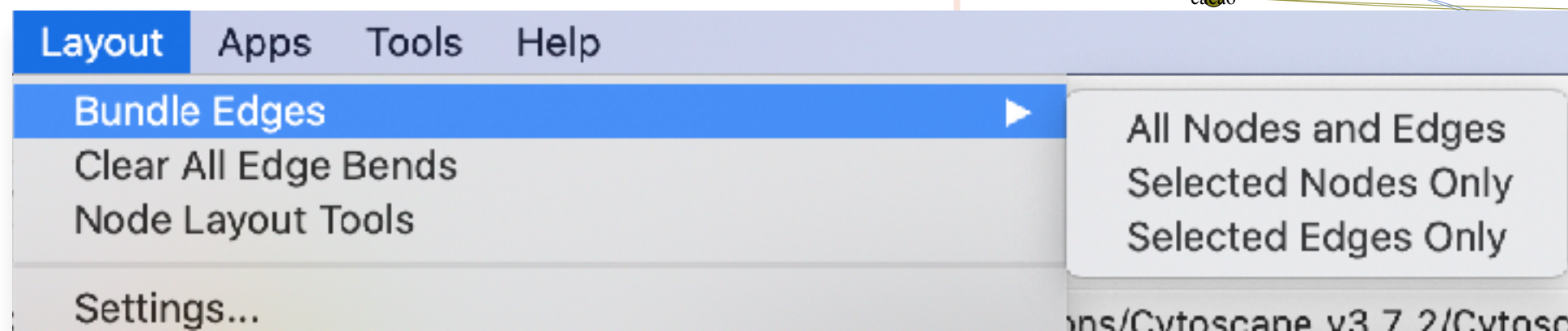
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# Summary

- Basics
  - file formats, code, databases
- Networks from data
  - common tasks and good practices
- Case studies and examples
- Machine learning for data and networks
- Visualization (*time permitting*)

# Challenges

- Hard to automate, generalize data analysis
  - upstream tasks defining the network
  - different fields have different needs
- Many tools, statistics, and algorithms—what to choose? standardize?
- Gap between models and data?
- Error analysis / Uncertainty quantification
- Big data:
  - Gap between research and industry needs
  - Graph databases—tech moving too quickly
  - Visualizations (at scale)

# Working with network data

Jim Bagrow

[james.bagrow@uvm.edu](mailto:james.bagrow@uvm.edu)

[bagrow.com](http://bagrow.com)

Complex Networks

Winter Workshop

2021-01-05



The University  
of Vermont



VERMONT  
COMPLEX SYSTEMS CENTER

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# THANK YOU



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